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**A Recommended Method of Analytically Determining  
the Competence of Hydraulic Telescopic Cantilevered Crane Booms**

**1. Scope**—This analysis applies to crane types as covered by Power Crane and Shovel Association Standard Number Two, Mobile Hydraulic Crane Standards and ANSI B30.15; refer to 5.1.

**1.1 Purpose**—This calculation method has been established to illustrate an analysis to determine the competence of hydraulic telescopic cantilevered crane booms.

**2. References**

**2.1 Applicable Publications**—The following publications form a part of this specification to the extent specified herein.

2.1.1 AISC, "Specification for the Design, Fabrication and Erection of Structural Steel for Buildings," adopted February 12, 1969. In addition, Supplement Nos. 1, 2, 3, and Commentary with additions and revisions where applicable.

2.1.2 AISI, "Specification for the Design of Cold-Formed Steel Structural Members," 1968 edition. In addition, "Commentary on the 1968 Edition," by George Winter and Supplementary Information Part II.

2.1.3 Column Research Council, "Guide to Design Criteria for Metal Compression Members," Second Printing, 1960.

2.1.4 "USS Steel Design Manual," by R. L. Brockenbrough and B. G. Johnston, November 1968 printing.

2.1.5 ANSI B30.15

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2.1.6 NOMENCLATURE

- a =Clear distance between transverse stiffeners on side plate; also the ratio of the material yield of the web to the material yield of the compression flange
- A =Actual area of section
- A<sub>e</sub> =Total effective area of section used in calculating F<sub>a</sub> (refer to Appendix E for illustration)
- A<sub>f</sub> =Area of compression flange
- A<sub>i</sub> =Area based on inside dimensions of section (refer to Appendix E for illustration)
- A<sub>m</sub> =Area based on mean dimensions of section (refer to Appendix E for illustration)
- A<sub>o</sub> =Area based on outside dimensions of section (refer to Appendix E for illustration)
- A<sub>st</sub> =Cross-sectional area of stiffener or pair of stiffeners
- A<sub>w</sub> =Area of both webs
- b =Actual width of stiffened and unstiffened compression elements whether flange or web (refer to Appendix F for illustration)
- b<sub>e</sub> =Effective width of stiffened compression element (refer to Appendix E for illustration)
- b<sub>f</sub> =Actual flange width (refer to Appendix E for illustration)
- b<sub>m</sub> =Mean width of section or b<sub>w</sub> - t<sub>w</sub> (refer to Appendix E for illustration)
- b<sub>w</sub> =Overall width of section (refer to Appendix E for illustration)
- C<sub>t</sub> =Distance from neutral axis to extreme tension fiber of box section (refer to Appendix E for illustration)
- C<sub>c</sub> =Distance from neutral axis to compressive fiber of box section (refer to Appendix E for illustration)
- C<sub>b</sub> =Bending coefficient dependent upon moment gradient; equal to (see Equation 1)

$$1.75 + 1.05 \left( \frac{M_{x\min}}{M_{x\max}} \right) + 0.3 \left( \frac{M_{x\min}}{M_{x\max}} \right)^2 \quad (\text{Eq. 1})$$

but not more than 1.3 (refer to Appendix C for illustration)

C<sub>c</sub> =Column slenderness ratio dividing elastic and inelastic buckling equal to (see Equation 2)

$$\sqrt{\pi^2 E / (F_y - \sigma_{rc})} \quad (\text{Eq. 2})$$

C'<sub>c</sub> =Effective column slenderness ratio dividing elastic and inelastic buckling equal to (see Equation 3)

$$\sqrt{\frac{\pi^2 E}{Q_s Q_a (F_y - \sigma_{re})}} \quad (\text{Eq. 3})$$

C<sub>m</sub> =Coefficient applied to bending term in the interaction formula and dependent upon column curvature caused by applied moments; use 0.85

C<sub>mx</sub> =0.85

C<sub>my</sub> =0.85

C<sub>v</sub> =Ratio of "critical" web stress, according to linear buckling theory, to the shear yield stress of web material

d =Overall depth of section (refer to Appendix E for illustration)

D =Factor depending upon type of transverse stiffeners

E =Modulus of elasticity 29 500 ksi

f =Computed axial and bending compression stress on appropriate flange or web

f<sub>a</sub> =Computed axial stress based on total section area

f<sub>b</sub> =Computed bending stress about the appropriate axis

f<sub>c</sub> =Sum of the computed axial and side bending compressive stresses

f<sub>bx</sub> =Computed bending stress about the x-x axis

f<sub>by</sub> =Computed bending stress about the y-y axis

f<sub>s</sub> =Sum of the computed torsional and vertical shear stress

f<sub>v</sub> =Computed average web or flange shear stress

f<sub>vs</sub> =Total shear transfer of stiffener(s), kips per inch of length

F<sub>a</sub> =Allowable axial stress permitted in the absence of a bending moment

F<sub>b</sub> =Allowable bending stress for the appropriate axis

F<sub>bx</sub> =Allowable bending stress about the x-x axis if this bending moment alone existed

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$F'_{bx}$  =Allowable bending stress in compression flange of box sections as reduced for hybrid sections or because of large web depth-to-thickness ratio  
 $F'_{by}$  =Allowable bending stress about the y-y axis if this bending moment alone existed  
 $F'_e$  =Euler stress divided by factor of safety; equal to (see Equation 4)

$$\frac{12\pi^2 E}{23(Kl/r)^2} \quad (\text{Eq. 4})$$

$F'_{ex}$  =Same as  $F'_e$  about the x-x axis  
 $F'_{ey}$  =Same as  $F'_e$  about the y-y axis  
 $F_v$  =Allowable web shear stress  
 $F_y$  =Specified minimum yield stress of material being used, based on "yield stress" or yield strength, whichever is applicable  
 $g$  =Wind load, lb/in<sup>2</sup>,  $g = 0.004 (\text{mph})^2/144$   
 $G$  =Shear modulus of elasticity 11 300 ksi  
 $h$  =Clear distance between flanges (refer to Appendix E for illustration)  
 $h_m$  =Mean height of section  $d - (t_c + t_t)/2$  (refer to Appendix E for illustration)  
 $h_v$  =Vertical height of horizontal stiffener  
 $H_o$  =Height to boom foot pin from ground  
 $H_p$  =Height to center of pressure on boom  
 $H_r$  =Reference height at which wind velocity is measured (20 ft in U.S.)  
 $I_x$  =Area moment of inertia about the x-x axis  
 $I_y$  =Area moment of inertia about the y-y axis  
 $I_{st}$  =Moment of inertia of a pair of intermediate stiffeners, or a single intermediate stiffener, with reference to an axis in the plane of the web  
 $I_{xe}$  =Effective moment of inertia about the x-x axis  
 $I_{ye}$  =Effective moment of inertia about the y-y axis  
 $J$  =Torsional constant; equal to (refer to Appendix D for other equations) (see Equation 5)

$$\frac{4(b_m)^2(h_m)^2}{\frac{2h_m}{t_w} + \frac{b_m}{t_c} + \frac{b_m}{t_t}} \quad (\text{Eq. 5})$$

$k$  =Coefficient relating linear buckling strength of a plate to its dimensions and conditions of edge support  
 $K$  =Effective length factor, for cantilevered section use the value 2 unless a smaller one can be justified  
 $K_t$  =Torsional length factor for cantilevered sections, use the value 4/3  
 $l$  =Dimensional lengths of boom  
 $L$  =Distance from tip to section in question  
 $L_b$  =Actual unbraced length of section in the plane of bending  
 $M$  =Bending moment about the appropriate axis  
 $M_1$  =Constant moment load about the x-x axis resulting from eccentric loading on the head  
 $M_2$  =Constant moment load about the y-y axis resulting from the side loading on the head  
 $M_{x\min}$  =Smaller moment at end of unbraced length of beam-column at tip  
 $M_{x\max}$  =Larger moment at end of unbraced length of beam-column at section in question  
 $M_x$  =Bending moment about the x-x axis  
 $M_y$  =Bending moment about the y-y axis  
 $N$  =Number of parts of line  
 $p$  =Wind velocity exponent  
 $P$  =Externally applied load at the tip  
 $P_a$  =Axial load applied to section  
 $P_x$  =Lateral loading component (side load)  
 $P_y$  =Vertical loading component  
 $P_z$  =Axial loading component  
 $Q_a$  =Ratio of effective profile area of an axially loaded member to its total profile area of  $A_e/A$   
 $Q_s$  =Axial stress reduction factor for unstiffened elements of a section; refer to Appendix F

