
**Pneumatic fluid power — Assessment
of component reliability by
accelerated life testing — General
guidelines and procedures**

*Transmissions pneumatiques — Évaluation de la fiabilité du
composant par essai de durée de vie accélérée — Lignes directrices
générales et modes opératoires*

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

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ISO/TR 16194 was prepared by Technical Committee ISO/TC 131, *Fluid power systems*.

Introduction

This document is being released to document progress that the working group has developed for accelerated testing. It is a new method with which the working group members have very little experience, but has been used by institutional laboratories and taught at academic levels.

Some experimentation on air cylinders has been done at the Korean Institute of Machinery and Materials (KIMM), but the application to pneumatic components in general has not been evaluated.

This document is offered to members as a reference and model procedure, so that they can develop experience with its use in their own laboratories.

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Pneumatic fluid power — Assessment of component reliability by accelerated life testing — General guidelines and procedures

1 Scope

This document provides general procedures for assessing the reliability of pneumatic fluid power components using accelerated life testing and the method for reporting the results. These procedures apply to directional control valves, cylinders with piston rods, pressure regulators, and accessory devices – the same components covered by the ISO 19973 series of standards.

This document does not provide specific procedures for accelerated life testing of components. Instead, it explains the variability among methods and provides guidelines for developing an accelerated test method.

The methods specified in this document apply to the first failure, without repairs.

2 Normative references

There are no normative references in this document.

3 Terms and definitions

For the purposes of this document, the terms and definitions given in ISO 5598, ISO 19973-1 and the following apply. ISO and IEC maintain terminological databases for use in standardization at the following addresses:

— IEC Electropedia: available at <http://www.electropedia.org/>

— ISO Online browsing platform: available at <http://www.iso.org/obp>

3.1

B_x life

life of a component or assembly that has not been altered since its production, where its reliability is (100 – x) %; or the time at which (100 – x) % of the population has survived

Note 1 to entry: The cumulative failure fraction is x %. For example, if x = 10, the B₁₀ life has a cumulative failure probability of 10 %.

3.2

acceleration factor

AF

ratio between the life at the normal use stress level and the life at the accelerated stress level

3.3

accelerated life test

ALT

process in which a component is forced to fail more quickly than it would have under normal use conditions and which provides information about the component's life characteristics

3.4

destruct limit

stress level at which one or more of the component's operating characteristics is no longer within specification or the component is damaged and cannot recover when the stress is reduced

Note 1 to entry: Destruct limits are classified as a lower destruct limit and upper destruct limit.

3.5

failure mechanism

physical or chemical process that produces instantaneous or cumulative damage to the materials from which the component is made

3.6

failure mode

manifestation of the failure mechanism resulting from component failure or degradation

Note 1 to entry: The failure mode is the symptom of the aggressive activity of the failure mechanism in the component's areas of weakness, where stress exceeds strength.

3.7

failure rate

λ

frequency at which a failure occurs instantaneously at time t , given that no failure has occurred before t

3.8

highly accelerated life test

HALT

process in which components are subjected to accelerated environments to find weaknesses in the design and/or manufacturing process

Note 1 to entry: The primary accelerated environments include pressure and heat.

3.9

model for accelerated life testing

model that consists of a life distribution that represents the scatter in component life and a relationship between life and stress

Note 1 to entry: Life distribution examples: Weibull, Lognormal, Exponential, etc.

Note 2 to entry: Life and stress examples: Arrhenius, Eyring, Inverse Power Law, etc.

3.10

normal use conditions

test conditions at which a component is commonly used in the field, which can be less strenuous than rated conditions

3.11

termination cycle count

number of cycles on a test item when it reaches a threshold level for the first time

4 Symbols and units

Symbol ^a	Definition
B_{10}	Time at which 10 % of the population is estimated to fail
η	Scale parameter (characteristic life) of the Weibull distribution
$F(t)$	Probability of failure of a component up to time t
β	Shape parameter (slope) of the Weibull distribution
$R(t)$	Reliability of a component at time t ; $R(t) = 1 - F(t)$
$\lambda(t)$	Failures per unit time
^a Other symbols could be used in other documents and software.	

Units of measurements are in accordance with ISO 80000-1.

5 Concepts of reliability and accelerated life testing

Reliability is the probability (a percentage) that a component does not fail (for example, exceed the threshold level or experience catastrophic failure) for a specified interval of time or number of cycles when it operates under stated conditions. This reliability can be assessed by test methods described in the ISO 19973 series.

Generally, reliability analysis involves analysing time to failure of a component, obtained under normal use conditions in order to quantify its life characteristics. Obtaining such life data is often difficult.

The reasons for this difficulty can include the typically long life times of components, the small time period between design and product release, and the necessity for testing components under normal use conditions. Given this difficulty and the need to observe failures of components to better understand their life characteristics, procedures have been devised to accelerate their failures by overstress, thus forcing components to fail more quickly than they would under normal use conditions. The term accelerated life testing (ALT) is used to describe such procedures.

However, a relationship between the reliability of a component determined by ALT, and its reliability at normal use conditions, is necessary. This can be assessed by extrapolating the test results obtained from an accelerated life test and comparing it to that obtained from testing at normal use conditions. [Figure 1](#) shows the graphical concept for this relationship.

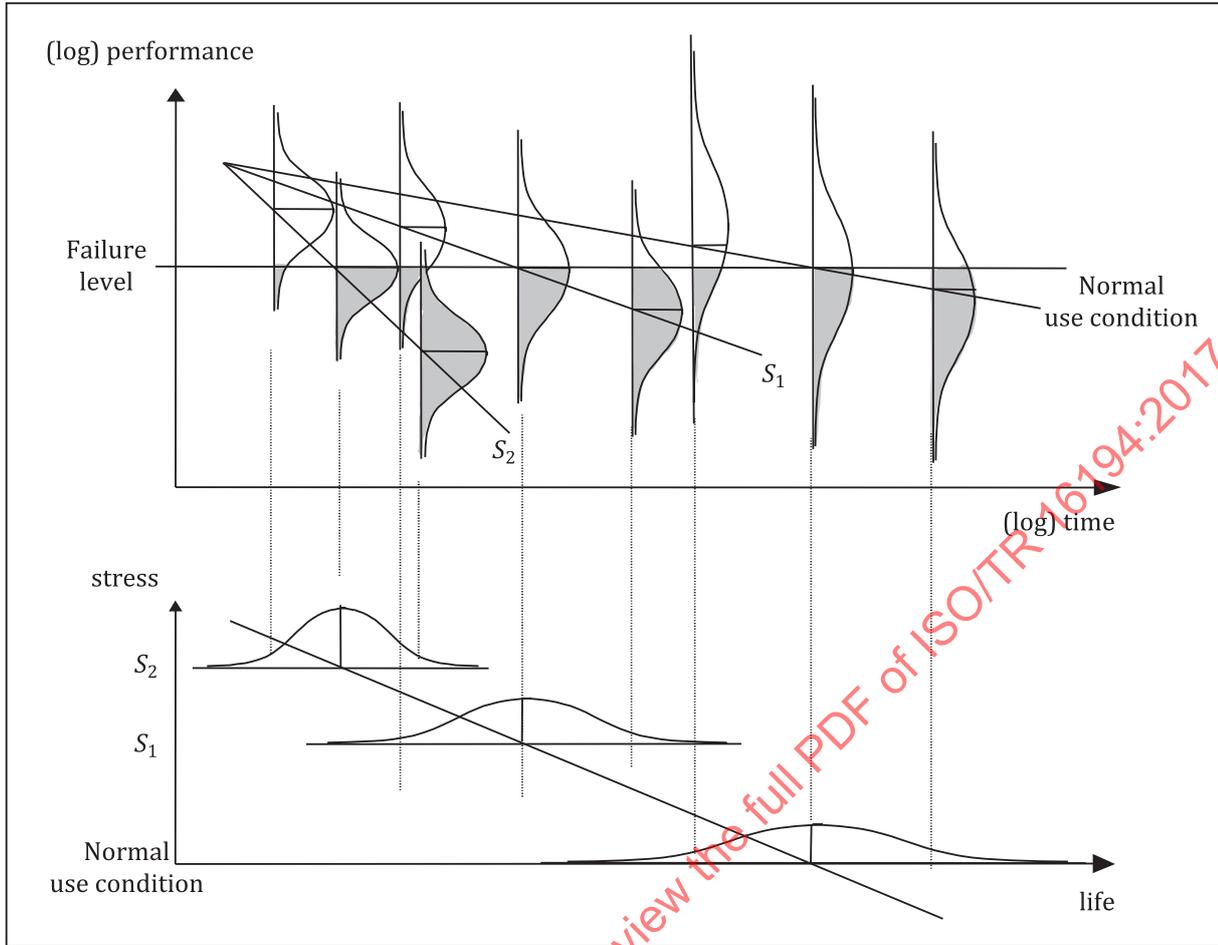


Figure 1 — Graphical explanation of relationship between S-N curve and accelerated life testing

NOTE Distributions in this concept [Figure 1](#) are not defined.

In [Figure 1](#), failures under normal use conditions are represented by the distribution S_3 , and the accelerated conditions are distributions S_1 and S_2 . Their relationship is shown by the connecting line(s).

6 Failure mechanism and mode

The failure mechanism is the physical or chemical process that produces instantaneous or cumulative damage to the materials from which the component is made. The failure mode is the manifestation of the failure mechanism resulting from component failure or degradation. The failure mode is the symptom of the aggressive activity of the failure mechanism in areas of component weakness where the stress exceeds the strength.

It is necessary that the failure modes observed in accelerated life test conditions are identical to those defined for normal use conditions.

7 Strategy of conducting accelerated life testing

Before starting an accelerated life test, it is important to identify the types of failures that might occur in service; especially any feedback from the field. Several methods are available to assist in this effort: design analysis and review using the quality function deployment (QFD), fault tree analysis (FTA), and failure modes and effect analysis (FMEA). Another method is a qualitative test like highly accelerated life testing (HALT). Qualitative tests are used primarily to reveal probable failure modes, but they do not quantify the life (or reliability) of the component under normal use conditions.

Accelerated life testing involves acceleration of failures with the single purpose of quantification of the life characteristics of the component at normal use conditions.

Therefore, accelerated life testing can be divided into two areas: qualitative accelerated testing (HALT) and quantitative accelerated life testing. In qualitative accelerated testing, the objective is to identify failures and failure modes without attempting to make any predictions as to the component's life under normal use conditions. In quantitative accelerated life testing, the objective is predicting the life of the component (life characteristics such as MTTF, B₁₀ life, etc.) at normal use conditions from data obtained in an accelerated life test.

The strategy for effectively conducting an accelerated life testing program includes the following:

- establishing a stress level that can be referred to as normal use conditions;
- determining the stress levels to use for accelerated testing; and
- determining the number of components to be tested at each stress level.

8 Design of accelerated life testing

8.1 Normal use conditions

Normal use conditions can often be defined from the ratings of the component's characteristics, for example: pressure, temperature, voltage, duty cycle, lubrication requirements, etc. However, these ratings often represent a maximum condition that is above commonly used conditions. Therefore, a definition for normal use conditions needs to be established from these characteristics before starting an accelerated test. An example definition for a pneumatic valve is shown in [Table 1](#).

Table 1 — Definition of normal use conditions for a pneumatic valve

Characteristic	Typical rating value	Common use application value	Proposed normal use value for testing
Pressure	1 000 kPa (10 bar)	630 kPa (6,3 bar)	630 kPa (6,3 bar)
Temperature	50 °C	25 °C	25 °C
Voltage	24 VDC	24 VDC	24 VDC
Duty cycle	Continuous	On-off varies	10 % on / 90 % off
Lubrication	Sometimes required	Sometimes applied	Not used
Air dryness	Dew point < 0 °C	Dew point ≤ 10 °C	Dew point = 10 °C

It is necessary to define this normal use conditions before starting an ALT program.

8.2 Preliminary tests

It is also necessary to determine the highest stress to be tested that does not result in failure modes different from those that occur under normal use conditions. Typically, these stresses or limits are unknown, so qualitative tests (HALT) with small sample sizes can be performed in order to determine the appropriate stress levels for use in the accelerated life test. Design of Experiments (DOE) methodology is a useful technique at this step.

The following steps can be taken to determine three stress levels:

- a) Propose the highest possible stress that might yield failure in less than 1 day of testing (approximately).
- b) Reduce this stress level to 90% of that value and test at least two test units to failure at this stress level, using the test procedures of one of the parts of the ISO 19973 series (modified for the conditions of the stress level).

- c) Examine the failure mode to determine if it is the same type of failure as would be experienced under normal use conditions. If it is not, reduce the level of stress and repeat steps b) and c) until failures are the same as would be experienced under normal use conditions. Identify this as stress level S_1 .
- d) Reduce the stress level by another 10% to 20% from step b) and test at least two more test units to failure. Again, examine the failure mode to determine if it is the same type of failure as would be experienced under normal use conditions. If it is not, modify the stress conditions and repeat the test. Identify this as stress level S_2 . See Figure 2.
- e) Identify a third, yet lower stress level S_3 that results in failures within the project timing constraints. This third level of stress is identified by extrapolating from the previous pairs of failures as shown in Figure 2. As an alternative, S_3 can be estimated by using an average value of S_1 and S_2 , so that $S_3 = \frac{1}{2} (S_2 - S_1)$.
- f) Test at least two more test units to failure at this third level of stress S_3 . Again, examine the failure mode to determine if it is the same type of failure as would be experienced under normal use conditions. If it is not, modify the stress conditions and repeat the test.

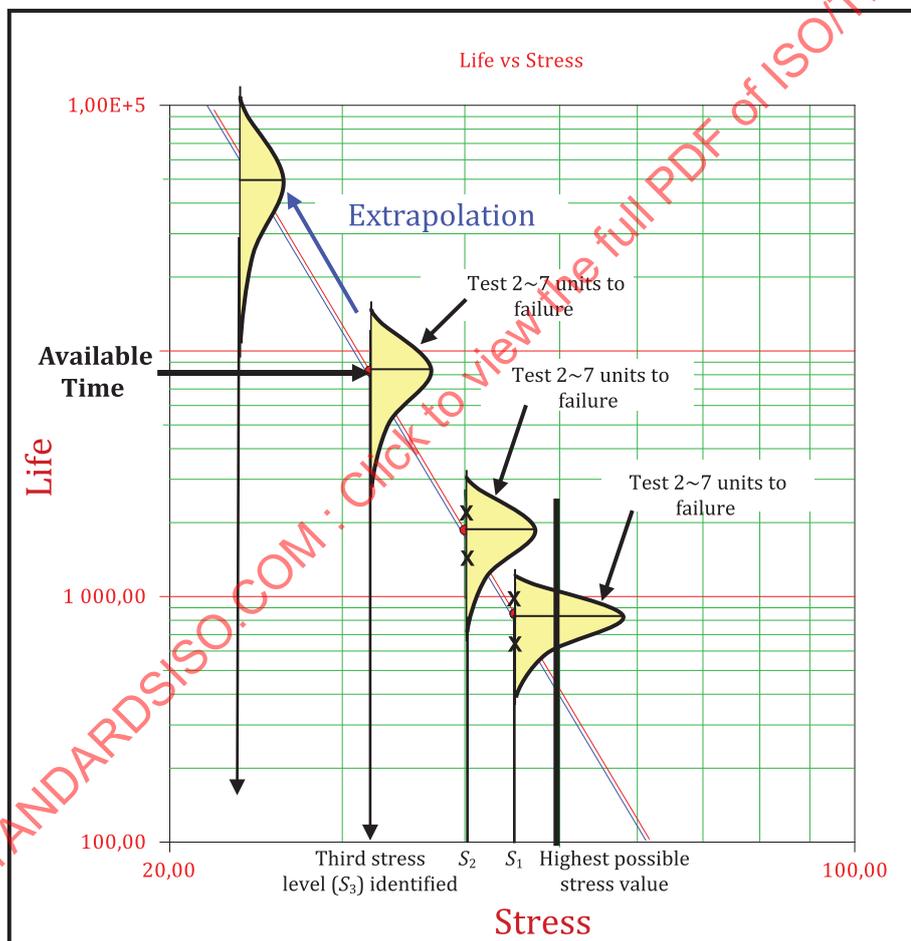


Figure 2 — Graphical explanation of determining stress levels during preliminary tests

These preliminary tests might have to be conducted several times before the necessary stress levels are determined.