$r$  =Radius of gyration for appropriate axis  
 $r_b$  =Radius of gyration about the axis of concurrent bending, computed on the basis of actual cross-sectional area  
 $R$  =Load radius from centerline of rotation to centerline of load  
 $R_h$  =Hoist cylinder reaction  
 $R_x$  =Reaction loads in the lateral direction  
 $R_y$  =Reaction loads in the vertical direction  
 $R_z$  =Reaction loads in the axial direction  
 $S_x$  =Strong axis section modulus with  $c$  taken to the compressive side  
 $S_y$  =Weak axis section modulus with  $c$  taken to the compressive side  
 $S_{xe}$  =Effective strong axis section modulus with  $c$  taken to the compressive side  
 $S_{ye}$  =Effective weak axis section modulus with  $c$  taken to the compressive side  
 $t$  =Thickness of flange or web in compression (refer to Appendix E for illustration)  
 $t_c$  =Thickness of compression flange (refer to Appendix E for illustration)  
 $t_t$  =Thickness of tension flange (refer to Appendix E for illustration)  
 $t_w$  =Thickness of web (refer to Appendix E for illustration)  
 $T$  =Torsional moment  
 $V_p$  =Wind velocity (mph) at center of pressure height  $H_p$   
 $V_r$  =Wind velocity (mph) at reference height  $H_r$   
 $V_x$  =Statical shear load on section in the lateral direction  
 $V_y$  =Statical shear load on section in the vertical direction  
 $w$  =Component weight, lb/in  
 $W$  =Total component weight  
 $x$  =Subscript relating symbol to strong axis bending  
 $Y$  =Ratio of yield stress of web steel to that of yield stress of stiffener steel  
 $y$  =Subscript relating symbol to weak axis bending  
 $z$  =Subscript relating symbol to axial loading  
 $\alpha$  =Boom centerline elevation angle relative to a horizontal plane, or the ratio of web yield stress to flange yield stress  
 $\theta$  =Angle between a line perpendicular to the boom axis and the hoist cylinder axis  
 $\sigma_{rc}$  =Residual compressive stress, equal to  $0.5 F_y$  in lieu of specific information on steel used  
 $u$  =Poisson's ratio—equal to 0.3

3. **Criteria**—Calculations shall include the dead weight loads, rated load and a minimum side load of 2% of the rated load at the rated load radius. The side load provides for "normal" conditions of machine operation. In addition, the effect of the wind on the boom should be considered, as is provided for in the calculations.

3.1 The factors of safety used herein are the recommended factors of the AISC "Specification for the Design, Fabrication and Erection of Structural Steel for Buildings," adopted February 12, 1969.

3.2 The boom shall be deemed competent when the solution of the interaction equations provided herein yield a value equal to or less than one (1.0).

#### 4. **Loads and Forces**

4.1 The 2% side load provides for "normal" conditions of boom motion. No allowances have been made for dynamic loads, duty cycle operation, effects of the wind on the load lifted or operations other than lifting crane service.

4.2 All forces and loads are expressed in pounds. Dimensions are in inches. Stresses both allowable and calculated are in units of ksi. Also, the modulus of elasticity is expressed in units of ksi.

## 5. Analytical Determination of Stresses and Critical Loads

**5.1 Applicability**—This analysis is applicable to multisectioned "box" type booms, which are totally enclosed and cantilevered beyond the base section.

**5.2 Basis for Analysis**—The equations presented in this analysis are based on laterally unsupported beam column formulas, the solution of which are combined in interaction equations. In determining the section properties, the effective width of the plates in compression are used. The areas covered in this analysis consist of axial and torsional loading, bidirectional bending, and panel buckling. Of primary importance in the analysis are the compressive stress calculations.

The work of this committee is not intended to cover all design concepts, but rather a basic system. However, other design configurations may use alternative calculation methods when substantiated with suitable test data.

**5.3 Summary**—Where strain gage results are available they should be used to supplement the analytical data.

## 6. Load Moment Diagrams and Equations

### 6.1 Assumptions Used on Load Moment Equations

- 6.1.1 Wind force is negligible on head (should include effects if jib used).
- 6.1.2 Torque is created by the side load P on the head (would also be applicable for a jib).
- 6.1.3 Equations are still applicable if jib used but dimensions, weights, and center of gravity to be adjusted accordingly.
- 6.1.4  $P_y = P \cos \alpha$ ;  $P_z = P \sin \alpha$
- 6.1.5 Winch rope fleet angle and angle relative to boom is negligible.
- 6.1.6 Wind force is uniformly distributed along the exposed length of the side of the section with its reaction at the center (is a valid assumption since each section considered individually).
- 6.1.7 That the dimensions are to the reaction points and that the tips of each section beyond these points are small in length and will not affect the validity of the equations.
- 6.1.8 That the axial stresses produced by the friction forces due to the section reaction points from one to the next are small in comparison to the other stresses, that the section support cylinders carry the axial loads.
- 6.1.9 That equations and formulations appearing in the foregoing analysis are for the boom in the extended position —Figure 1, Figure 2, Figure 3, Figure 4, Figure 5, Figure 6, Figure 7. Partially retracted positions will require reformulation of some equations; as an example in Figure 4 when  $I_{11}$  is zero or negative the cylinder no longer takes the axial load at the section being considered. The moment equations would then appear as those written for reference Figure 3. Similar changes would appear in the axial load, reactions, and shear force equations.