8.3 Levels of accelerated stress

The levels of stress identified from 8.2 are used to conduct a series of accelerated tests on randomly selected test units, in accordance with one of the parts of ISO 19973. Generally, these stress levels

fall outside of the limits of the component's specification. It is important, therefore, to constantly examine the types of failures obtained to be sure they are the same as those experienced at normal use conditions. If they are not, the test units would be designated as suspensions, or the test conditions would be modified and the testing restarted.

Conduct the tests at each of the selected stress levels. It is also helpful to conduct at least one test at a stress level that is as close as possible to the normal use conditions.

At the higher levels of stress in an accelerated test, the required test duration decreases, and the uncertainty in the extrapolation increases. Confidence intervals provide a measure of the uncertainty in extrapolation.

The most common stresses for pneumatic fluid power components are pressure and temperature. Testing can be conducted either at one set of stress conditions on a sample lot, or two stresses on different sample lots. Cylinder speed, and cycle rate of valves and regulators are other possibilities.

Temperature of the process air used to test components is usually heated (or cooled) to approximately equal the environmental test temperature.

When conducting an accelerated life test, arrangements are made to ensure that the failures of the components are independent of each other (e.g. so that failures due to temperature do not influence the failures due to pressure).

8.4 Sample size

Ideally, at least seven test units are subjected to each stress level for the accelerated life test. However, the number of test units allocated to each stress level is usually inversely proportional to the level of applied stress; that is, more test units are subjected to lower stress levels than to higher stress levels because of the higher proportion of failures expected at the higher stress levels. A good ratio for the number of test units among the stress levels, from highest to lowest, is 1:2:4. If test units are expensive, four test units each at stress levels S_1 and S_2 would be tested; and five or more test units would be tested at stress level S_3 . As an option, the number of test units could be two if time is limited, but the estimation uncertainty at the normal use condition will increase.

8.5 Data observation and measurement

No repairs are made to the test units during accelerated life testing.

The test operator determines the intervals between measurements to obtain data during accelerated life testing. Short intervals between measurements give better statistical results and are conducted during testing at the high stress level. At the low stress levels, longer intervals between measurements are adequate.

8.6 Types of stress loading

There are two possible stress loading schemes: loading in which the stress is time-independent (where the stress does not vary over time), and loading in which the stress is time-dependent (where the stress does vary over time). This document uses constant time-independent stress loading, which is the most common type used in an accelerated life test; see [Figure 3](#). However, non-constant stress loads, such as step stress, cycling stress, random stress, etc., can be used. These types of loads are classified according to their dependence on time and are described in [Annex A](#). The method specified in [Annex A](#) is used where a time-dependent analysis is required.

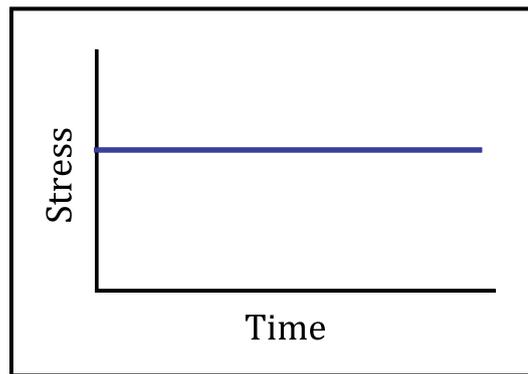


Figure 3 — Constant stress model

Time-independent stress loading has many advantages over time-dependent stress loading. Specifically:

- most components are assumed to operate at a constant stress under normal use conditions;
- it is far easier to run a constant stress test;
- it is far easier to quantify a constant stress test;
- models for data analysis are widely publicized and are empirically verified; and
- extrapolation from a well-executed constant stress test is more accurate than extrapolation from a time-dependent stress test.

9 End of test

9.1 Minimum number of failures required

Confidence levels are generated when at least four test units have failed (which includes their reaching a threshold level) at each stress level.

9.2 Termination cycle count

When a test unit fails between consecutive observations, the data collected is referred to as left-censored or interval data. In this case, both the last cycle count at which the test unit was operating properly and the cycle count at which the test unit was observed to have failed, are recorded. This data is usually processed in accordance with ISO 19973-1:2015, 10.2.

9.3 Suspended or censored test units

Individual test units on which testing was stopped before failure occurred are known as suspensions. Some examples of suspensions include:

- the test unit needed to be disassembled for inspection;
- the test unit experienced a failure mode different than the type being considered; and
- the test unit was accidentally damaged from a source not related to the test.

Because these test units had achieved a number of cycles before the point of suspension, the data has a positive influence on the calculation of the statistical parameters. However, they cannot be returned to the testing program.

If the minimum number of failures has been reached, but some test units have not failed (reached a threshold level), the test can be stopped. The remaining test units are designated as censored.

Data from suspended test units is considered the same as data from censored test units. The method specified in [Annex D](#) allows calculation of the statistical parameters for these types of data

10 Statistical analysis

10.1 Analysis of failure data

The failure data from testing at all stress levels is analysed in accordance with [10.2](#), [10.3](#) and [10.4](#).

10.2 Life distribution

Select an initial life distribution (it can be changed later, if necessary). For pneumatic components, the Weibull distribution is commonly used, and its scale parameter, η , is selected to be the life characteristic that is stress-dependent; while the slope β is assumed to remain constant across different stress levels.

Plot the raw data from all stress levels on one graph and obtain a best fit straight line to the data from each stress level (see [Figure 4](#) for an example). If the slopes β from each stress level are not parallel, consider a compromise slope for each set of stress levels (see [Figure 5](#)). A judgment is necessary as to whether the compromise slope is statistically acceptable (see example in [Annex C](#)), and if it is judged not acceptable, the testing program is restarted with improved data collection methods. It is necessary to have a constant value of the slope β for each stress level.

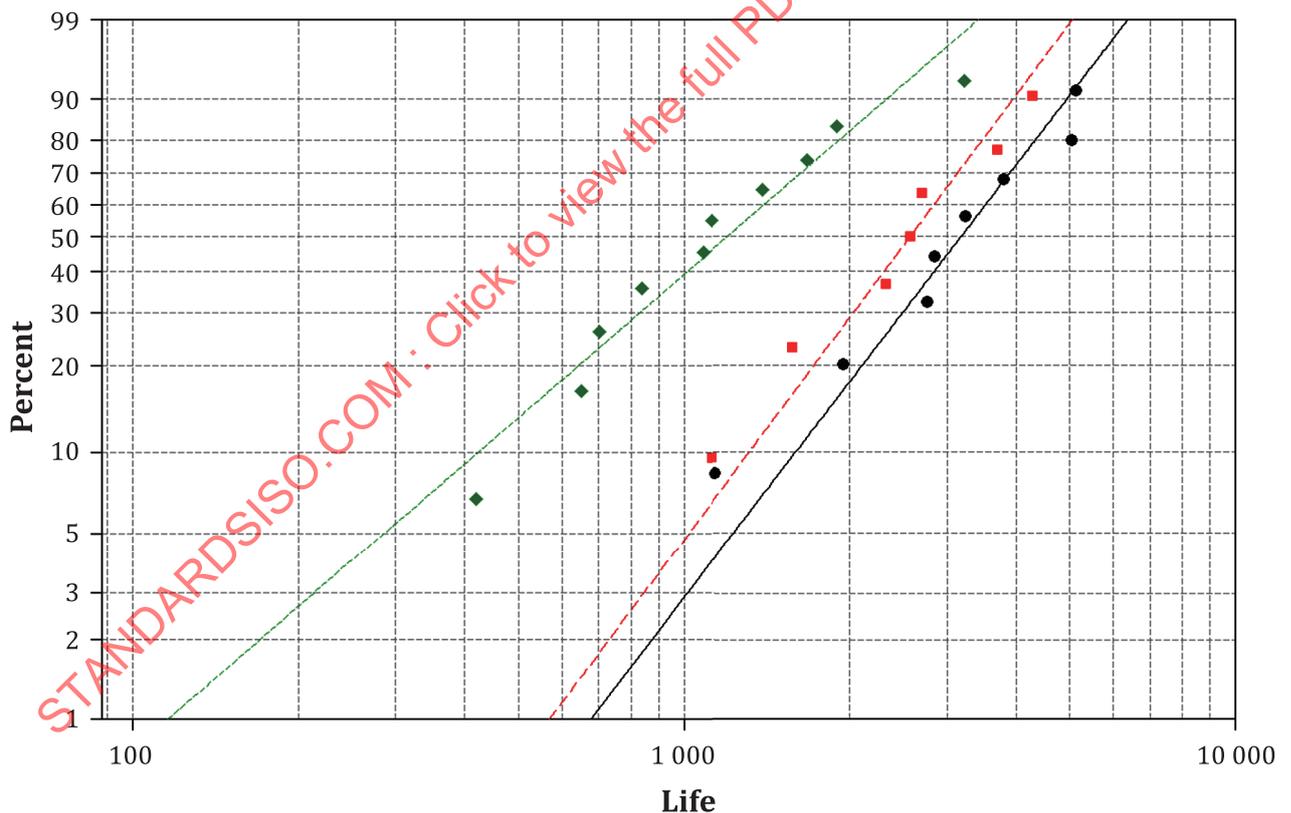


Figure 4 — Best fit slope to raw data

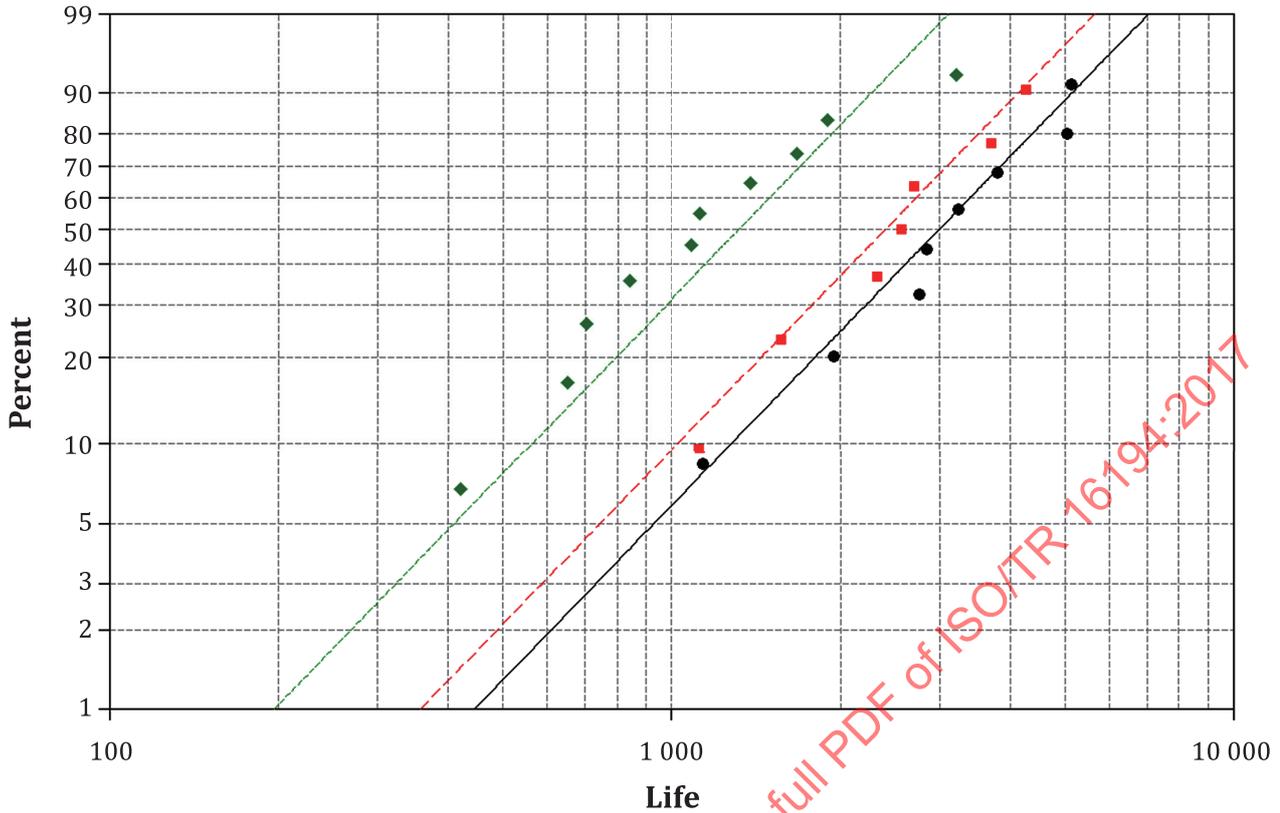


Figure 5 — Compromised equal slope lines

The resulting distribution is verified by statistical analysis as described in [Annex C](#). If the lines fitted from the plotted data at each accelerating stress level are parallel, it implies that the failure mechanism at each stress level is the same, and the selected stress levels for the accelerated testing are appropriate.

10.3 Accelerated life testing model

Select or create a model of accelerated life testing that describes a life characteristic of the distribution from one stress level to another; this is also called a life-stress relationship model. Examples of these models include the Arrhenius, Eyring, Inverse Power Law, etc., and are described in [Annex B](#).

10.4 Data analysis and parameter estimation

Using the selected life-stress relationship model, estimate the parameters of the life-stress distribution using either a graphical method, a least squares method, or the maximum likelihood estimation (MLE) method. An example using the Arrhenius model with a graphical estimation method is shown in [Figure 6](#).

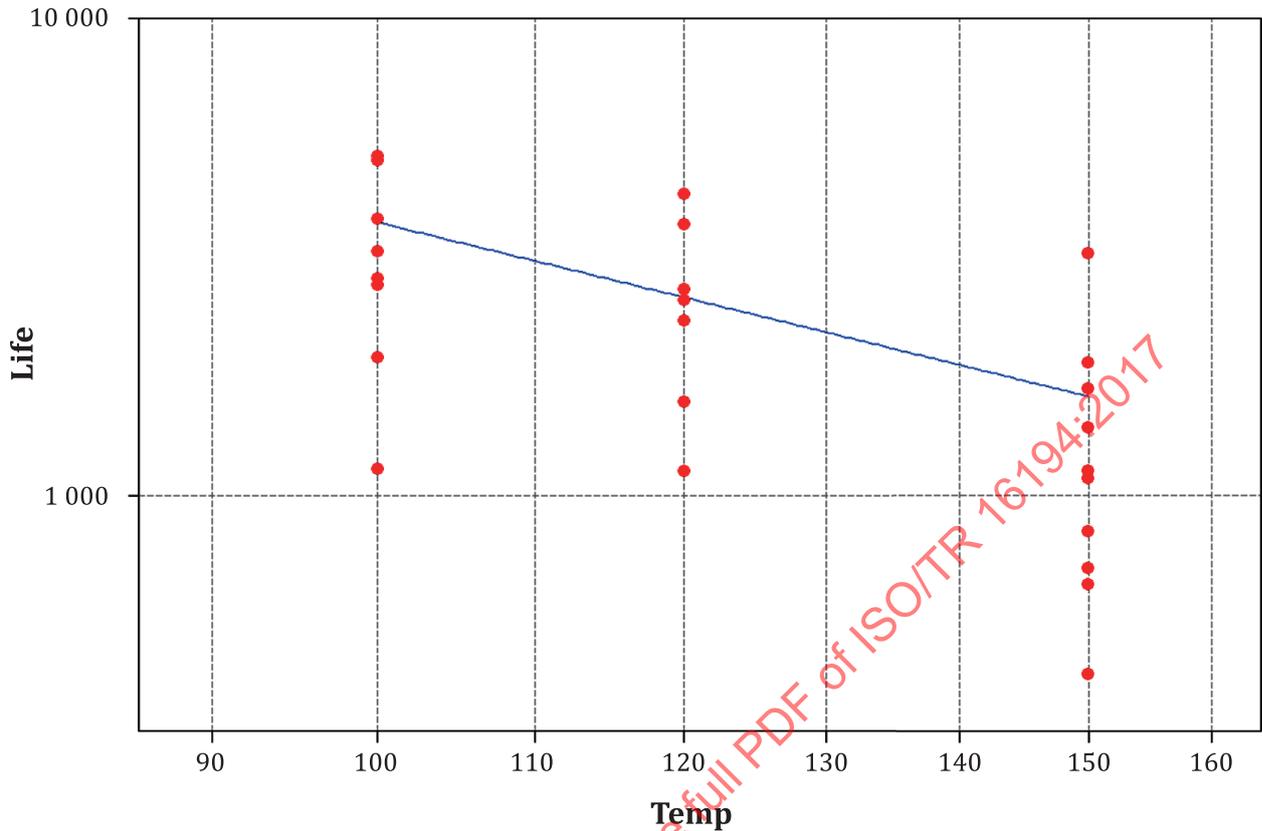


Figure 6 — Arrhenius plot of data from Figure 5

In Figure 6, the individual dots are the raw data points, and the connecting line joins the characteristic life η from each stress level. The example curves in Figures 4, 5 and 6 used a Weibull distribution.

NOTE Commercial software can be helpful in developing all of these plots.

The acceleration factor (AF) can now be determined from a simple proportion of lives at the normal use life to those at any accelerated condition. Methods of calculating acceleration factors are given in Annex B of this document and an example is shown in Annex C.

11 Reliability characteristics from the test data

To improve the interpretation of the calculation results, the failure mode for each test unit is recorded. Calculations are made from the test data at each stress level to determine:

- characteristic life η ;
- Weibull shape parameter β , slope of the straight line in the Weibull plot;
- the mean life, which provides a measure of the average time of operation to failure;
- B_x life, which is the time by which X% of the components are estimated to fail; and
- the confidence intervals of the B_x life at the 95% confidence level using Fisher information matrix,

Calculations are made from the life-stress analysis to determine:

- model parameters and acceleration factor; and
- B_x life and confidence intervals of B_x life at the normal use conditions.

12 Test report

The test report includes at least the following data:

- a) the number of this document, including the component-specific part number;
- b) date of the test report;
- c) component description (manufacturer, type designation, series number, date code);
- d) sample size;
- e) test conditions (types of stress, number of stress levels, stress loading, etc.);
- f) threshold levels;
- g) shape parameter (β);
- h) types of failures for each test unit;
- i) B_{10} life and confidence intervals of B_{10} life at 95% confidence level under normal use conditions;
- j) characteristic life η under normal use conditions;
- k) number of failures considered;
- l) method used to calculate the Weibull data (Maximum likelihood, etc.);
- m) model for accelerated life testing (Arrhenius-Weibull, Eyring-Weibull, Inverse power law-Weibull, etc.);
- n) acceleration factor;
- o) parameters of the selected acceleration model;
- p) other remarks, as necessary.

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Annex A (informative)

Determining stress levels when stress is time-dependent

When the stress is time-dependent, the component is subjected to a stress level that varies with time. Components subjected to time-dependent stress loadings yield failures more quickly, and models that fit them are valuable methods of accelerated life testing.

The step-stress model and the related ramp-stress model are typical cases of time-dependent stress tests. In these cases, the stress load remains constant for a period of time and then is stepped/ramped into a different stress level where it remains constant for another time interval until it is stepped/ramped again. There are numerous variations of this concept as shown in Figures A.1 to A.4:

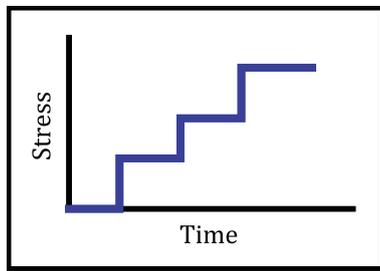


Figure A.1 — Step stress model

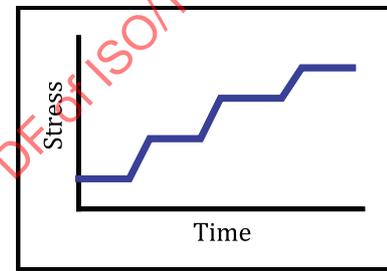


Figure A.2 — Ramp stress model

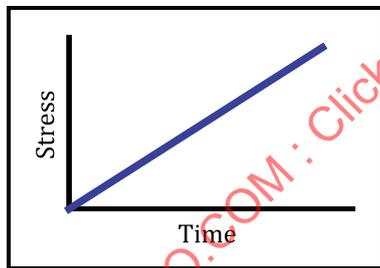


Figure A.3 — Increasing stress model

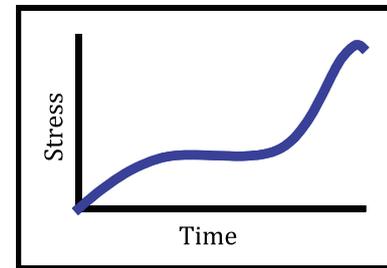


Figure A.4 — Complete time-dependent stress model

There are some cases where the stress in a field operating condition is variable. In that case, the following steps are helpful to process the accelerated life test:

- a) First, identify the field operating condition for a related component. The result using histogram is shown in Figure A.5.
- b) Calculate equivalent load needed for accelerated life testing using Palmgren-Miner's rule (see [Annex F](#)). Figure A.6 represents the equivalent load for the resulting accelerated life test.

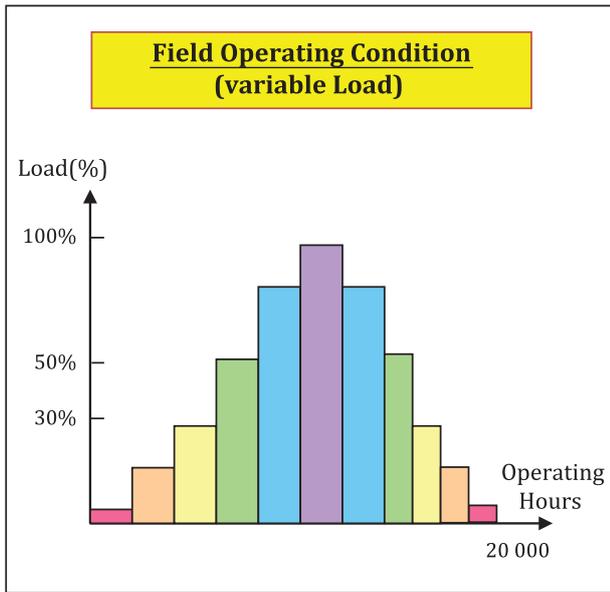


Figure A.5 — Field operating condition

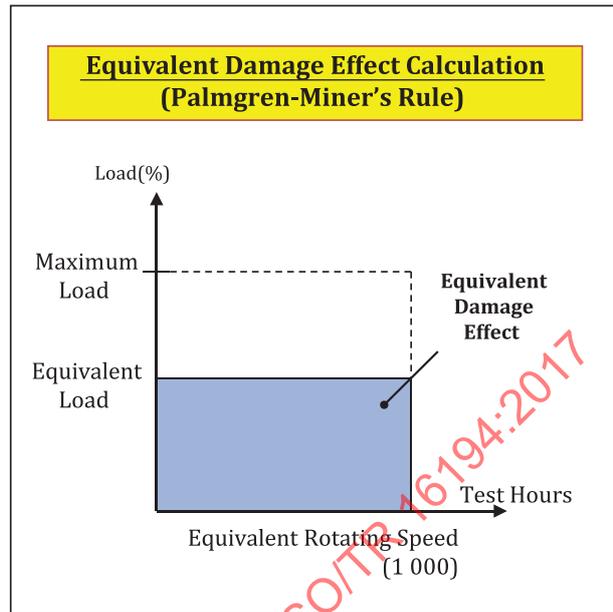


Figure A.6 — Equivalent damage effect calculation

- c) Decide upon a step-stress loading method to determine a destruct limit and yield point for the accelerated life testing. Figure A.7 shows step-stress loading method.
- d) Determine the appropriate stress range using destruct limit, operating limit (or elastic limit), and specification limit (proportional limit) of a strain-stress curve as shown in Figure A.8.
- e) Find the accelerated stress level using an accelerated life test curve as shown in Figure A.9. In the field of mechanical engineering, overstress levels commonly used in industry are 120 %, 133 %, and 150 %.
- f) Determine the stress levels using a step by step process (see Figure A.10) and the procedure given in 8.2. Accelerated life testing at the three accelerating stress levels can then be performed.

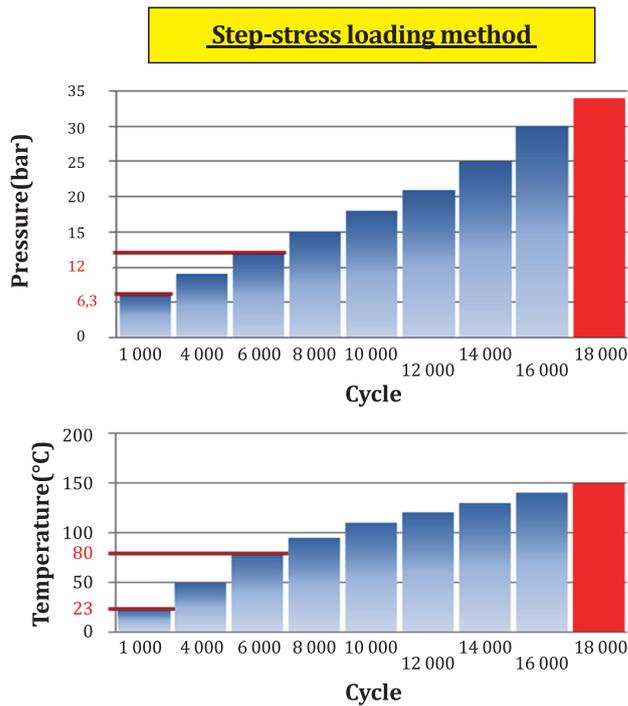


Figure A.7 — Step-stress loading method

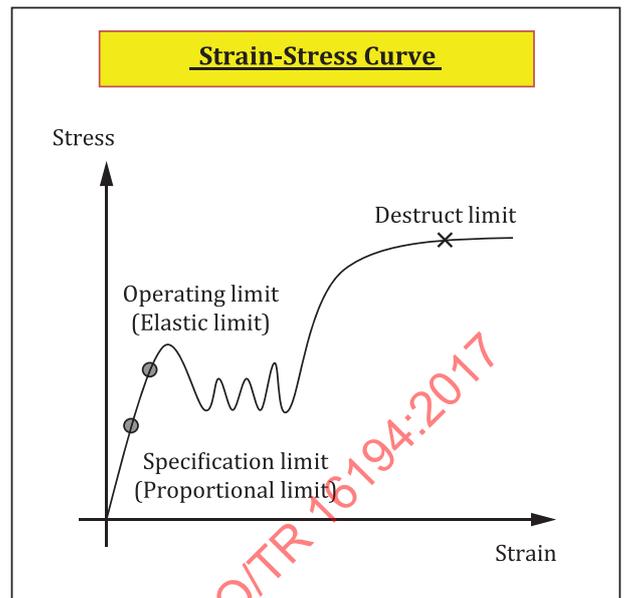


Figure A.8 — Strain-stress curve

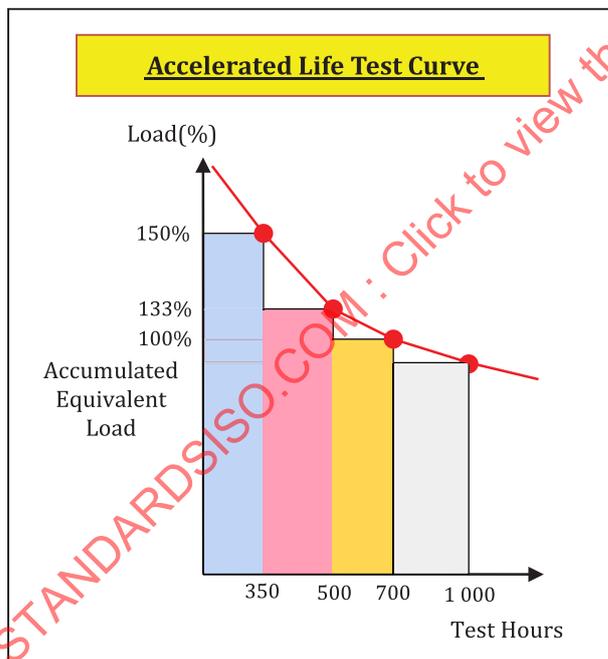


Figure A.9 — Accelerated life test curve

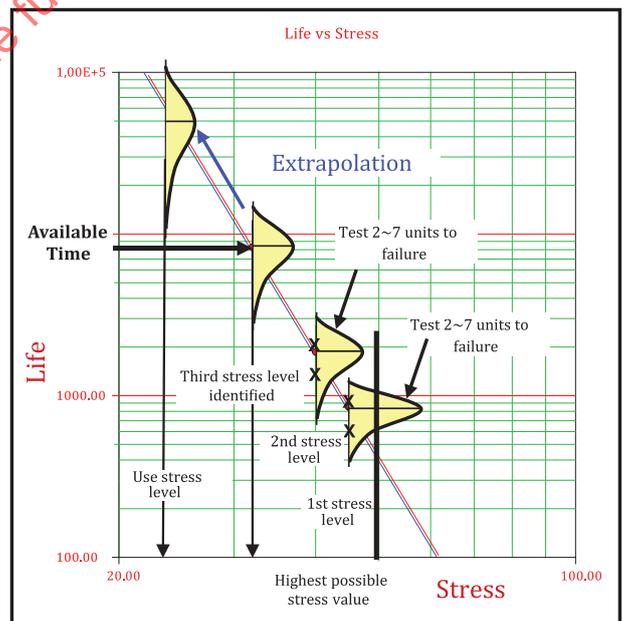


Figure A.10 — Decision method of stress levels

- g) Before estimating the reliability characteristics, check on the validation of accelerated test using probability plot in Figure A.11. If the fitted lines of the plotted data at each accelerating stress levels are parallel, it means that assumed lifetime distribution is appropriate and the accelerating stress is effective.
- h) Check the error between the estimates of the considered model and real test results. First, check that the shape parameters acquired from the considered model, and tested results in normal use conditions, are the same. Second, check if the scale parameter of the considered model resides in the

confidence intervals of scale parameter from the test results. Finally, if the scale parameter of the considered model is within the confidence intervals, it could be judged that both the characteristic life of the considered model and test result are not statistically different. Figure A.12 shows the graphical explanation of the error between estimate of the considered model and test result.