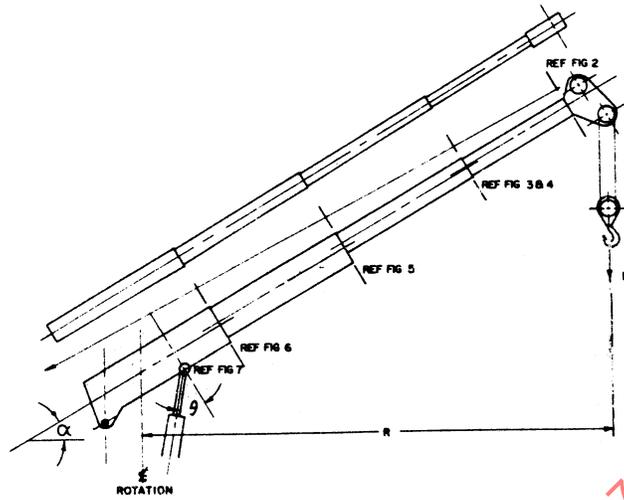


FIGURE 1—LOADING DIAGRAM—BOOM ASSEMBLY

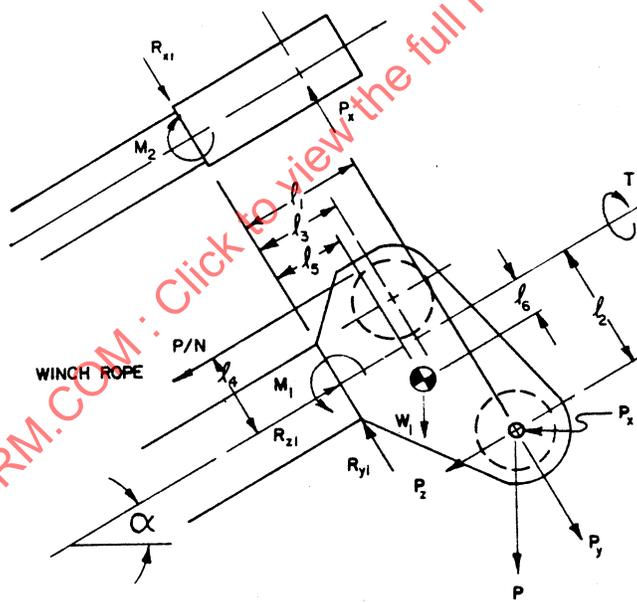


FIGURE 2—LOAD MOMENT DIAGRAM—HEAD SECTION

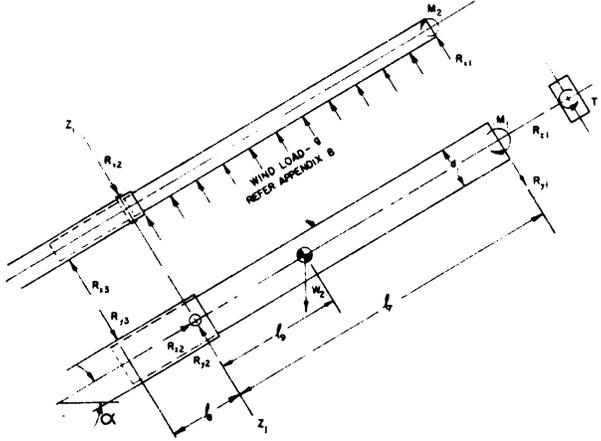


FIGURE 3—LOAD MOMENT DIAGRAM—TIP SECTION

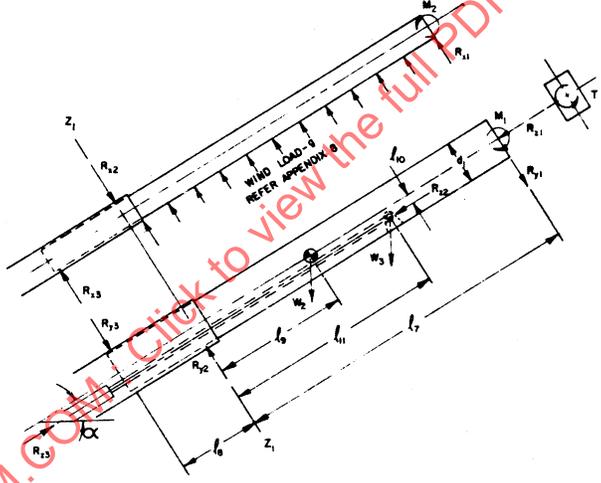


FIGURE 4—LOAD MOMENT DIAGRAM—ALTERNATE TIP SECTION

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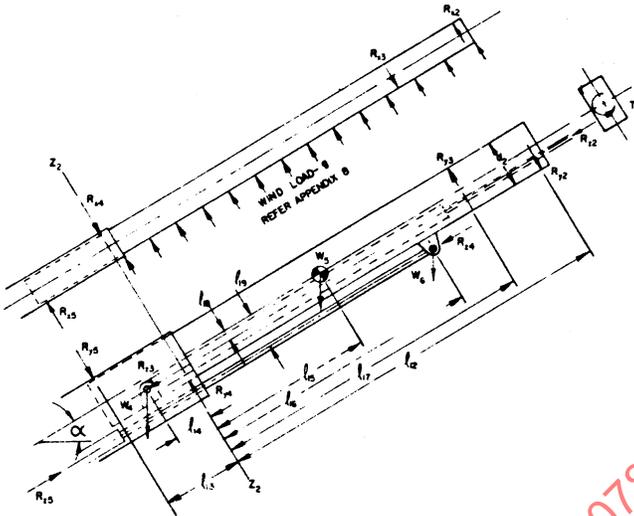


FIGURE 5—LOAD MOMENT DIAGRAM—INTERMEDIATE SECTION

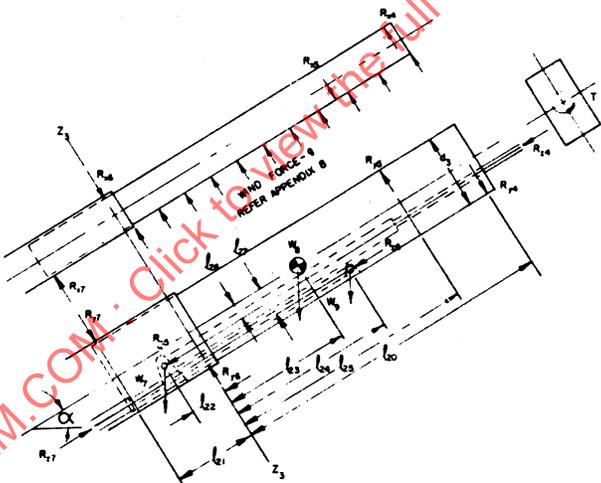


FIGURE 6—LOAD MOMENT DIAGRAM—INTERMEDIATE SECTION

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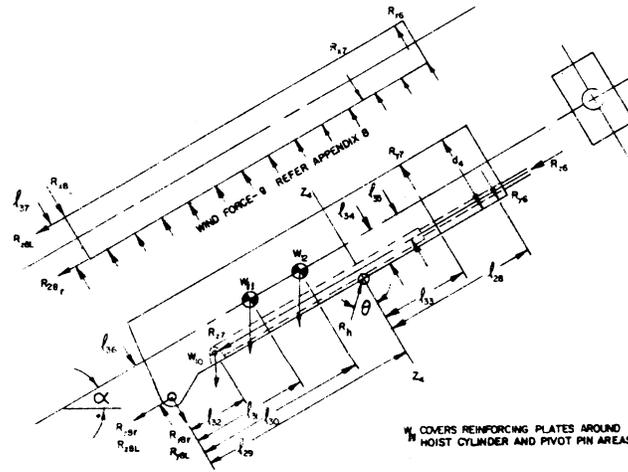


FIGURE 7—LOAD MOMENT DIAGRAM—BASE SECTION

**6.2 Refer Figure 2—Load Moment Equations—Reaction of Head Forces on Tip Section** (see Equations 6, 7, 8, and 9)

MOMENT (Equation 6)

$$\begin{aligned}
 M_1 &= P_y l_1 + P_z l_2 - P/N l_4 + W_1 [l_5 \cos \alpha + l_6 \sin \alpha] \\
 M_2 &= P_x l_1 \\
 T &= P_x l_2
 \end{aligned}
 \tag{Eq. 6}$$

AXIAL LOAD (Equation 7)

$$R_{z1} = P/N + P_z + W_1 \sin \alpha \tag{Eq. 7}$$

SHEAR LOADS (Equation 8)

$$\begin{aligned}
 V_x &= -R_{x1} = P_x \\
 V_y &= -R_{y1} = W_1 \cos \alpha + P_y
 \end{aligned}
 \tag{Eq. 8}$$

SIDE LOAD (Equation 9)

$$P_x = 0.02P \tag{Eq. 9}$$

**6.3 Refer Figure 3—Load Moment Equations for Tip Section at Section Z<sub>1</sub> - Z<sub>1</sub>** (see Equations 10, 11, 12, 13, 14, 15, and 16)

MOMENTS (Equation 10)

$$M_x = M_1 + R_{y1}l_7 + \frac{0.5W_2 \cos \alpha l_7^2}{1_7 + 1_8} \quad (\text{Eq. 10})$$

$$M_y = M_2 + R_{x1}l_7 + 0.5gd_1 l_7^2$$

$$T = P_x l_2$$

AXIAL LOAD ON PIN (Equation 11)

$$P_{z2} = P_{z1} + W_2 \sin \alpha \quad (\text{Eq. 11})$$

AXIAL LOAD ON SECTION (Equation 12)

$$P_{ar} = R_{z1} + W_2 \sin \alpha \frac{l_7}{1_7 + 1_8}; P_{aL} = W_2 \sin \alpha \frac{l_8}{1_7 + 1_8} \quad (\text{Eq. 12})$$

VERTICAL REACTIONS (Equation 13)

$$R_{y3} = \frac{M_x}{l_8} - 0.5W_2 \cos \alpha \frac{l_8}{1_7 + 1_8}; R_{y2} = R_{y1} + R_{y3} + W_2 \cos \alpha \quad (\text{Eq. 13})$$

LATERAL REACTIONS (Equation 14)

$$R_{x3} = \frac{M_y}{l_8}; R_{x2} = R_{x1} + R_{x3} + gd_1 l_7 \quad (\text{Eq. 14})$$

VERTICAL SHEAR FORCES (Equation 15)

$$V_{yr} = R_{y1} + W_2 \cos \alpha \frac{l_7}{1_7 + 1_8}; V_{yL} = R_{y3} + W_2 \cos \alpha \frac{l_8}{1_7 + 1_8} \quad (\text{Eq. 15})$$

LATERAL SHEAR FORCES (Equation 16)

$$V_{xr} = R_{x1} + gd_1 l_7; V_{xL} = R_{x3} \quad (\text{Eq. 16})$$

NOTE— Subscripts r and L refer to right and left of Section Z<sub>1</sub> - Z<sub>1</sub>

**6.4 Refer Figure 4—Load Moment Equations for Alternate Tip Section at Section Z<sub>1</sub> - Z<sub>1</sub>** (see Equation 17, Equation 18, Equation 19, Equation 20, Equation 21, Equation 22, Equation 23)

MOMENTS (Equation 17)

$$M_x = M_1 + R_{y1}1_7 + 0.5W_2 \cos \alpha \frac{1_7^2}{1_7 + 1_8} + W_3 \cos \alpha 1_{11} \mp R_{x2}1_{10} \quad (\text{Eq. 17})$$

$$M_y = M_2 + R_{x1}1_7 + 0.5gd_1 1_7^2$$

$$T = P_x 1_2$$

AXIAL LOAD ON CYLINDER SUPPORT (Equation 18)

$$R_{z2} = R_{z1} + W_2 \sin \alpha \quad (\text{Eq. 18})$$

AXIAL LOAD ON SECTION (Equation 19)

$$P_{ar} = P_{aL} = \frac{W_2 1_8}{1_7 + 1_8} \sin \alpha \quad (\text{Eq. 19})$$

VERTICAL REACTIONS (Equation 20)

$$R_{y3} = \frac{M_x}{1_8} - 0.5W_2 \cos \alpha \frac{1_8}{1_7 + 1_8}; R_{y2} = R_{y1} + R_{y3} + W_2 \cos \alpha + W_3 \cos \alpha \quad (\text{Eq. 20})$$

LATERAL REACTIONS (Equation 21)

$$R_{x3} = \frac{M_y}{1_8}; R_{x2} = R_{x1} + R_{x3} + gd_1 1_7 \quad (\text{Eq. 21})$$

VERTICAL SHEAR FORCES (Equation 22)

$$V_{yr} = R_{y1} + W_2 \cos \alpha \frac{1_7}{1_7 + 1_8} + W_3 \cos \alpha; V_{yL} = R_{y3} + W_2 \cos \alpha \frac{1_8}{1_7 + 1_8} \quad (\text{Eq. 22})$$

LATERAL SHEAR FORCES (Equation 23)

$$V_{xr} = R_{x1} + gd_1 1_7; V_{xL} = R_{x3} \quad (\text{Eq. 23})$$

NOTE—Subscripts r and L refer to right and left of Section Z1 - Z1

**6.5 Refer Figure 5—Load Moment Equations for Intermediate Section at Section Z<sub>2</sub> - Z<sub>2</sub>** (see Equation 24, Equation 25, Equation 26, Equation 27, Equation 28, Equation 29, Equation 30)

MOMENTS (Equation 24)

$$M_x = R_{y2}1_{12} - R_{y3}1_{17} + W_6 \cos \alpha 1_{16} + 0.5W_5 \cos \alpha \frac{1_{12}^2}{1_{12} + 1_{13}} \mp W_5 \sin \alpha 1_{19} \mp P_{x3}(1_{19} - 1_{18}) \quad (\text{Eq. 24})$$

$$M_y = R_{x2}1_{12} - R_{x3}1_{17} + 0.5gd_2 1_{12}^2$$

$$T = P_x 1_2$$

AXIAL LOAD ON CYLINDER SUPPORTS (Equation 25)

$$R_{z3} = R_{z2} + (W_3 + W_4) \sin \alpha; R_{z4} = R_{z3} + W_5 \sin \alpha \quad (\text{Eq. 25})$$

AXIAL LOAD ON SECTION (Equation 26)

$$P_{ar} = P_{aL} = R_{z3} + W_5 \sin \alpha \frac{1_{13}}{1_{12} + 1_{13}} \quad (\text{Eq. 26})$$

VERTICAL REACTIONS (Equation 27)

$$R_{y5} = \frac{M_x}{1_{13}} - W_4 \cos \alpha \frac{1_{14}}{1_{13}} - 0.5W_5 \cos \alpha; R_{y4} = R_{y2} - R_{y3} + R_{y5} + \cos \alpha (W_4 + W_5 + W_6) \quad (\text{Eq. 27})$$

LATERAL REACTIONS (Equation 28)

$$R_{x5} = \frac{M_y}{1_{13}}; R_{x4} = R_{x2} - R_{x3} + R_{x5} + g d_2 1_{12} \quad (\text{Eq. 28})$$

VERTICAL SHEAR FORCES (Equation 29)

$$V_{yr} = R_{y2} - R_{y3} + W_y \cos \alpha + W_5 \cos \alpha \frac{1_{12}}{1_{12} + 1_{13}} \quad (\text{Eq. 29})$$

$$V_{yL} = R_{y5} + W_4 \cos \alpha + W_5 \cos \alpha \frac{1_{13}}{1_{12} + 1_{13}}$$

LATERAL SHEAR FORCES (Equation 30)

$$V_{xr} = R_{x2} - R_{x3} + g d_2 1_{12}; V_{xL} = R_{x5} \quad (\text{Eq. 30})$$

NOTE— Subscripts r and L refer to the right and left of Section Z<sub>2</sub> - Z<sub>2</sub>

**6.6 Refer Figure 6—Load Moment Equations for Intermediate Section at Section Z<sub>3</sub> - Z<sub>3</sub>** (see Equation 31, Equation 32, Equation 33, Equation 34, Equation 35, Equation 36, Equation 37)

MOMENTS (Equation 31)

$$M_x = R_{y4} 1_{20} - R_{y5} 1_{25} + W_9 \cos \alpha 1_{24} + 0.5W_8 \cos \alpha \frac{1_{20}^2}{1_{20} + 1_{21}} \mp W_8 \sin \alpha 1_{27} \mp R_{z5} (1_{27} - 1_{26}) \quad (\text{Eq. 31})$$

$$M_y = R_{x4} 1_{20} - R_{x5} 1_{25} + 0.5g d_3 1_{20}^2$$

$$T = P_x 1_2$$

AXIAL LOAD ON CYLINDER SUPPORTS (Equation 32)

$$R_{z5} = R_{z4} + (W_6 + W_7) \sin \alpha; R_{z6} = R_{z5} + W_8 \sin \alpha \quad (\text{Eq. 32})$$

AXIAL LOAD ON SECTION (Equation 33)

$$P_{ar} = P_{aL} = P_{z5} + W_8 \sin \alpha \frac{1_{21}}{1_{20} + 1_{21}} \quad (\text{Eq. 33})$$

VERTICAL REACTIONS (Equation 34)

$$R_{y7} = \frac{M_x}{1_{21} - W_7} \cos \alpha \frac{1_{22}}{1_{21}} - 0.5W_8 \cos \alpha \frac{1_{21}}{1_{20} + 1_{21}} \quad (\text{Eq. 34})$$

$$R_{y6} = R_{y4} - R_{y5} + R_{y7} + \cos \alpha (W_7 + W_8 + W_9)$$

LATERAL REACTIONS (Equation 35)

$$R_{x7} = \frac{M_y}{1_{21}}; R_{x6} = R_{x4} - R_{x5} + R_{x7} + g d_3 1_{20} \quad (\text{Eq. 35})$$

VERTICAL SHEAR FORCES (Equation 36)

$$V_{yr} = R_{y4} - R_{y5} + W_9 \cos \alpha + W_8 \cos \alpha \frac{1_{20}}{1_{20} + 1_{21}} \quad (\text{Eq. 36})$$

$$V_{yL} = R_{y7} + W_7 \cos \alpha + W_8 \cos \alpha \frac{1_{21}}{1_{20} + 1_{21}}$$

LATERAL SHEAR FORCES (Equation 37)

$$V_{xr} = R_{x4} - R_{x5} + g d_3 1_{20}; V_{xL} = R_{x7} \quad (\text{Eq. 37})$$