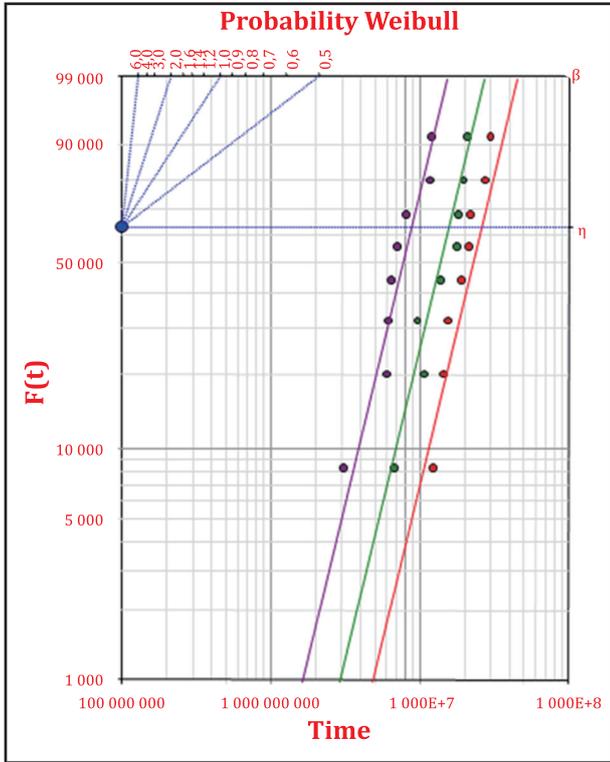


Figure A.11 — Validation and verification of accelerated test

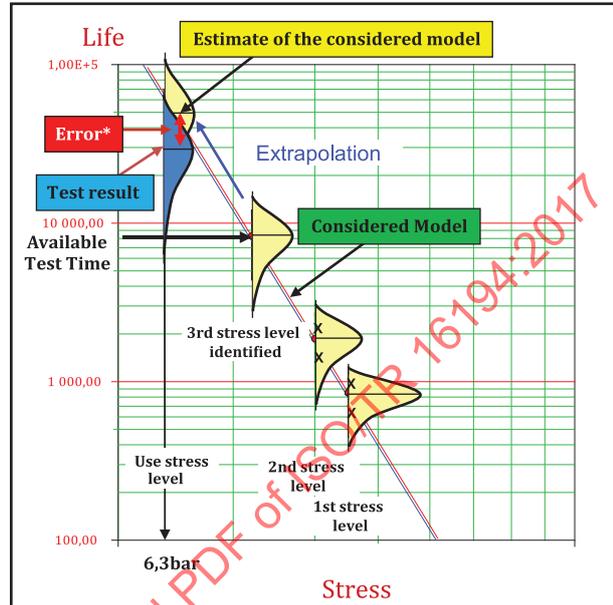


Figure A.12 — Graphical explanation of the error between test estimate of the considered model and test result

Annex B (informative)

Life-stress relationship models

B.1 Acceleration factor

The acceleration factor is a unitless number that relates a component's life at an accelerated stress level to the life at the normal use stress level. It is defined by;

$$AF = \frac{L_U}{L_A} \quad (\text{B.1})$$

where

L_U is the life at the normal use stress level

L_A is the life at the accelerated stress level

As it can be seen in [Formula \(B.1\)](#), the acceleration factor depends on the life-stress model and is thus a function of stress.

B.2 Arrhenius life-stress model

The Arrhenius life-stress model (or relationship) is probably the most common life-stress model utilized in accelerated life testing. It has been widely used when the stimulus or accelerated stress is thermal (i.e. temperature).

The Arrhenius life-stress model is formulated by assuming that life is proportional to the inverse reaction rate of the process, thus the Arrhenius life-stress model is given by;

$$L(V) = C \cdot e^{\frac{B}{V}} \quad (\text{B.2})$$

where

L is the quantifiable life measure (mean life, characteristic life, median life, B_x life, etc.)

V is the stress level (temperature values in degrees Kelvin)

C and B are the model parameter ($C > 0$, $B > 0$)

The choice of the Arrhenius model is justified by the fact that this is a physics-based model derived for temperature dependence.

The Arrhenius model is linearized by taking the natural logarithm of both sides in [Formula \(B.2\)](#).

$$\ln(L(V)) = \ln(C) + \frac{B}{V} \quad (\text{B.3})$$

Depending on the application (and where the stress is exclusively thermal), the parameter B can be replaced by;

$$B = \frac{E_A}{K} = \frac{\text{activation energy}}{\text{Boltzman's constant}} = \frac{\text{activation energy}}{8,623 \times 10^{-5} \text{ eVK}^{-1}} \quad (\text{B.4})$$

The activation energy is meant to be known a priori. If the activation energy is known, then only model parameter C remains. Because this is rarely the case in most real-life situations, all subsequent formulations can assume that this activation energy is unknown and treat B as one of the model parameters. B is a measure of the effect that the stress (i.e. temperature) has on the life. The larger the value of B , the higher the dependency of the life on the specific stress.

Most practitioners use the term acceleration factor to refer to the ratio of the life (or acceleration characteristic) between the normal use level and a higher test stress level. For the Arrhenius model, acceleration factor is;

$$AF = \frac{L_{USE}}{L_{Accelerated}} = \frac{C \cdot e^{\frac{B}{V_U}}}{C \cdot e^{\frac{B}{V_A}}} = e^{\left(\frac{B}{V_U} - \frac{B}{V_A} \right)} \quad (\text{B.5})$$

The probability density function for 2-parameter Weibull distribution is given by;

$$f(t) = \frac{\beta}{\eta} \left(\frac{t}{\eta} \right)^{\beta-1} e^{-\left(\frac{t}{\eta} \right)^\beta} \quad (\text{B.6})$$

The scale parameter (or characteristic life) of the Weibull distribution is η . The Arrhenius-Weibull model's probability density function at a stress level V can then be obtained by setting $\eta = L(V)$ in [Formula \(B.2\)](#);

$$\eta = L(V) = C \cdot e^{\frac{B}{V}} \quad (\text{B.7})$$

and substituting for η in [Formula \(B.6\)](#);

$$f(t;V) = \frac{\beta}{C \cdot e^{\frac{B}{V}}} \left(\frac{t}{C \cdot e^{\frac{B}{V}}} \right)^{\beta-1} e^{-\left(\frac{t}{C \cdot e^{\frac{B}{V}}} \right)^\beta} \quad (\text{B.8})$$

The mean time to failure (MTTF) of the Arrhenius-Weibull model is given by;

$$MTTF = C \cdot e^{\frac{B}{V}} \cdot \Gamma\left(\frac{1}{\beta} + 1 \right) \quad (\text{B.9})$$

where $\Gamma(\cdot)$ is the gamma function.

The Arrhenius-Weibull reliability function at stress level V is given by;

$$R(t;V) = e^{-\left(\frac{t}{C \cdot e^{\frac{B}{V}}}\right)^\beta} \quad (\text{B.10})$$

B.3 Inverse power law life-stress model

The inverse power law (IPL) model is commonly used for non-thermal accelerated stresses and is given by;

$$L(V) = \frac{1}{KV^n} \quad (\text{B.11})$$

where

L is the quantifiable life measure (mean life, characteristic life, median life, B_x life, etc.)

V is the stress level

K and n are model parameters ($K > 0, n > 0$)

The inverse power law appears as a straight line when plotted on a log-log paper. The equation of the line is given by;

$$\ln(L) = -\ln(K) - n \ln(V) \quad (\text{B.12})$$

The parameter η in the inverse power model is a measure of the effect of the stress on the life, i.e. the larger the value of n , the greater the effect of the stress. A value of n approaching 0 indicates small effect of the stress on the life, with no effect (constant life with stress) when $n = 0$.

For the inverse power law model, the acceleration factor is given by;

$$AF = \frac{L_{USE}}{L_{Accelerated}} = \frac{\frac{1}{KV_U^n}}{\frac{1}{KV_A^n}} = \left(\frac{V_A}{V_U}\right)^n \quad (\text{B.13})$$

The inverse power law Weibull model can be derived by setting $\eta = L(V)$, yielding the following IPL-Weibull probability density function at stress level V ;

$$f(t;V) = \beta \cdot K \cdot V^n \left(K \cdot V^n \cdot t\right)^{\beta-1} e^{-\left(K \cdot V^n \cdot t\right)^\beta} \quad (\text{B.14})$$

The mean time to failure (MTTF) of the IPL-Weibull model is given by;

$$MTTF = \frac{1}{KV^n} \cdot \Gamma\left(\frac{1}{\beta} + 1\right) \quad (\text{B.15})$$

The IPL-Weibull reliability function at stress level V is given by;

$$R(t;V) = e^{-\left(K \cdot V^n \cdot t\right)^\beta} \quad (\text{B.16})$$

B.4 Eyring life-stress model

The Eyring life-stress model was formulated from quantum mechanics principles and is most often used when thermal stress (temperature) is the acceleration variable. However, the Eyring model is also often used for stress variables other than temperature, such as humidity. The model is given by;

$$L(V) = \frac{1}{V} e^{-\left(\frac{A-B}{V}\right)} \tag{B.17}$$

where

L is the quantifiable life measure (mean life, characteristic life, median life, B_x life, etc.)

V is the stress level

A and B are model parameters

For the Eyring model the acceleration factor is given by;

$$AF = \frac{L_{USE}}{L_{Accelerated}} = \frac{\frac{1}{V_u} e^{-\left(\frac{A-B}{V_u}\right)}}{\frac{1}{V_A} e^{-\left(\frac{A-B}{V_A}\right)}} = \frac{V_A}{V_U} e^{B\left(\frac{1}{V_U} - \frac{1}{V_A}\right)} \tag{B.18}$$

The Eyring-Weibull model can be derived by setting $\eta = L(V)$, yielding the following Eyring-Weibull probability density function at stress level V ;

$$f(t;V) = \beta \cdot V \cdot e^{\left(\frac{A-B}{V}\right)} \left(t \cdot V \cdot e^{\left(\frac{A-B}{V}\right)} \right)^{\beta-1} e^{-\left(t \cdot V \cdot e^{\left(\frac{A-B}{V}\right)} \right)^\beta} \tag{B.19}$$

The mean time to failure (MTTF) of the Eyring-Weibull model is given by;

$$MTTF = \frac{1}{V} \cdot e^{-\left(\frac{A-B}{V}\right)} \cdot \Gamma\left(\frac{1}{\beta} + 1\right) \tag{B.20}$$

The Eyrin-Weibull reliability function at stress level V is given by;

$$R(t;V) = e^{-\left(V \cdot t \cdot e^{\left(\frac{A-B}{V}\right)} \right)^\beta} \tag{B.21}$$

B.5 Temperature-humidity combination model

The temperature-humidity (T-H) combination model, a variation of the Eyring relationship, has been proposed for predicting the life at normal use conditions when temperature and humidity are the accelerated stresses in a test. This combination model is given by;

$$L(V;U) = A \cdot e^{\left(\frac{\Phi}{V} + \frac{b}{U}\right)} \quad (\text{B.22})$$

where

L is the quantifiable life measure (mean life, characteristic life, median life, B_x life, etc.)

V is the temperature

U is the relative humidity (decimal or percentage)

Φ is a model parameter

B is a model parameter (also known as the activation energy for humidity)

A is a constant and model parameter

The T-H combination model can be linearized and plotted on a life vs. stress plot. The model is linearized by taking the natural logarithm of both sides in [Formula \(B.22\)](#), or;

$$\ln(L(V;U)) = \ln(A) + \frac{\Phi}{V} + \frac{b}{U} \quad (\text{B.23})$$

Depending on which type of stress is kept constant, it can be seen from [Formula \(B.23\)](#) that either the parameter Φ or the parameter b is the slope of the resulting line. If, for example, the humidity is kept constant, then Φ is the slope of the life line in a life vs. temperature plot. The steeper the slope, the more the component's life depends on the effect of temperature. In other words, Φ is a measure of the effect that temperature has on the life, and b is a measure of the effect that relative humidity has on the life. The larger the value of Φ , the more the life depends on the effect of temperature. Similarly, the larger the value of b , the more the life depends on the effect of relative humidity.

The acceleration factor for the T-H model is given by;

$$AF = \frac{L_{USE}}{L_{Accelerated}} = \frac{A \cdot e^{\left(\frac{\Phi + b}{V_U + U_U}\right)}}{A \cdot e^{\left(\frac{\Phi + b}{V_A + U_A}\right)}} = e^{\left(\frac{1}{V_U} - \frac{1}{V_A}\right) + b \left(\frac{1}{U_U} - \frac{1}{U_A}\right)} \quad (B.24)$$

By setting $\eta = L(V;U)$ as given in [Formula \(B.22\)](#), the T-H Weibull model's probability density function at stress level V and U is given by

$$f(t;V;U) = \frac{\beta}{A} e^{-\left(\frac{\Phi + b}{V + U}\right)} \left(\frac{t}{A} e^{-\left(\frac{\Phi + b}{V + U}\right)} \right)^{\beta-1} e^{-\left(\frac{t}{A} e^{-\left(\frac{\Phi + b}{V + U}\right)}\right)^\beta} \quad (B.25)$$

The mean time to failure (MTTF) of the T-H Weibull model is given by;

$$MTTF = A \cdot e^{\left(\frac{\Phi + b}{V + U}\right)} \cdot \Gamma\left(\frac{1}{\beta} + 1\right) \quad (B.26)$$

The T-H Weibull reliability function at stress level V and U is given by;

$$R(t;V;U) = e^{-\left(\frac{t}{A} e^{-\left(\frac{\Phi + b}{V + U}\right)}\right)^\beta} \quad (B.27)$$

B.6 Temperature-nonthermal combination model

When temperature and a second non-thermal stress (e.g. voltage or pressure) are the accelerated stresses of a test, then the Arrhenius and the inverse power law relationships can be combined to yield the temperature-nonthermal (T-NT) combination model. This model is given by;

$$L(V;U) = \frac{C}{U^n \cdot e^{-\frac{B}{V}}} \quad (B.28)$$

where

L is the quantifiable life measure (mean life, characteristic life, median life, B_x life, etc.)

V is the temperature (in degrees K)

U is the non-thermal stress (i.e. voltage, vibration, pressure, etc.)

B, C and n are model parameters

The T-NT combination model can be linearized and plotted on a life vs. stress plot. The model is linearized by taking the natural logarithm of both sides in [Formula \(B.28\)](#) or;

$$\ln(L(V;U)) = \ln(C) - n \ln(U) + \frac{B}{V} \quad (B.29)$$

Because the life is now a function of two stresses, a life vs. stress plot can only be obtained by keeping one of the two stresses constant and varying the other.