NOTE— Subscripts r and L refer to right and left of Section Z<sub>3</sub> - Z<sub>3</sub>

**6.7 Refer Figure 7—Load Moment Equations—Base Section at Section Z<sub>4</sub> - Z<sub>4</sub>** (see Equation 38, Equation 39, Equation 40, Equation 41, Equation 42, Equation 43, Equation 44, Equation 45, Equation 46)

MOMENTS (Equation 38)

$$M_x = R_{y6} 1_{28} - R_{y7} 1_{33} + 0.5w_{12} \cos \alpha \frac{1_{28}^2}{1_{28} + 1_{29}} \quad (\text{Eq. 38})$$

$$M_y = R_{x6} 1_{28} - R_{x7} 1_{33} + 0.5g d_4 1_{28}^2$$

$$T = P_x 1_2$$

AXIAL LOAD ON CYLINDER SUPPORT (Equation 39)

$$R_{z7} = R_{z6} + (W_9 + W_{10}) \sin \alpha \quad (\text{Eq. 39})$$

AXIAL LOAD ON SECTION (Equation 40)

$$P_{ar} = P_{aL} = W_{12} \sin \alpha \frac{1_{28}}{1_{28} + 1_{29}} \quad (\text{Eq. 40})$$

VERTICAL SHEAR FORCE (Equation 41)

$$V_{yr} = R_{y6} - R_{y7} + W_{12} \cos \alpha \frac{1_{28}}{1_{28} + 1_{29}} \quad (\text{Eq. 41})$$

$$V_{yL} = R_{y8r} + R_{y8L} + (W_{10} + W_{11}) \cos \alpha + W_{12} \cos \alpha \frac{1_{28}}{1_{28} + 1_{29}}$$

LATERAL SHEAR FORCE (Equation 42)

$$V_{xr} = R_{x6} - R_{x7} + gd_4 1_{28}; V_{xL} = R_{x8} - gd_4 1_{29} \quad (\text{Eq. 42})$$

HOIST CYLINDER REACTIONS (Equation 43)

$$\begin{aligned} R_h = & [R_{y6}(1_{28} + 1_{29}) - R_{y7}(1_{29} + 1_{33}) + W_{10} 1_{32} \cos \alpha \\ & + W_{11}(1_{31} \cos \alpha - 1_{36} \sin \alpha) + W_{12}(1_{30} \cos \alpha - 1_{36} \sin \alpha) \\ & - R_{z7}(1_{36} - 1_{35})] / \left[ 1_{29} - \left( \frac{1_{36} - 1_{34}}{\cotan \theta} \right) \right] \cos \theta \end{aligned} \quad (\text{Eq. 43})$$

PIVOT PIN LOADING

LATERAL REACTION (Equation 44)

$$R_{x8} = R_{x6} - R_{x7} + gd_4(1_{28} + 1_{29}) \quad (\text{Eq. 44})$$

AXIAL REACTIONS (Equation 45)

$$\begin{aligned} R_{z8r} = & \frac{R_h \sin \theta}{2} + R_{x6} \frac{1_{28} + 1_{29}}{1_{37}} - R_{x7} \left( \frac{1_{29} + 1_{33}}{1_{37}} \right) \\ & - \frac{R_{z7} - (W_{11} + W_{12}) \sin \alpha}{2} + \frac{0.5gd_4(1_{28} + 1_{29})^2}{1_{37}} \\ R_{z8L} = & \frac{R_h \sin \theta}{2} - R_{x6} \frac{1_{28} + 1_{29}}{1_{37}} + R_{x7} \left( \frac{1_{29} + 1_{33}}{1_{37}} \right) \\ & - \frac{R_{z7} - (W_{11} + W_{12}) \sin \alpha}{2} - \frac{0.5gd_4(1_{28} + 1_{29})^2}{1_{37}} \end{aligned} \quad (\text{Eq. 45})$$

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VERTICAL REACTIONS (Equation 46)

$$\begin{aligned}
 R_{y8r} &= 0.5[R_h \cos \theta + R_{y7} - R_{y6} - (W_{10} + W_{11} + W_{12}) \cos \alpha] \\
 &\quad - P_x \frac{1_2 - 1_{36}}{1_{37}} + g d_4 (1_{28} + 1_{29}) \frac{1_{36}}{1_{37}} \\
 R_{y8L} &= 0.5[R_h \cos \theta + R_{y7} - R_{y6} - (W_{10} + W_{11} + W_{12}) \cos \alpha] \\
 &\quad + P_x \frac{1_2 - 1_{36}}{1_{37}} - g d_4 (1_{28} + 1_{29}) \frac{1_{36}}{1_{37}}
 \end{aligned}
 \tag{Eq. 46}$$

NOTE—Subscripts r and L refer to right and left of Section Z<sub>4</sub> - Z<sub>4</sub>**7. Calculation Procedure****7.1 Step 1—Preliminary Data**

- a. Provide description of geometry and loading, such as boom length, working radius, boom angle, rated load, etc.
- b. Identify boom arrangement.
  1. Generate shear and moment diagrams.
  2. Solve for forces and moments from Section 3.
- c. Identify boom section for analysis.
  1. Determine material properties.
  2. Determine section properties.

**7.2 Step 2—Calculation of Section Properties, Based on Compressive Stresses, the Actual Stress, and the Allowable Stress****7.2.1 TO DETERMINE SECTION PROPERTIES**

- a. Determine if plates in compression are fully effective at yield.
  1. For vertical bending loads compute the b/t ratio for the compressive flange.
  2. For side bending loads compute the b/t ratio for the compressive web.
  3. For axial loads compute the b/t ratio for both webs and both flanges. If  $b/t \leq 184/\sqrt{f}$ , where  $f = 0.6F_y$ , then the entire section will be fully effective at yield. The properties can then be computed based on the actual section. Proceed to 7.2.2 for the allowable stress computations. If  $b/t > 184/\sqrt{f}$ , for any or all plates, the section may still be fully effective for the actual stress. AISC (1.9.2.2)
- b. Determine if plates in compression are fully effective at the actual stress.
  1. Compute actual stresses based on full section properties.
    - 1.1 For compression flange,  $f = f_a + f_{bx}$
    - 1.2 For compression web,  $f = f_a + f_{bx}$
    - 1.3 For axial (all plates),  $f = f_a$

Use this calculated stress for f and recompute the b/t ratios.

NOTE—For the axial case the effective widths will be different. Refer to Appendix E.

If  $b/t \leq 184/\sqrt{f}$ , for all plates, the entire section is fully effective at a stress level 1.67 times the actual stress. Proceed to 7.2.2 for the allowable stress computations. If  $b/t > 184/\sqrt{f}$ , for any one or all plates, the section is not fully effective for stress level  $f$  and an effective width calculation must be made for each plate that exceeds this ratio.

- c. Determine effective width of plates that have  $b/t$  ratio greater than  $184/\sqrt{f}$ .
  1. Calculate the effective width of plates which are not fully effective accordingly:

$$b_c = \frac{253t}{\sqrt{f}} \left( 1 - \frac{50.3}{(b/t)\sqrt{f}} \right) \quad \text{AISC (C3-1)}$$

where:

$f$  is the actual stress computed from 7.2.1.B.1.1, 7.2.1.B.1.2, and 7.2.1.B.1.3 from the previous paragraph

2. Calculate new section properties  $A_e$ ,  $S_{xe}$ , and  $S_{ye}$  based on the effective widths  $b_e$ .

NOTE— The effective widths  $b_e$  used in computing  $A_e$  do not require an iterative solution because the stress  $f_a$  is based on the actual area  $A$ .

3. Recompute new stress levels based on new properties.
4. Recompute new effective widths based on new stress levels.
5. Continue until stress level stabilizes—approximately three iterations. Proceed to 7.2.2 for the allowable stress computations.

## 7.2.2 TO DETERMINE ALLOWABLE STRESSES

- a. Allowable axial stress  $F_a$

NOTE— If the stress is a tensile value, then  $F_a = 0.6F_y$ , proceed to 7.2.2B.

1. Factor  $Q_a$

$$Q_a = \frac{\text{effective area } (A_e)}{\text{actual area } (A)} \quad \text{AISC (C4)}$$

where:

$A_e$  equals the effective area of all stiffened elements, both flanges and webs, corresponding to the actual stress

If all plates are fully effective  $Q_a = 1$ .

2. Factor  $Q_s$ ; see Appendix F to determine if this computation must be made. Applies to outstanding plates free on one edge.

$$3. \quad C_c = \sqrt{\frac{\pi^2 E}{Q_s Q_a (F_y - \sigma_{rc})}} \quad \text{AISC (C5)}$$

where:

$$Q_s Q_a \leq 1.0$$

4. Compute  $(KL/r)$  of both axis and use the largest  $KL/r$  value for the  $F_a$  calculation

$$r = \sqrt{\frac{I}{A}}$$

5. If  $(KL/r) < C'_c$ —inelastic range

$$F_a = \frac{Q_s Q_a \left[ 1 - \frac{\sigma_{rc} (KL/r)^2}{F_y (C'_c)^2} \right] F_y}{5/3 + 3/8 \left( \frac{KL/r}{C'_c} \right) - 1/8 \left( \frac{KL/r}{C'_c} \right)^3} \quad \text{AISC (C5-1)}$$

6. If  $(KL/r) \geq C'_c$ —elastic range

$$F_a = \frac{12\pi^2 E}{23(KL/r)^2} \quad \text{AISC (1.5-2)}$$

NOTE—L as used previously is the distance from the outer end of the section in question to the point where the stresses are to be calculated in that section.

- b. Allowable compressive bending stresses  $F_b$  for x and y directions considering lateral torsional buckling.

1. Inelastic lateral buckling check

$$(KL/r) \text{ equiv.} = \frac{\sqrt{5.1K_t L S_x}}{\sqrt{J I_y}} \sqrt{C_b} \quad \text{CRC(4.7)}$$

where:

$$K_t = 4/3$$

L = distance from tip to section in question

$$C_b = 1.75 + 1.05 \left( \frac{M_{x\min}}{M_{x\max}} \right) + 0.3 \left( \frac{M_{x\min}}{M_{x\max}} \right)^2 ; 1.0 \leq C_b \leq 1.3$$

CRC p. 101

$M_{x\min}$  = the moment at the tip

$M_{x\max}$  = the moment at the section in question at L

NOTE—Clockwise moments are positive. Counterclockwise moments are negative. Refer to Appendix C for further discussion.

2. Compute first check on allowable compressive stresses.

$$2.1 \text{ If } (KL/r) \text{ equiv.} \leq \sqrt{\frac{102\,000}{F_y}}$$

$$F_{bx} = 0.6F_y$$

$$F_{by} = 0.6F_y$$

$$2.2 \text{ If } \sqrt{\frac{102\,000}{F_y}} < \left(\frac{KL}{r}\right) \text{ equiv.} \leq \sqrt{\frac{51\,000}{F_y}}$$

$$F_{bx} = F_y \left( \frac{2}{3} - \frac{5.1 K_t L S_x F_y}{1\,530\,000 C_b \sqrt{I_y}} \right) \leq 0.6F_y \quad \text{AISC(1.5-6a)}$$

$$F_{by} = 0.6F_y$$

$$2.3 \text{ If } \left(\frac{KL}{r}\right)_{\text{equiv}} > \sqrt{\frac{510\,000}{F_y}}$$

$$F_{bx} = 170\,000 / (KL/r)^2 \text{ equiv.}$$

$$F_{by} = 0.6F_y$$

AISC (1.5-6b)

If there are unstiffened elements on the section that result in a value for  $Q_s$  less than 1, then  $F_b$  shall be the smaller value  $0.6F_y Q_s$  or that provided by 7.2.2.B.2.1, 7.2.2.B.2.2, and 7.2.2.B.2.3 multiplied by  $Q_s$ , whichever is applicable.

c. Determine if a further reduction in  $F_{bx}$  is required

1. If web  $(h/t) > 760/\sqrt{F_{bx}}$ , then:

$$F_{bx} = F_{bx} \left[ 1.0 - 0.0005 \frac{A_w}{A_f} \left( \frac{h}{t} - \frac{760}{\sqrt{F_{bx}}} \right) \right] \quad \text{AISC (1.10-5)}$$

If web  $(h/t) > 760 \sqrt{5.4} / \sqrt{F_{bx}}$  and horizontal stiffeners are used and placed at 0.4 the distance between the compression flange and the neutral axis as measured from the compression flange (refer to Appendix G) then:

$$F_{bx} = F_{bx} \left[ 1.0 - 0.0005 \frac{A_w}{A_f} \left( \frac{h}{t} - \frac{760 \sqrt{5.4}}{\sqrt{F_{bx}}} \right) \right]$$

2. And if the section is a hybrid,  $F_{bx}$  in either flange shall not exceed the previous or

$$F_{bx} = F_{bx} \left( \frac{12 + (A_w/A_f)(3a - a^3)}{12 + 2A_w/A_f} \right) \quad \text{AISC (1.10-6)}$$

where:

$a = F_y$  of web/ $F_y$  of flange

**7.3 Step 3—Solution to the Interaction Equation(s) for the Compressive Stresses**

NOTE— The actual stresses  $f_{bx}$  and  $f_{by}$  are based on the effective section properties, if applicable,  $S_{xe}$  and  $S_{ye}$ . The axial stress  $f_a$  is based on the total area ( $A$ ) of the section. Also, the  $f_a$  term may be positive for some sections. Refer to 7.2.2A.

1. If  $f_a/F_a \leq 0.15$ , then compute

$$\frac{f_a}{F_a} + \frac{f_{bx}}{F_{bx}} + \frac{f_{by}}{F_{by}} \leq 1.0 \quad \text{AISC (1.6-2)}$$

2. If  $f_a/f_a > 0.15$ , then compute both 2.1 and 2.2

$$2.1 \quad \frac{f_a}{0.6F_y} + \frac{f_{bx}}{F_{bx}} + \frac{f_{by}}{F_{by}} \leq 1.0 \quad \text{AISC (1.6-1b)}$$

$$2.2 \quad \frac{f_a}{F_a} + \frac{C_{mx}f_{bx}}{\left(1 - \frac{f_a}{F_{ex}}\right)F_{bx}} + \frac{C_{my}f_{by}}{\left(1 - \frac{f_a}{F_{ey}}\right)F_{by}} \leq 1.0 \quad \text{AISC (1.6-1a)}$$

where:

$$C_{mx} = C_{my} = 0.85$$

$$F_e = \frac{12\pi^2 E}{23 \left(\frac{KL_b}{r_b}\right)^2}$$

Do for both x and y axes using their corresponding  $r_b$ .

**7.4 Step 4—Calculation of the Actual and Allowable Shear Stress in the Webs****7.4.1 I. TO DETERMINE THE ACTUAL STRESSES—**

$$f_a = V_y/2bt + T/2A_{m_i}$$

where:

$bt$  = the area of one web

$A_m$  = the area based on the mean dimensions of the section. Refer to Appendix E.

**7.4.2 II. TO DETERMINE THE ALLOWABLE SHEAR STRESS  $F_v$** 

- a. No stiffeners on the web plates if

1.  $h/t < 260$  and/or

$$h/t \leq \frac{14\,000}{\sqrt{F_y(F_y + 16.5)}} \quad \text{AISC (1.10.2)}$$

where:

$F_y$  = material yield of the compression flange

2.  $k = 5.34$

3.  $C_v = \frac{45\,000k}{F_y(h/t)^2}$

If  $C_v > 0.8$ , then  $C_v = \frac{190}{(h/t)} \sqrt{\frac{k}{F_y}}$  AISC (1.10-1)

4.  $F_v = \frac{F_y C_v}{2.89} \leq 0.4F_y$  AISC (1.10-1)

5.  $f_s \leq F_v$

b. If part A is not met, then proceed accordingly—stiffeners are required.