The acceleration factor for the T-NT model is given by;

$$AF = \frac{L_{USE}}{L_{Accelerated}} = \frac{\frac{C}{U_U^n} e^{\frac{B}{V_U}}}{\frac{C}{U_A^n} e^{\frac{B}{V_A}}} = \left(\frac{U_A}{U_U} \right)^n \cdot e^{B \left(\frac{1}{V_U} - \frac{1}{V_A} \right)} \quad (B.30)$$

By setting $\eta = L(V, U)$ as given in [Formula \(B.28\)](#), the T-NT Weibull model's probability density function at stress levels V and U is given by

$$f(t; V; U) = \frac{\beta \cdot U^n \cdot e^{-\frac{B}{V}}}{C} \left(\frac{t \cdot U^n \cdot e^{-\frac{B}{V}}}{C} \right)^{\beta-1} e^{-\left(\frac{t \cdot U^n \cdot e^{-\frac{B}{V}}}{C} \right)^\beta} \quad (B.31)$$

The mean time to failure (MTTF) of the T-NT Weibull model is given by;

$$MTTF = \frac{C}{U^n \cdot e^{-\frac{B}{V}}} \cdot \Gamma \left(\frac{1}{\beta} + 1 \right) \quad (B.32)$$

The T-NT Weibull reliability function at stress levels V and U is given by;

$$R(t; V; U) = e^{-\left(\frac{t \cdot U^n \cdot e^{-\frac{B}{V}}}{C} \right)^\beta} \quad (B.33)$$

B.7 General log-linear model

When a test involves multiple accelerating stresses or requires an engineering variable and the interaction terms between stress variables, a general multivariable model is needed. Such a model is the general log-linear (GLL) model, which describes a life characteristic as a function of n stresses. Mathematically the model is given by;

$$L(X_1, X_2, \dots, X_n) = \exp \left(\alpha_0 + \sum_{j=1}^n \alpha_j X_j \right) \quad (B.34)$$

where

α_0, α_j are model parameters

X_x is the stress or interaction between stress variables

This model can be further modified through the use of transformations and can be reduced to the model discussed previously. As an example, consider two stresses and interaction between two stresses application of this GLL model and inverse, natural logarithmic, and linear transformation on X_s . Stress variables of this model are temperature (X_1), pressure (X_2), and interaction (X_1X_2) of temperature and pressure. This model can use three stress variables through transformation such as inverse

transformation on temperature ($1/X_1$), natural logarithmic transformation on pressure ($\ln(X_2)$), and linear transformation on interaction ($\ln(X_2)/X_1$).

$$L = \exp\left(\alpha_0 + \frac{\alpha_1}{T} + \alpha_2 \ln(P) + \alpha_3 \frac{\ln(P)}{T}\right) \tag{B.35}$$

where

T is temperature

P is pressure

The model is linearized by taking the natural logarithm of both sides in [Formula \(B.35\)](#) or;

$$\ln(L) = \alpha_0 + \frac{\alpha_1}{T} + \alpha_2 \ln(P) + \alpha_3 \frac{\ln(P)}{T} \tag{B.36}$$

The appropriate transformations for some widely used life-stress relationships are given in [Table B.1](#)

Table B.1 — Transformation for the life-stress relationship

Life-stress relationship	Arrhenius	Inverse Power Law	Temperature-Nonthermal
Transformation	$1/X$	$\ln(X)$	Temperature: $1/X_1$ Nonthermal: $\ln(X_2)$

The general log-linear model can be combined with any of the available life distributions by expressing a life characteristic from that distribution with the GLL model. The GLL-Weibull model can be derived by setting $\eta = L(X_1, X_2, L, X_n)$ in [Formula \(B.34\)](#), yielding the following GLL-Weibull probability density function;

$$f(t; X_1, X_2, \dots, X_n) = \beta \cdot t^{\beta-1} \cdot \exp\left(-\beta \left(\alpha_0 + \sum_{j=1}^n \alpha_j X_j\right)\right) \cdot \exp\left(-t^\beta \cdot \exp\left(-\beta \left(\alpha_0 + \sum_{j=1}^n \alpha_j X_j\right)\right)\right) \tag{B.37}$$

The total number of unknowns to solve for in this model is $n+2$ ($\beta, \alpha_0, \alpha_1, \dots, \alpha_n$).

The maximum likelihood estimation method can be used to determine the parameters for the GLL model and the selected life distribution. For each distribution, the likelihood function can be derived,

and the model parameters (in the case of Weibull: $\beta, \alpha_0, \alpha_1, \dots, \alpha_n$) can be obtained by maximizing the log likelihood function. The log likelihood function for the Weibull distribution is given by:

$$\ln(L) = \sum_{i=1}^{Fe} N_i \ln \left[\beta \cdot T_i^{\beta-1} \exp \left(-T_i^\beta \cdot \exp \left(-\beta \left(\alpha_0 + \sum_{j=1}^n \alpha_j X_{i,j} \right) \right) \right) \cdot \exp \left(-\beta \left(\alpha_0 + \sum_{j=1}^n \alpha_j X_{i,j} \right) \right) \right] - \sum_{i=1}^S N_i' (T_i')^\beta \exp \left(-\beta \left(\alpha_0 + \sum_{j=1}^n \alpha_j X_{i,j} \right) \right) + \sum_{i=1}^{FI} N_i'' \ln [R_{Li}'' - R_{Ri}''] \quad (B.38)$$

where

$$R_{Li}'' = \exp \left(- \left(T_{Li}'' \cdot \exp \left(\alpha_0 + \sum_{j=1}^n \alpha_j X_j \right) \right)^\beta \right)$$

$$R_{Ri}'' = \exp \left(- \left(T_{Ri}'' \cdot \exp \left(\alpha_0 + \sum_{j=1}^n \alpha_j X_j \right) \right)^\beta \right)$$

and

F_e is the number of groups of exact times-to-failure data points

N_i is the number of times-to-failure in the i^{th} time-to-failure data group

λ is the failure rate parameter (unknown)

T_i is the exact failure time of the i^{th} group

S is the number of groups of suspension data points

N_i'' is the number of suspensions in the i^{th} group of suspension data points

T_i' is the running time of the i^{th} suspension data group

FI is the number of interval data groups

N_i'' is the number of intervals in the i^{th} group of data intervals

T_{Li}'' is the beginning of the i^{th} interval

T_{Ri}'' is the ending of the i^{th} interval

Annex C (informative)

Verification of compromise Weibull slopes

Before estimating the reliability characteristics, it is necessary to judge if the compromised parallel lines to the raw data are statistically acceptable. This is accomplished by a hypothesis test, where the null hypothesis is that the Weibull slopes of the compromised parallel lines are not equal; and the alternate hypothesis is that they are equal.

The process is demonstrated by using actual data from a pneumatic cylinder test as shown in [Figure C.1](#).

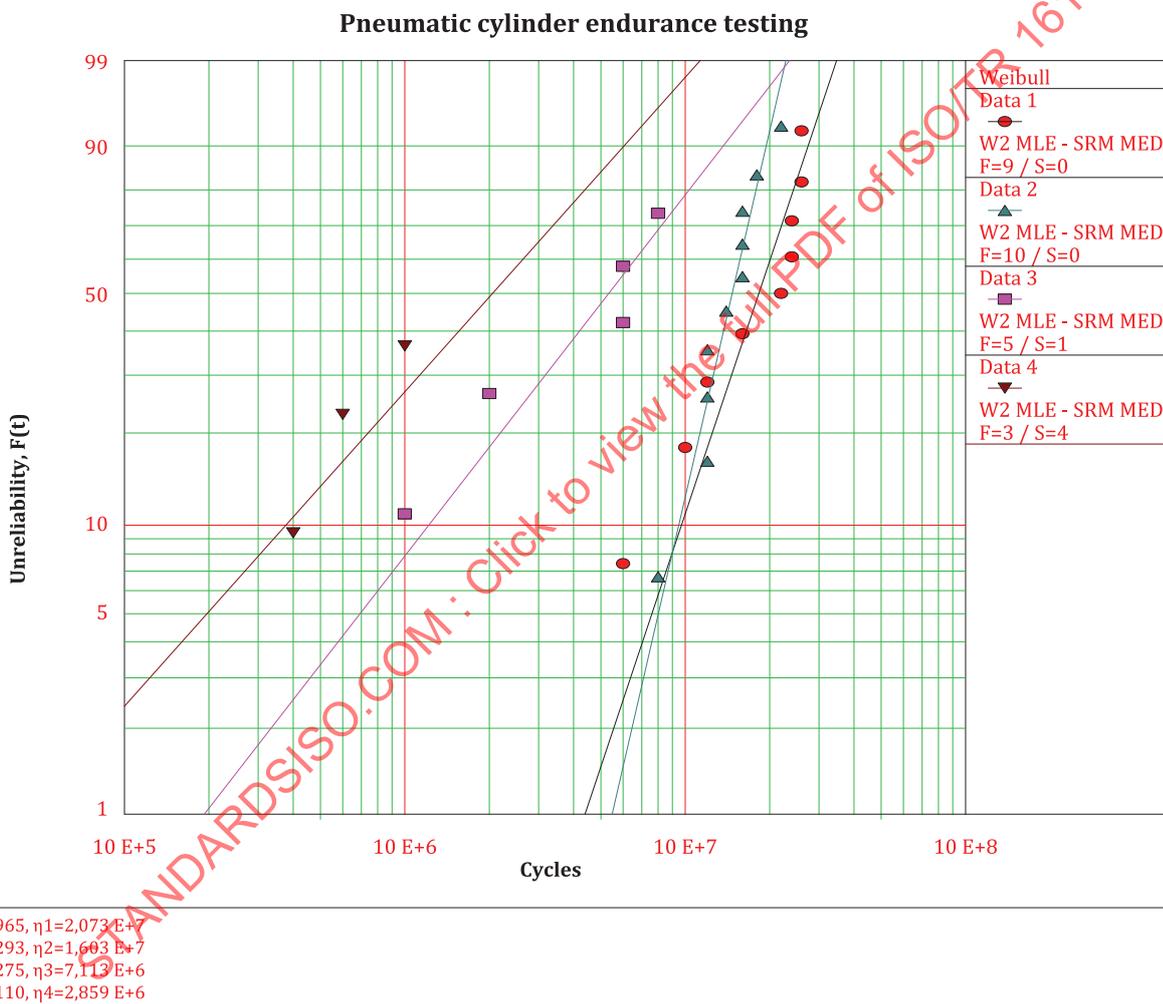


Figure C.1 — Pneumatic cylinder test

The test included data for 6,3 bar, which is the normal condition that is desired to be estimated from the accelerated testing. So, for this example, it can be used to judge the accuracy of the projection from the accelerated conditions. All tests were conducted at the normal temperature of 23°C.

But, the Weibull curve for the 8 bar data is observed to be quite different than the other curves and would create inaccuracies in making a compromise adjustment to obtain parallel Weibull slopes. When such a condition is observed, the test conduct and specimens are examined to determine the cause of the problem. Then the test is usually rerun to get better data. For the sake of this example however,

assume that a new set of data (artificial) was obtained as described in the column for 8 bar in [Table C.1](#). Data for the other columns are the actual test results.

Table C.1 — Example of test results at normal, and three accelerated stress levels

Stress (pressure)	6,3 bar (Normal)	8 bar	12 bar	18 bar
Cycles to failure	6,0E+06	3,00E+06	1,00E+06	4,00E+05
	1,0E+07	6,00E+06	2,00E+06	6,00E+05
	1,2E+07	9,00E+06	6,00E+06	1,00E+06
	1,6E+07	9,00E+06	6,00E+06	^a 1,20E+06
	2,2E+07	1,20E+07	8,00E+06	^a 2,00E+06
	2,4E+07	1,40E+07	^a 1,20E+07	^a 2,00E+06
	2,4E+07	1,60E+07		
	2,6E+07	1,60E+07		
	2,6E+07	1,80E+07		
		2,20E+07		
^a indicates suspension				

The Weibull probability plot of the new raw data is shown in [Figure C.2](#), with the Weibull slopes and characteristic lives. Using a Minitab software program, adjustments are made to obtain compromised parallel slopes for the three sets of curves at the higher, accelerated pressures; and this is shown in [Figure C.3](#). The curve for 6,3 bar pressure is not included but is used later to check the accuracy of the acceleration projection.

[Table C.2](#) describes the calculations used for the statistical judgment of the compromise adjustments to the parallel Weibull curves. The L_{RAW} log likelihood data is from the Weibull software, and data for β , η and $L_{PARALLEL}$ are from the Minitab software analysis. The log likelihood ratio, and Chi-squared calculations are also shown.

Table C.2 — Calculation results — parallel slopes

Test pressure (bar)	β	η	$L_{PARALLEL}$	L_{RAW}
8	1,687	13 334 574	-170,180	-169,3063
12	1,687	7 355 518	-83,928	-83,6220
18	1,687	2 347 152	-48,177	-47,7888
Total			-302,285	-300,7171

NOTE: Log likelihood ratio statistic:

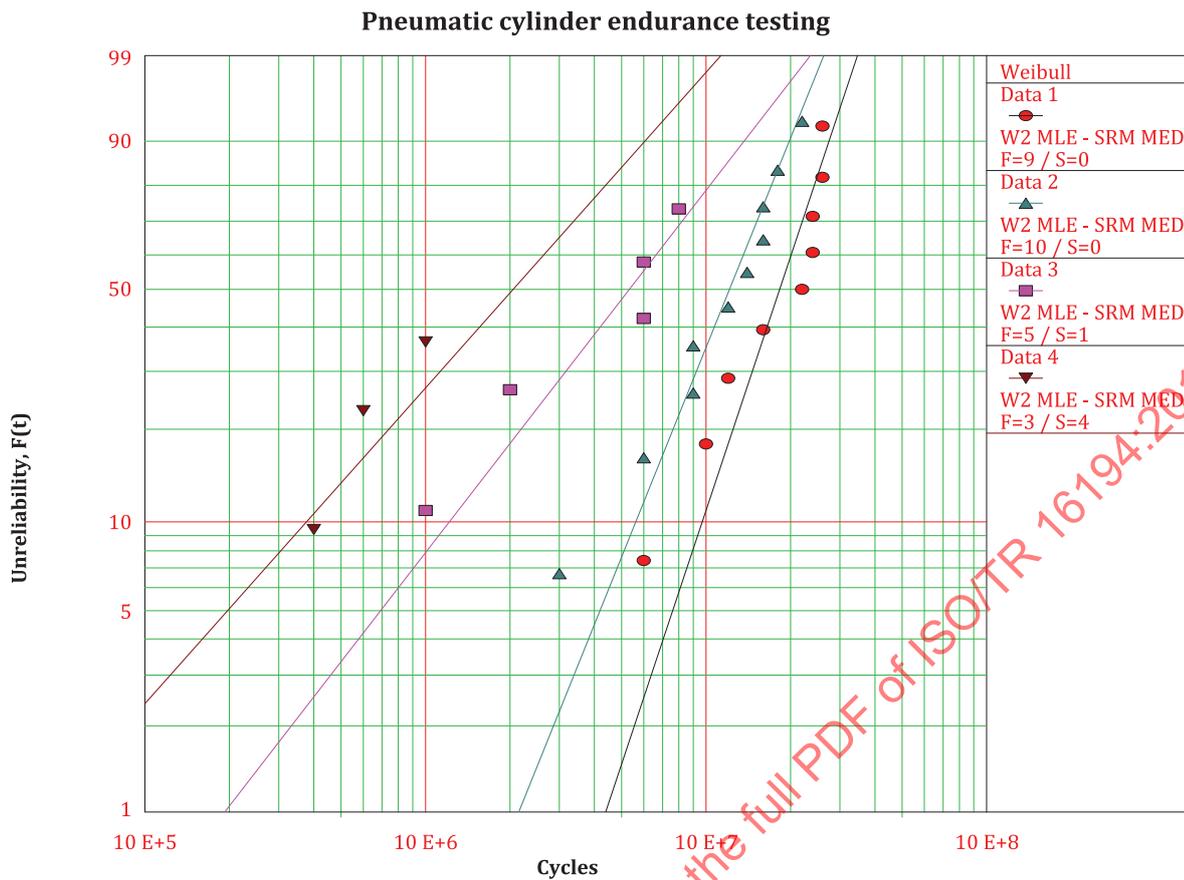
$$T = 2(\Sigma L_{RAW} - \Sigma L_{PARALLEL}) = 3,1358$$

Chi-squared @ $\alpha = 0,05$; DF = 2:

$$X^2 = 5,9915$$

$T \leq X^2$ therefore:

The slopes of the Weibull distributions do not differ significantly at the 5% significance level.