1. If  $a/h \leq 1.5$ , then  $h/t$  may be as much as  $\frac{2000}{\sqrt{F_y}}$ . If  $a/h < 1.0$ , then  $h/t$  may be as much as  $\frac{2500}{\sqrt{F_y}}$ . Where

$F_y$  is the same as before, otherwise  $h/t$  is limited to  $\frac{14\,000}{\sqrt{F_y(F_y + 16.5)}}$  in any case  $a/h \leq \left(\frac{260}{h/t}\right)^2$  to

a maximum of 3

2. If  $a/h < 1.0$ ;  $k = 4 + 5.34/(a/h)^2$  AISC (1.10.5.2)  
If  $a/h > 1.0$  (up to 3);  $k = 5.34 + 4/(a/h)^2$

3.  $C_v = \frac{45\,000k}{F_y(h/t)^2}$ ; however, if  $C_v > 0.8$ , then  
 $C_v = \frac{190}{h/t} \sqrt{\frac{k}{F_y}}$

4. If  $C_v \leq 1.0$ , then  
 $F_v = \frac{F_y}{2.89} \left[ C_v + \frac{1 - C_v}{1.15 \sqrt{1 + (a/h)^2}} \right] \leq 0.4F_y$  AISC (1.10-2)

5. If  $C_v > 1.0$ , then  
 $F_v = \frac{F_y C_v}{2.89} \leq 0.4F_y$

6.  $f_s \leq F_v$

## c. Stiffener properties

## 1. Required cross-sectional area

$$A_{st} = \frac{1 - C_v}{2} \left( \frac{a}{h} - \frac{(a/h)^2}{\sqrt{1 + (a/h)^2}} \right) y \cdot D \cdot h \cdot t \quad \text{AISC (1.10-3)}$$

where:

$Y = F_y$  of web/ $F_y$  of stiffener (see Appendix G)

$D = 1.0$  for stiffeners in pairs

$= 1.8$  for single angle stiffeners

$= 2.4$  for single plate stiffeners

NOTE—If  $F_v$  was computed from IIB-4 previously, then

$$A_{st} = A_{st} \frac{f_s}{F_v}$$

## 2. Required moment of inertia with reference to an axis in the plane of the web.

$$I_{st} \geq \left( \frac{h}{50} \right)^4 \quad \text{AISC (1.10.5.4)}$$

## 3. Required weld to connect stiffener to the web.

$$f_{vs} \geq h \sqrt{\left( \frac{F_y}{340} \right)^3} \quad \text{AISC (1.10-4)}$$

where:

$F_y =$  material yield of web

$f_{vs} =$  kips per lineal inch

NOTE—If  $F_v$  was computed from IIB-4 previously, then

$$f_{vs} = f_{vs} \frac{f_s}{F_v}$$

## 7.5 Step 5—Calculation for Tensile Stresses

### 7.5.1 I. ACTUAL STRESS WITHOUT STIFFENERS—

$$-f_a + f_{bx} + f_{by} \leq 0.6F_y$$

NOTE—If the section is a hybrid, then the limit is  $F'_{bx}$  from 7.2.2.C.1 and/or 2. On some sections  $f_a$  may be positive.

### 7.5.2 II. If stiffeners are used and if $F_v$ came from 7.4.2.B.4, then the bending tensile stress is limited accordingly.

$$f_{bx} + f_{by} \leq \left( 0.825 - 0.375 \frac{f_s}{F_v} \right) \leq 0.6F_y \quad \text{AISC (1.10-7)}$$

7.5.3 III. If the flanges and webs are of ASTM A 514 steel and stiffeners are used, and if

$f_{bx} + f_{by} > 0.75F_{bx}$  or  $F_{bx}$ , if applicable,

then  $f_s$  shall not exceed  $F_v$  as computed from 8.4.2.B.5.

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APPENDIX A—

Critical flexural stress due to lateral-torsional buckling for the compression flange

$$\left(\frac{KL}{r}\right)_{\text{equiv}}^2 = \frac{5.1K_tLS_x}{\sqrt{JI_y}}/C_b \quad (\text{Eq. A1})$$

(Section 1.5.1.4.4 Commentary on AISC)

Terms:

L = distance from tip to section in question

S<sub>x</sub> = major axis section modulus to the compressive flange

I<sub>y</sub> = minor axis moment of inertia

J = torsional constant of the beam cross section

K<sub>t</sub> = 4/3 cantilevered section with no end restraint

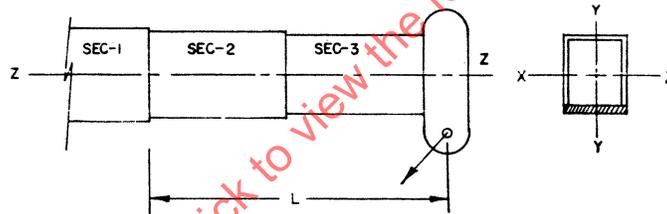


FIGURE A1—

AISC (1.5-6a)

$$F_{bx} = \left(\frac{2}{3} - \frac{F_y(L/r_t)^2}{1530 \times 10^3}\right) F_y \leq 0.6F_y$$

substitute  $(KL/r)_{\text{equiv}}$  for  $(L/r_t)$  to obtain expression for  $F_{bx}$ :

$$F_{bx} = F_y \left(\frac{2}{3} - \frac{5.1K_tLS_xF_y}{1\,530\,000\,C_b\sqrt{JI_y}}\right) \leq 0.6F_y$$

(Refer to Appendix C for value of C<sub>b</sub>.)

APPENDIX B—

Relationship between *relative effectiveness* and width-thickness ratio for a stiffened compression element based on 0.60  $F_y$  compressive stress level, uniformly distributed. (*Safety factor = 1.67 for  $k_c = 4.0$* )

$$b/t = 1.9 \sqrt{\frac{0.6E}{f_{\max}}} \left( 1 - (0.91) \frac{(0.415)}{w/t} \sqrt{\frac{0.6E}{f_{\max}}} \right) \quad (\text{Eq. B1})$$

where:

$$f_{\max} \leq 0.6F_y$$

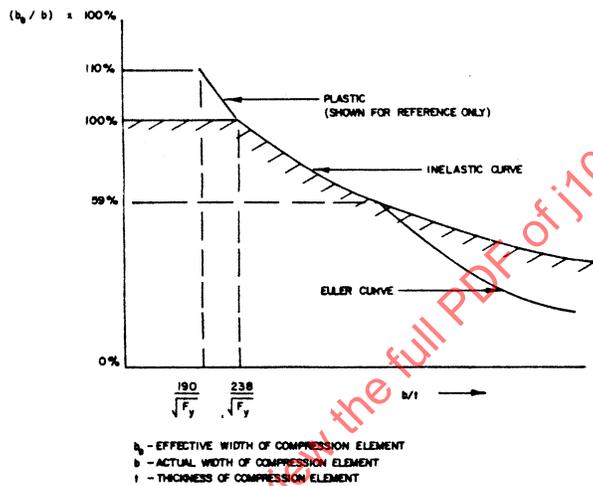


FIGURE B1—

APPENDIX C  
BENDING COEFFICIENT  $C_b$

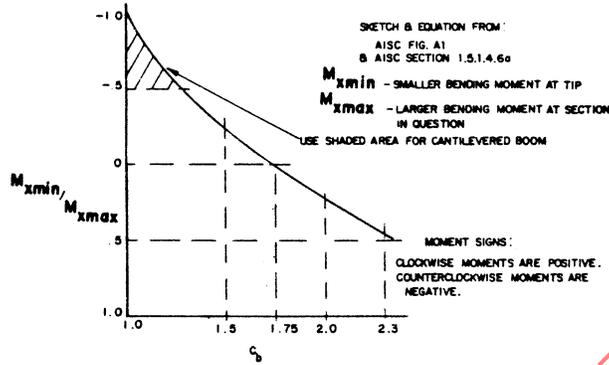


FIGURE C1—

Equation:

$$C_b = 1.75 + 1.05 \left( \frac{M_{xmin}}{M_{xmax}} \right) + 0.3 \left( \frac{M_{xmin}}{M_{xmax}} \right)^2 \quad (\text{Eq. C1})$$

where

$$1 \leq C_b \leq 1.3$$

CRC p. 101

OTHER REFERENCE—AISI Commentary—Flexural members chapter, subject—lateral buckling