$\beta_1=2,965, \eta_1=2,073 \text{ E}+7$
 $\beta_2=2,449, \eta_2=1,409 \text{ E}+7$
 $\beta_3=1,275, \eta_3=7,113 \text{ E}+6$
 $\beta_4=1,110, \eta_4=2,859 \text{ E}+6$

Figure C.2 — Weibull plot for pneumatic cylinder with new, raw test data

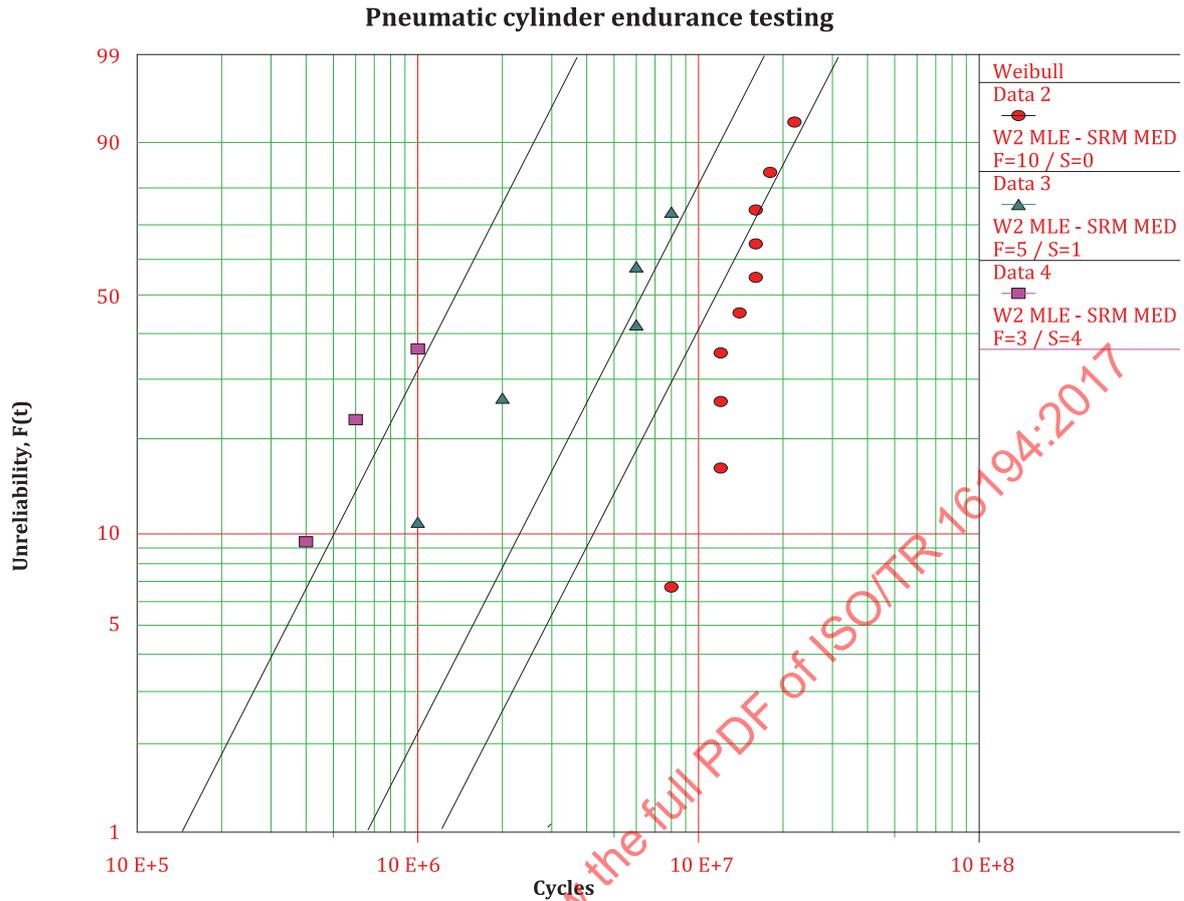


Figure C.3 — Weibull plot for pneumatic cylinder with compromised parallel slopes

The conclusion from the Chi-squared analysis is that the null hypothesis is rejected because the Weibull slopes do not differ significantly in the 5% significance level. Therefore, the alternate hypothesis is accepted that the Weibull curves are essentially parallel using the compromise slopes. A linear projection from the accelerated curves is shown in Figure C.4; along with the raw, normal pressure at 6,3 bar for comparison.

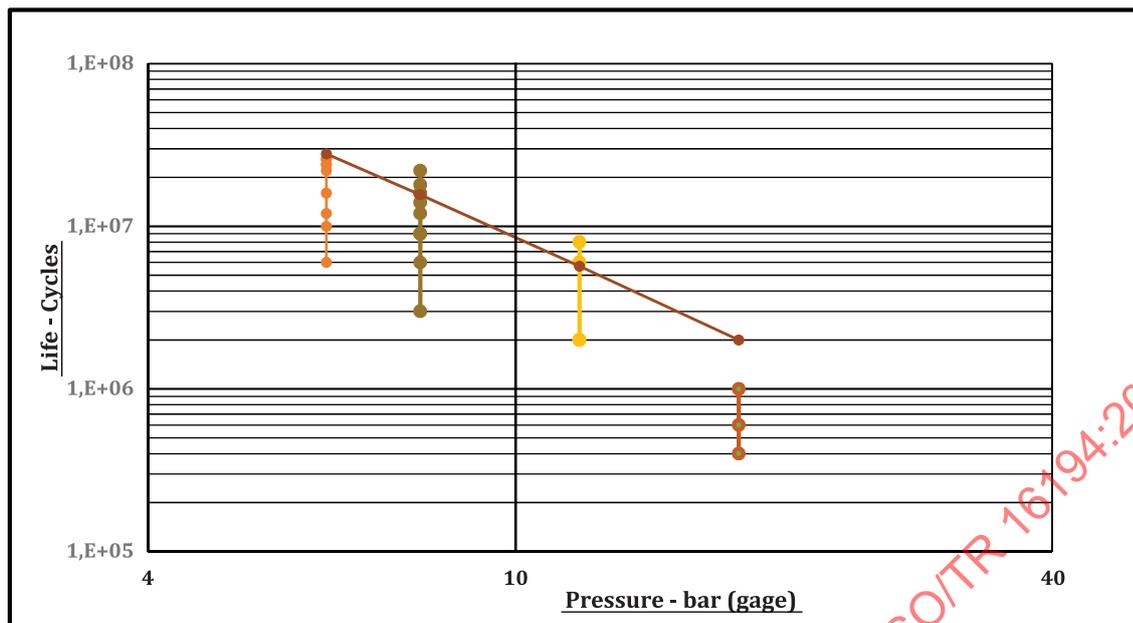


Figure C.4 — Acceleration projection plot

The linear projection (on log-log coordinates) is from the inverse power law, which is described in [Formula C.1](#):

$$L = \frac{1}{K(p)^n} \quad (C.1)$$

where

L life

p absolute pressure

K and n are constants

Using the characteristic life from the compromised slope test data, the constants for the inverse power law are determined by using a least squares best fit. This requires transforming [Formula C.1](#) and taking their logs to obtain a linear equation:

$$LP^n = \frac{1}{K} ; \ln L + \ln P^n = \ln \frac{1}{K} ; \ln L = \ln \frac{1}{K} - n \ln P ; y = a - nx \quad (\text{C.2})$$

The last equation in C.2 is modified to show a difference, instead of zero, when the terms are collected on one side:

$$\delta = y - a + nx \quad (\text{C.3})$$

This is now evaluated with the “Solver” program in Excel and tabulated results are shown below:

p (gage)	L	y = ln L	x = ln P	a = ln(1/K)	n	δ	δ ²	Σδ ²	L equation	Accuracy
6,3									2,3709E+07	85,6%
8	13334574	16,406	2,197	21,61012	2,328497	-0,088	0,008	0,045	1,4561E+07	90,8%
12	7355518	15,811	2,565			0,173	0,030		6,1850E+06	115,9%
18	2347152	14,669	2,944			-0,085	0,007		2,5561E+06	91,1%
			K =	4,12E-10						

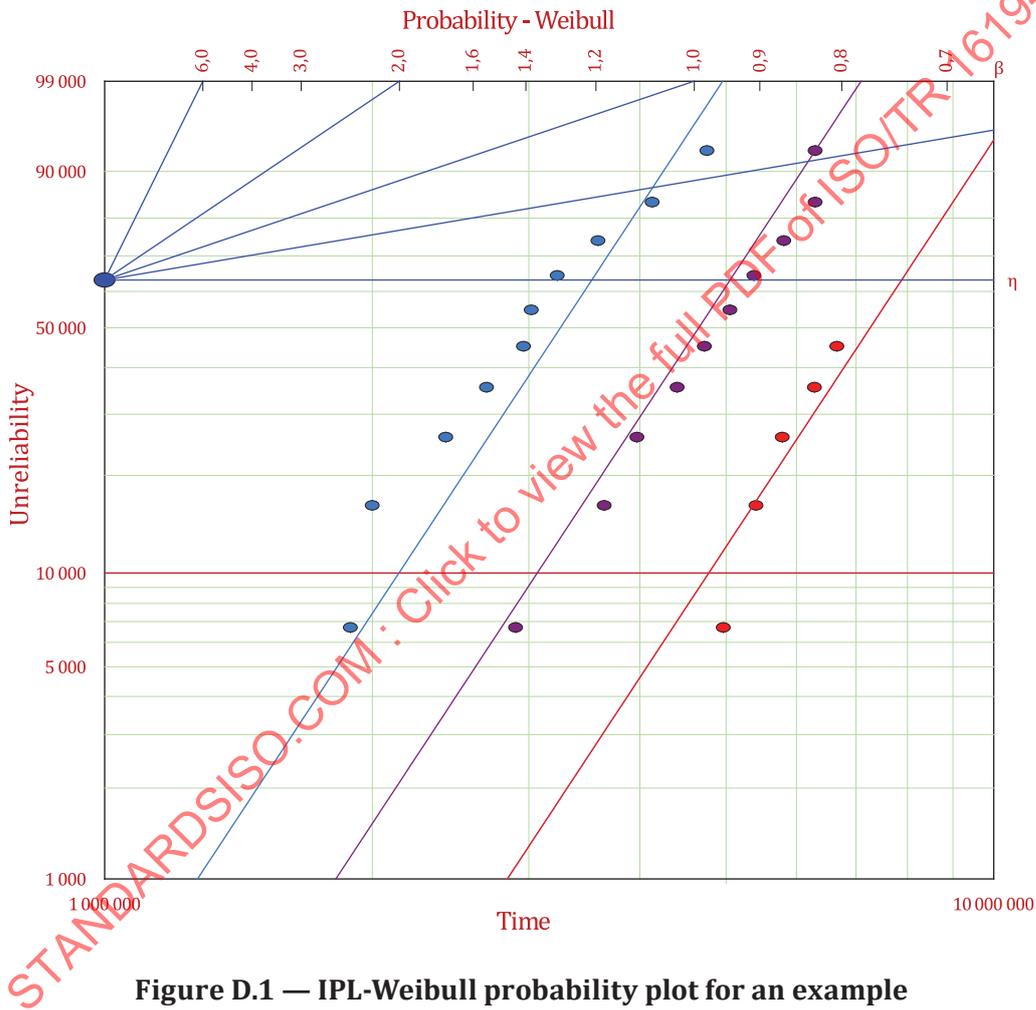
The column labelled “L” is the characteristic life in cycles from the compromised slope test data, and the column labelled “y” uses the absolute pressure. Constants “a” and “n” are determined from the Solver program. The column labelled “L equation” is the calculated life in cycles using [Formula C.1](#). The result of this calculation is the projection of the characteristic life from the accelerated levels of pressure, to the normal pressure of 6,3 bar – which is the value 2,3709x10⁷ cycles. This compares to the tested value of 2,0728x10⁷ cycles as shown in the footnotes of the graphs of [Figures C.1](#) and [C.2](#). The last column describes the accuracy of the projection (85,6%), as well as the accuracy of [Formula C.1](#) with the best fit constants.

Annex D (informative)

Calculation procedures for censored data

Consider an accelerated life test run on a sample of 10 test units at each stress level. Pressure is considered as stress factor. Levels of stress are 630 kPa, 900 kPa, and 1 200 kPa.

In this example, Inverse power law and Weibull parameters are then determined from a maximum likelihood estimation. Results are graphed on a Weibull plot as shown in [Figure D.1](#).



From [Figure D.1](#), it is possible to approximately estimate the values of scale parameter at three stress levels and common shape parameter.

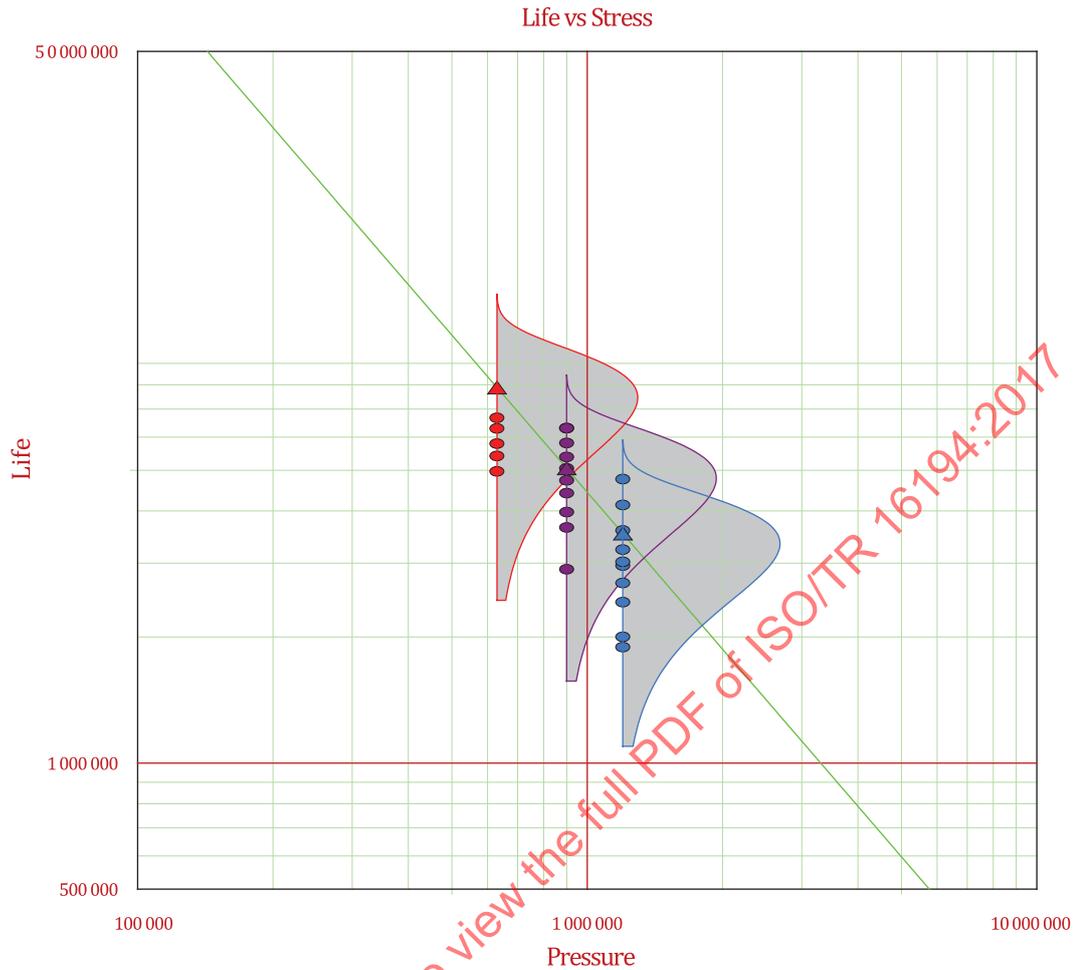


Figure D.2 — Life vs. stress plot for an example

The characteristic life time (η) corresponding to the stress (pressure) level can be obtained using [Figure D.2](#).

Results determined by software for the Inverse power law (IPL)-Weibull model are;

$$K = 4,1452E-8$$

$$n = 1,2453$$

$$\beta = 4,5$$

The IPL-Weibull model can be obtained by putting K , n , and stress level in [Formula \(B.11\)](#). If the stress in the normal use condition is 630 kPa, the scale parameter is estimated at;

$$L = \frac{1}{0,000000041452 \times 630^{1,2453}} = 7\,879 \text{ h}$$

Acceleration factor (AF) of this example can be obtained by putting accelerated stress level (V_A), normal use stress level (V_U), and n in [Formula \(B.13\)](#).

$$AF = \left(\frac{V_A}{V_U} \right)^n = \left(\frac{1\,200}{630} \right)^{1,2453} = 2,23$$

MTTF under normal use condition is;

$$MTTF = \frac{1}{0,000000041452 \times 630^{1,2453}} \times \Gamma \left(\frac{1}{4,5} + 1 \right) = 7\,191 \text{ h}$$

Confidence intervals of MTTF with confidence level of 0,95 are (6 019, 8 592) h.

B_{10} life under normal use condition is;

$$F(B_{10}) = 1 - R(t, V) = 1 - e^{-\left(K \cdot V^n \cdot t \right)^\beta} = 1 - e^{-\left(0,000000041452 \times 630^{1,2453} \cdot t \right)^\beta}$$

$$0,1 = 1 - e^{-\left(0,000000041452 \times 630^{1,2453} \cdot t \right)^\beta}$$

B_{10} life: 4 782 h

Confidence intervals of B_{10} with confidence level of 0,95 are (3 847, 5 943) h.

Annex E (informative)

Examples of using accelerated life testing in industrial applications

E.1 Pneumatic cylinder

Pneumatic cylinders are widely used as key components in various industries, like automation production lines. If a failure occurs, there is significant effect on the whole system. Depending on the type of cylinder, a normal use condition life test could take about 30×10^6 cycles (8 400 h). This could be reduced to $2,5 \times 10^6$ cycles (700 h) through the use of accelerated life testing.

Leakage caused by seal wear is the main failure mode in a pneumatic cylinder; and temperature and pressure are accelerated stress factors that can be applied to a pneumatic cylinder. It is possible to use a Temperature-Nonthermal model for accelerated life testing of a pneumatic cylinder. The accelerated model and the acceleration factor (AF) of a pneumatic cylinder are determined as follows;

$$L(V;U) = \frac{C}{U^n \cdot e^{\frac{B}{V}}} \quad (\text{E.1})$$

$$AF = \left(\frac{U_A}{U_U}\right)^n \cdot e^{B\left(\frac{1}{V_U} - \frac{1}{V_A}\right)} \quad (\text{E.2})$$

U and V represent the pressure stress and temperature stress (in absolute units). Coefficients C , n and B are calculated from the test data. Subscripts A and U refer to the acceleration condition and normal use condition.

Table E.1 — Example of a test plan for pneumatic cylinder

		Temperature		
		S ₃ (80°C)	S ₂ (90°C)	S ₁ (100°C)
Pressure	S ₃ (140 kPa)			③
	S ₂ (160 kPa)			②
	S ₁ (180 kPa)	⑤	④	①

[Table E.1](#) represents the accelerated life testing plan for pneumatic cylinders. Temperature and pressure level values (140 kPa, 160 kPa, 180 kPa; 80°C, 90°C, 100°C) are randomly selected values. Accelerated coefficients C , n and B are calculated using test results in the conditions of ①~⑤. The acceleration factor is calculated from n , B , and stress factors level values in normal use condition, plus the accelerated condition. Life at normal use condition is estimated using the acceleration factor. Commercial software can be helpful for all of these analyses.

E.2 Flexible hose assemblies

Flexible hoses assemblies are piping components that conduct fluid (liquid or gas) under pressure. They are significantly important in reliability.

Stressing in accelerated tests for a flexible hose assembly includes impulse pressure, temperature, and flexing. [Table E.2](#) represents an accelerated life testing plan for flexible hose assemblies. One Impulse

cycle lasts approximately 1 s. The test is conducted until failure or until the test item reaches a specific number of cycles. Typical failure modes are leakage, burst and fitting blow off.

Table E.2 — Example of a test plan for flexible hose assemblies

Procedure	1	2	3	4	5	6
Test standard	ISO 6605 or ISO 6803	ISO 6605 or ISO 6803	ISO 6605 or ISO 6803	ISO 6802	ISO 6802	ISO 6802
Product standard	ISO 1436 Type 1SN	ISO 1436 Type 2SN	ISO 3862 Type R12	ISO 1436 Type 1SN	ISO 1436 Type 2SN	ISO 3862 Type R12
Maximum working pressure ¹	4 to 25 MPa	7 to 41,5 MPa	17,5 to 28 MPa	4 to 25 MPa	7 to 41,5 MPa	17,5 to 28 MPa
Impulse test pressure	125% of max. working pressure	133% of max. working pressure	133% of max. working pressure	125% of max. working pressure	133% of max. working pressure	133% of max. working pressure
Impulse test pressure waveform	Square (See Fig. E.1)					
Flexing	No	No	No	Yes	Yes	Yes
Temperature	(100±3)°C	(100±3)°C	(120±3)°C	(100±3)°C	(100±3)°C	(120±3)°C
Durability (cycles)	1,5x10 ⁵	2,0x10 ⁵	5,0x10 ⁵	1,5x10 ⁵	2,0x10 ⁵	5,0x10 ⁵

¹ Maximum working pressure is dependent on the hose size.

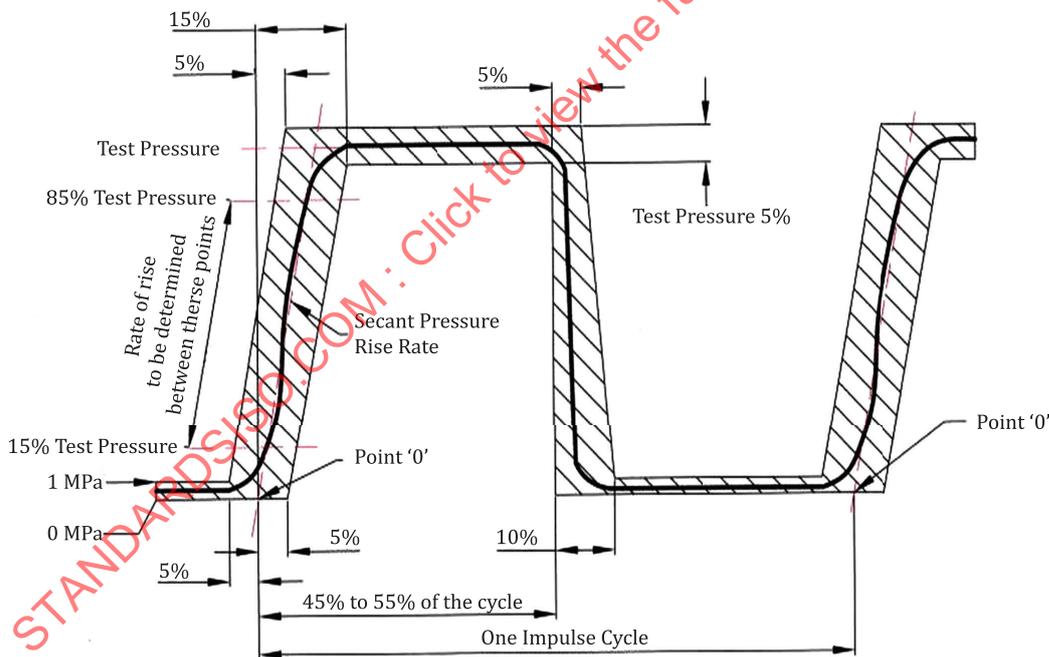


Figure E.1 — Test pressure waveform for flexible hose assemblies

Annex F (informative)

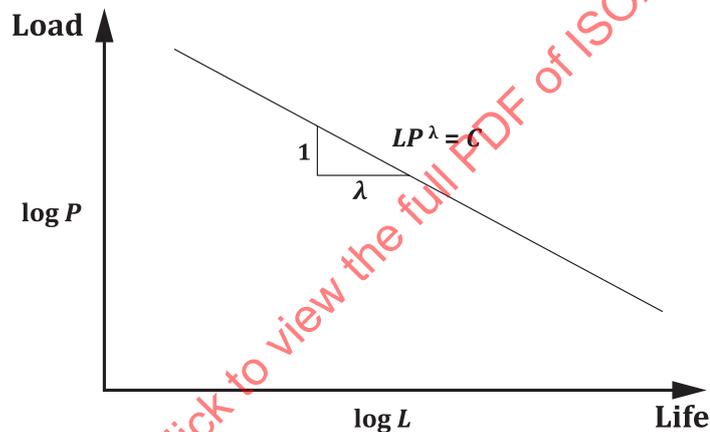
Palmgren-Miner's rule

The accumulation of fatigue due to multiple stress levels or a spectrum of loads might be covered by Miner's rule, or the Palmgren-Miner's rule. This summarizes the impact on the component by the accumulation of all the loads. Eventually, these loads can lead to failure of the component.

Stress-life relationship in accelerated life testing can be explained as follows (see [Figure F.1](#));

$$LP^\lambda = \text{const.} \quad (\text{F.1})$$

where



L is the life of a component

P is the stress (load)

λ is the load factor

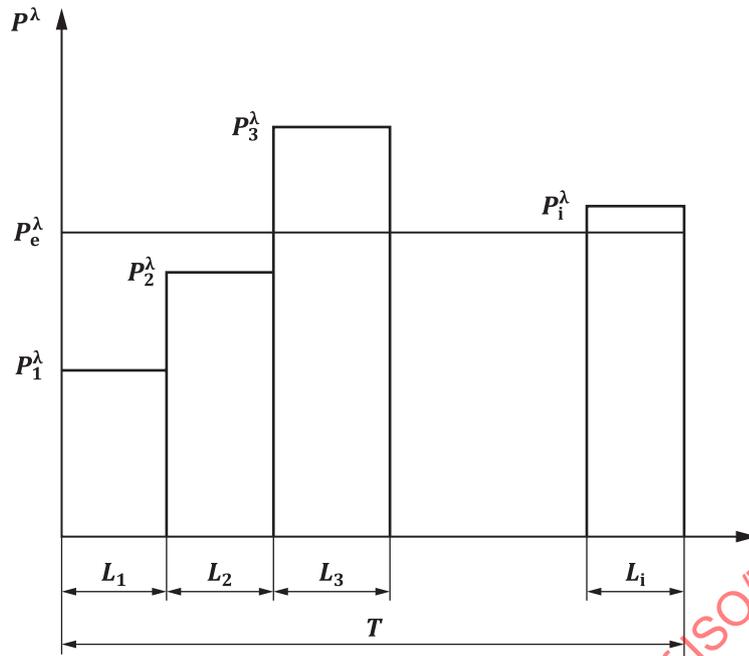
Figure F.1 — Stress-life relationship

In the case where stress is varying for time T , the stress-life relationship can be written as follows (see [Figure F.2](#));

$$P_1^\lambda L_1 + P_2^\lambda L_2 + P_3^\lambda L_3 + \dots + P_i^\lambda L_i = D \quad (\text{F.2})$$

(Palmgren-Miner's rule)

where



- L_i is the operating time for the stress condition i
- P_i is the stress for the stress condition i
- D is the total accumulated damage

Figure F.2 — Example of varying stress

Then equivalent stress (load) can be determined as follows (see [Figure F.2](#));

$$P_e^\lambda (L_1 + L_2 + L_3 + \dots L_i) = P_e^\lambda \cdot T = D \tag{F.3}$$

$$P_e = \left(\frac{P_1^\lambda L_1 + P_2^\lambda L_2 + P_3^\lambda L_3 + \dots P_i^\lambda L_i}{L_1 + L_2 + L_3 + \dots L_i} \right)^{\frac{1}{\lambda}} \tag{F.4}$$

This formula can take a dynamic load situation and turn it into a simple equivalent static load, or serve as a way to accelerate failure modes.

Annex G (informative)

ALT experimental results for pneumatic cylinder

The following slides and their description was a presentation at the ISO pneumatic working group meeting on 22 October 2010.

G.1 General

This is a report on an experimental program for accelerated testing conducted in the laboratory of the Reliability and Assessment Center (RAC) of the Korean Institute of Machinery and Materials (KIMM). The program used over 300 air cylinders from two manufacturers, but tested them in small batches. This is only a status report because the program was still in progress at the time of the presentation.

This report is composed of parts as follows:

1. Introduction: the benefits from accelerated testing and a description of the program;
2. Initial testing to measure the baseline reliability and operational limits;
3. A sampling of the accelerated test results (not all data is shown); and
4. Conclusions to-date;

Consider an automated machine and the consequences of downtime. Planned maintenance programs can be developed and carried out at convenient times if the life probability of its components were known (such as B10 life). But, there are many variations to the duty cycle: loads, orientation, and sizes of the components. Testing all of these variations for each component at the machine's normal conditions takes a long time. Accelerated testing can reduce the test time and provide the reliability information needed. There are equations for projecting test results from accelerated levels to normal levels. But, confidence in the accuracy of this method requires knowledge and experience. This report describes some of the experience being gained from air cylinder testing.

Preliminary testing was done on two groups of cylinders at normal conditions of 23 °C and 6,3 bar to obtain baseline reference data. Results obtained later from accelerated testing are then compared to the baseline data to determine accuracy. In addition, a series of high stress tests were made to find the destructive and yield limits – similar in concept to the points on a stress-strain curve. This helps determine an operating limit (above the catalogue rating) for conducting the accelerated testing.

All phases of this program were conducted in accordance with ISO 19973-3 for cylinders. The high stress tests for determining operating limits used the step stress method as shown in [Figure G.1](#). Stress was applied to a small number of units in progressively increasing steps until failure occurred.

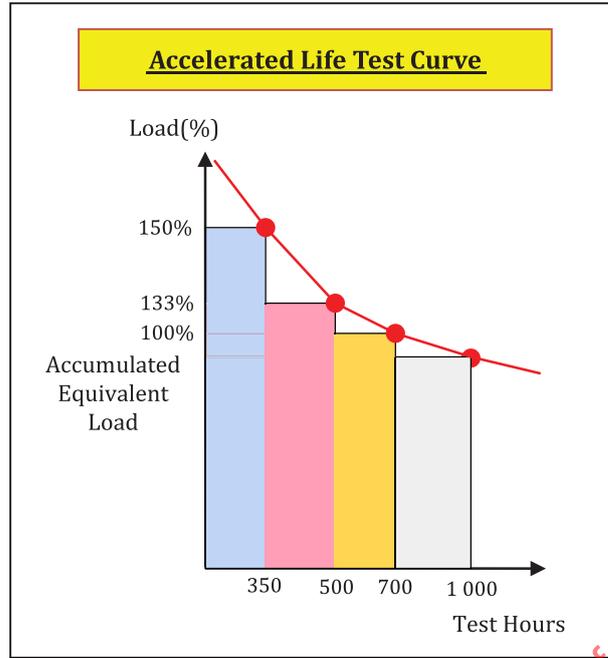


Figure G.1 — Step stress method

G.2 Baseline testing at normal conditions

Figure G.2 shows the rack of test cylinders operating in the KIMM lab, and the mounting arrangement for each cylinder. These were operated at normal conditions, defined for this test as 23 °C temperature and 6,3 bar pressure. Samples of cylinders from two manufacturers were independently purchased. The sample size for the normal condition test for Manufacturer A was 9 cylinders; and 8 cylinders for manufacturer B. This phase of the program required a year of testing to fail enough cylinders to obtain sufficient data for analysis.