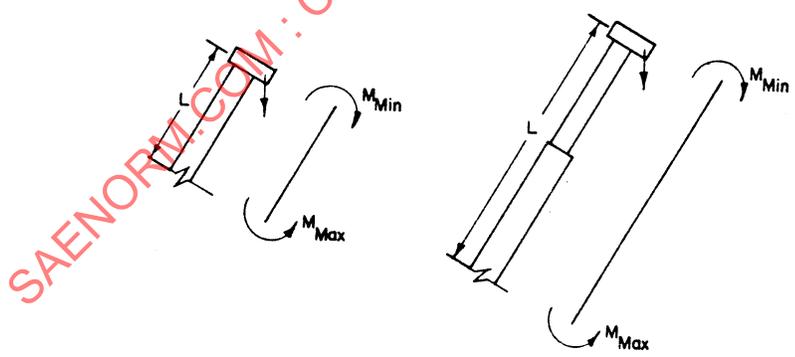


FIGURE C2—

APPENDIX D

TORSIONAL CONSTANT J FOR CLOSED RECTANGULAR SECTIONS—

General equation:

$$J = \frac{2(A_o + A_i)A_m}{\frac{2h_m}{t_w} + \frac{b_m}{t_1} + \frac{b_m}{t_2}} \quad (\text{Eq. D1})$$

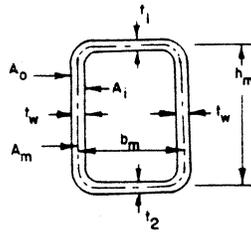


FIGURE D1—

CASE I—for thin wall sections

Top and bottom flanges are the same thickness

$$J = \frac{2t_1 t_w b_m^2 h_m^3}{b_m t_w + h_m t_1} \quad (\text{Eq. D2})$$

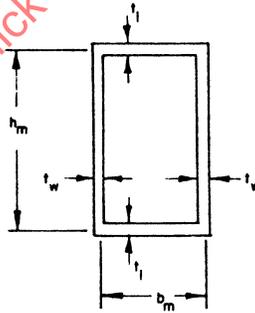


FIGURE D2—

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Case II—for thin wall sections

Top and bottom flanges are not the same thickness

$$J = \frac{4b_m^2 h_m^2}{\left(\frac{2h_m}{t_w} + \frac{b_m}{t_1} + \frac{b_m}{t_2}\right)} \quad (\text{Eq. D3})$$

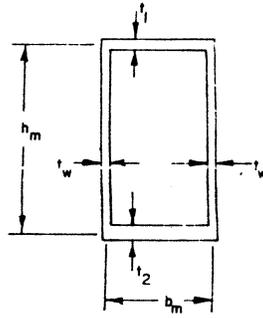


FIGURE D3—

$$\begin{aligned} A_m &= b_m \times h_m \\ A_i &= b_f \times h \\ A_o &= b_w \times d \end{aligned} \quad (\text{Eq. D4})$$

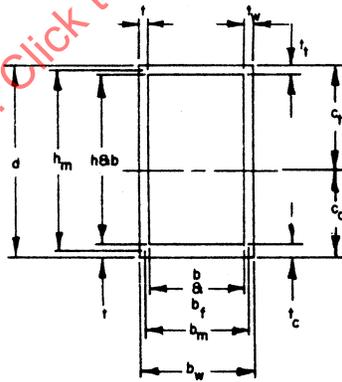
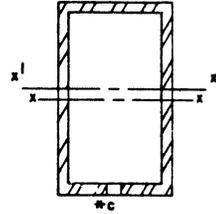


FIGURE D4—

APPENDIX E

EFFECTIVE WIDTH OF CROSS SECTION

$S_{x0}$  : BASED ON EFFECTIVE AREA



$S_{y0}$  : BASED ON EFFECTIVE AREA. (AN EQUAL AREA MAY BE CONSERVATIVELY REMOVED TO FROM THE TENSILE SIDE TO MAKE THE SECTION SYMMETRICAL AND THUS FACILITATE THE SECTION MODULUS CALCULATION )



NOTE: \*c INDICATES COMPRESSION SIDE

FIGURE E1—

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APPENDIX F  
UNSTIFFENED ELEMENTS

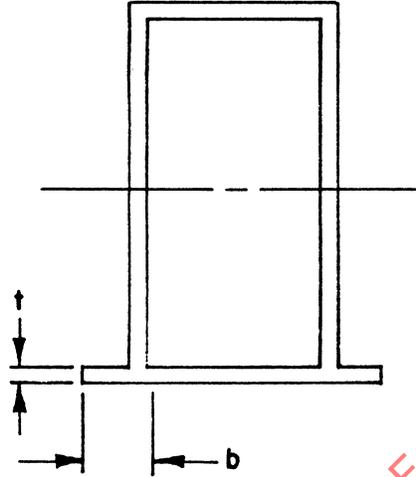


FIGURE F1—

if:

$$(b/t) \leq 95.0/\sqrt{F_y} \quad Q_s = 1 \quad (\text{Eq. F1})$$

when:

$$95.0/\sqrt{F_y} < (b/t) < 176/\sqrt{F_y} \quad (\text{Eq. F2})$$

$$Q_s = 1.415 - 0.00437(b/t)\sqrt{F_y}$$

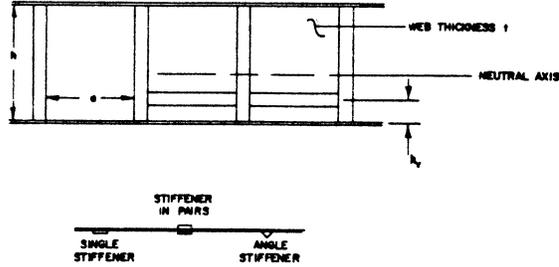
when:

$$(b/t) \geq 176/\sqrt{F_y} \quad (\text{Eq. F3})$$

$$Q_s = 20\,000/[F_y(b/t)^2]$$

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APPENDIX G  
 PANEL STIFFENERS



$h_v = 0.4$  the distance between the compression flange and the neutral axis as measured from the compression flange

if  $a/h < 1.0$ :  $k = 4.0 + 5.34/(a/h)^2$

if  $1.0 < a/h \leq 3.0$ :  $k = 5.34 + 4.0/(a/h)^2$

if  $a/h > 3.0$ :  $k = 5.34$  (use of tension field action is not counted upon)

FIGURE G1—

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## APPENDIX H

## WIND LOAD

**H.1** Relationship between Wind Velocity and height.

$$V = V_r(H/H_r)^p \quad (\text{Eq. H1})$$

$V_r$  = wind velocity (mph) at height  $H_r$

$H_r$  = reference height at which wind velocity is measured (usually  $H_r = 20$  ft)

$H$  = height to center of wind pressure on boom or boom section from ground  $H = H_o + H_p$

$V$  = wind velocity (mph) at wind pressure height  $H$

$p$  = wind velocity exponent

where:

for  $V_r = 20$  mph at  $H_r = 20$  ft, use  $p = 0.17$

for  $V_r = 50$  mph at  $H_r = 20$  ft, use  $p = 0.25$

NOTE— 20 mph is for in-service condition

50 mph is four out-of-service condition

**H.2** Wind load  $g$ , pounds per square inch

$$g = 0.004(V)^2/144 \quad (\text{Eq. H2})$$

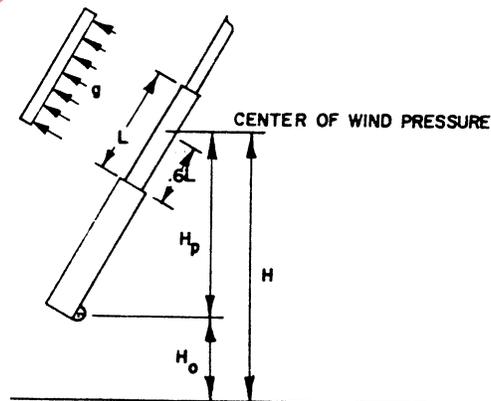
**H.3** Center of wind pressure is found for a given section at 60% of its extended length, the wind velocity for that section is found at that point.

FIGURE H1—