Figure G.2 — Test rack of cylinders in KIMM lab

[Figure G.3](#) is a bar graph of time to fail each specimen from company A. The test was terminated after 7 of the 9 specimens failed. The cause of failures and test times are shown for each specimen. The failure lives were all obtained from the first failure observed when a specimen exceeded the threshold, as defined in ISO 19973-3. Examination of the cylinders after testing indicated that wear of the piston seals and wear of the cushion seals were the modes of failure.

Normal condition testing data (23 °C, 6,3 bar) for company A

● Failure Data

Test results after 24 million cycles, 7 specimens out of 9 failed.

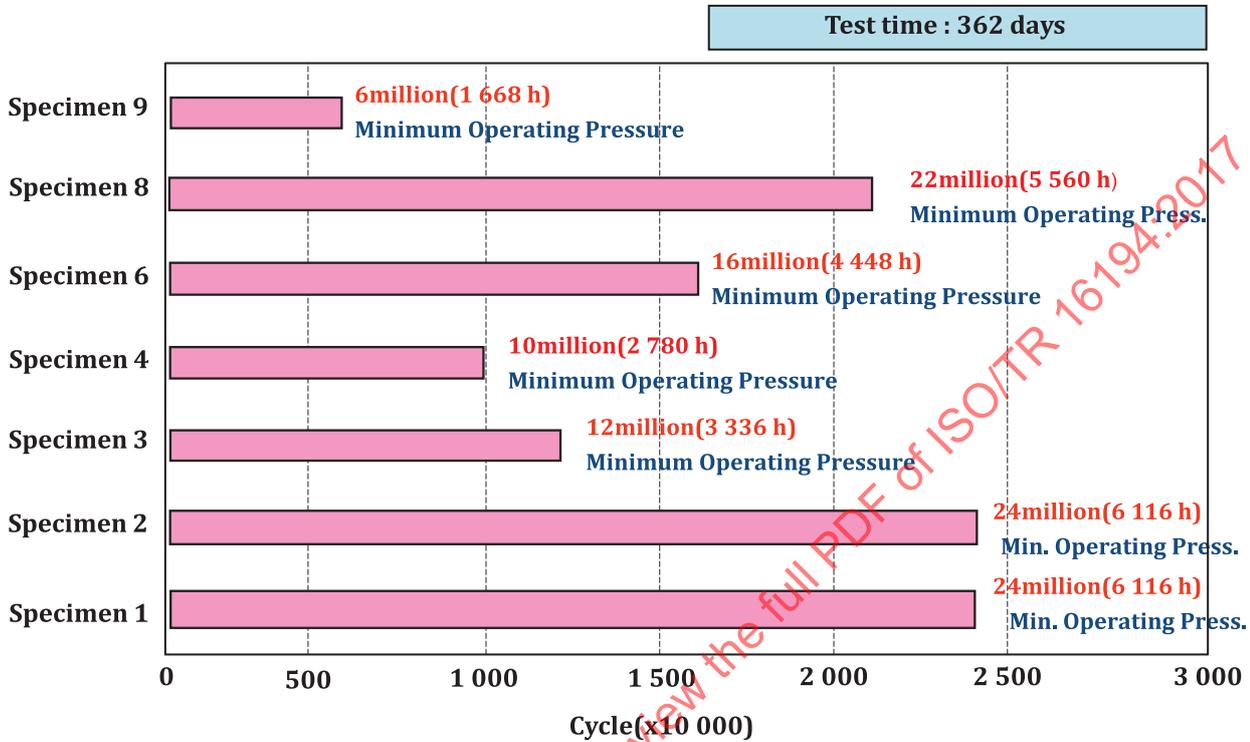


Figure G.3 — Baseline data at normal conditions for company A

Figure G.4 is a Weibull plot of the failure distribution at normal conditions for company A. The failures are shown as a range – the left side is where the last inspection indicated satisfactory operation, and the right side is where the failure was observed. The software draws these symbols and marks (with a dot) the most probable point of failure. The blue line is the median for the best fit of the data to the Weibull equation, and the red curve is the lower 95%, one sided confidence limit. From this, the B₁₀ life at the 95% limit is shown as 3,9162 x 10⁶ cycles.

Analysis result of normal condition testing data for company A

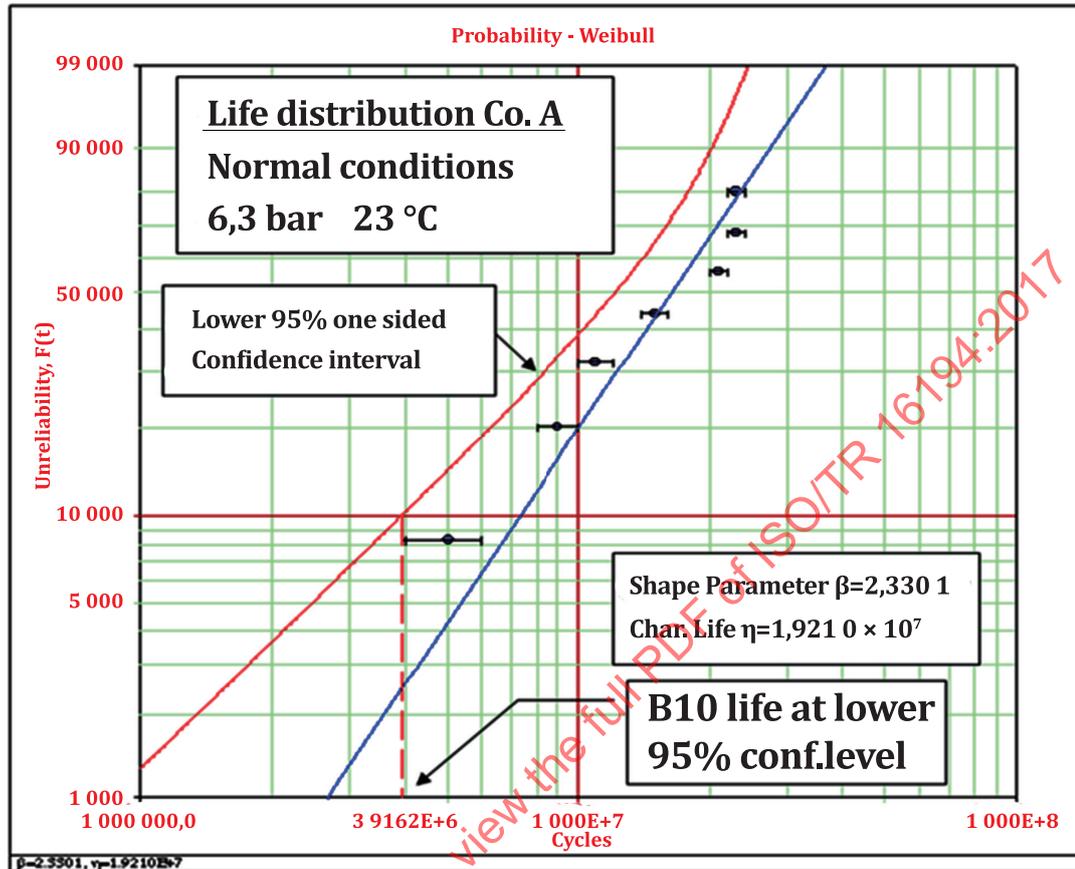


Figure G.4 — Weibull plot of baseline data for company A

Figure G.5 is a bar graph of time to fail for company B. All eight specimens in this sample failed, but had a mixture of failure causes (all as defined in ISO 19973-3). Examination of failures after testing indicated that wear of piston seals, and blockage of the cushion needle valve hole from debris, were the modes of failure.

Normal condition testing data (23 °C, 6,3 bar) for company B

● Failure Data

Test results after 30 million cycles, 8 specimens out of 8 failed.

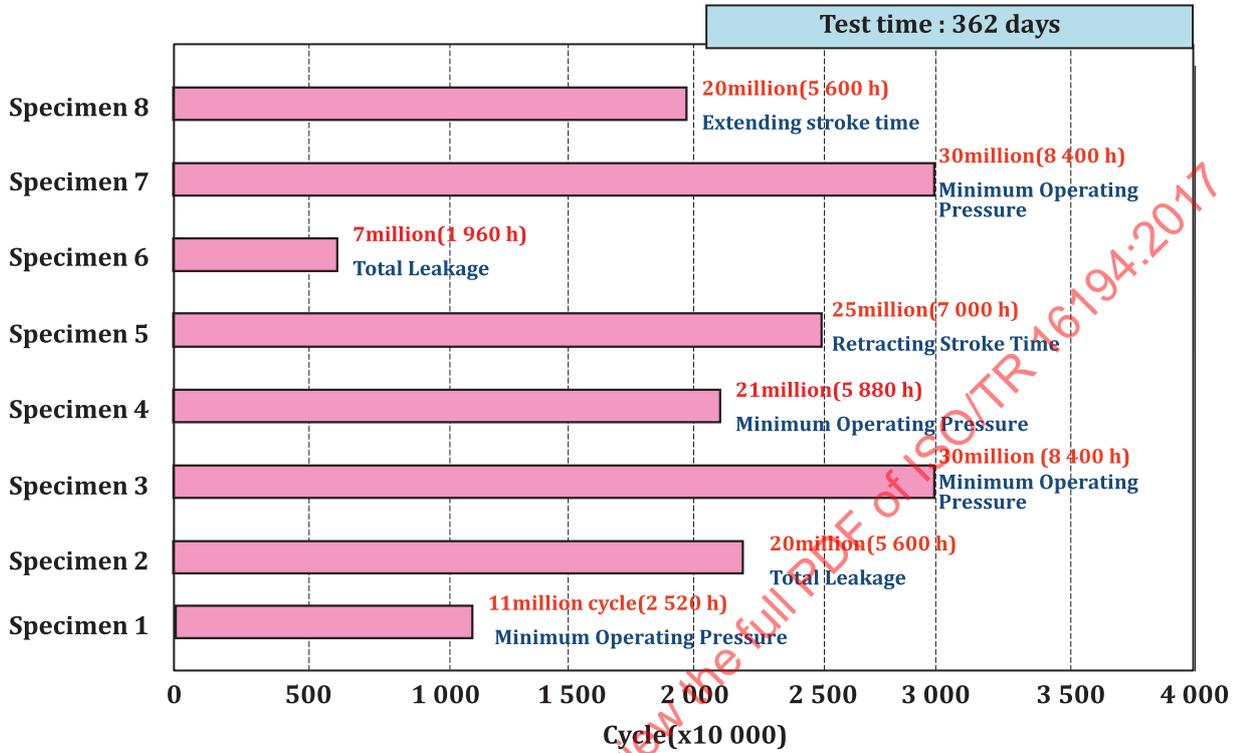


Figure G.5 — Baseline data at normal conditions for company B

Figure G.6 is the Weibull plot of the failure distribution for company B. The B₁₀ life at the 95% lower confidence level is 6,5733 x 10⁶ cycles.

Analysis result of normal condition testing data for company B

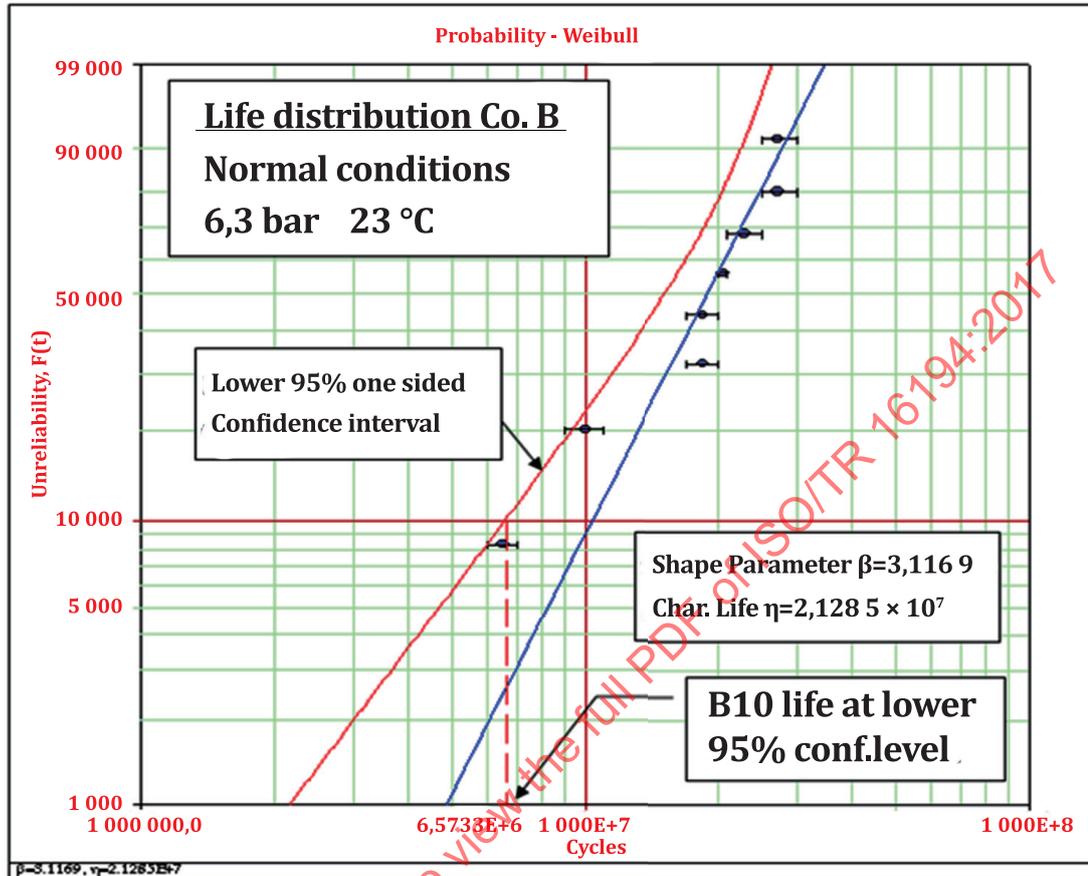


Figure G.6 — Weibull plot of baseline data for company B

G.3 Step stress tests

In the step stress test, two cylinders were used in each of a series of trials. In the first trial, temperature was held constant at 23 °C while the pressure was raised in steps. Beginning at 12 bar, the two cylinders were operated for 2 000 cycles and stopped for performance measurements. Then the pressure was raised to 15 bar and operated for another 2 000 cycles. After another set of performance measurements, the pressure was raised to 18 bar and operated for another 2 000 cycles. This series of steps were continued until the failure criterion was reached.

Table G-1 shows results of the stress step test for company A using pressure as the steps while temperature was held constant at 23 °C. Each step was 2 000 cycles in duration until failure was reached at 34 bar. The columns for failure criteria include data for each of the two cylinder units in the test. At 34 bar, the minimum operating pressure was less than the threshold level, which is 1,2 bar. Thus, the failure was determined to occur at 34 bar operating pressure.

Table G.1 — 2 000 cycle pressure step stress data for company A

Pressure Testing Results for company A (step size: 2000 cycles)

Cycles	Pressure bar	Leakage dm ³ /h (Unit 1/2)	Stroke Time sec		Min. Operating Pressure, bar	
			Extend (Unit 1/2)	Retract (Unit 1/2)	Extend (Unit 1/2)	Retract (Unit 1/2)
2 000	12	0,00/0,00	0,45/0,38	0,49/0,48	0,29/0,21	0,53/0,55
4 000	15	0,00/0,00	0,48/0,41	0,46/0,49	0,21/0,16	0,79/0,54
6 000	18	0,01/0,01	0,38/0,33	0,47/0,49	0,17/0,16	0,55/0,55
8 000	21	0,01/0,02	0,38/0,33	0,45/0,45	0,16/0,18	0,58/0,54
10 000	25	0,02/0,02	0,38/0,35	0,46/0,46	0,12/0,17	0,60/0,53
12 000	30	0,02/0,02	0,35/0,35	0,47/0,49	0,24/0,20	0,92/0,48
14 000	34	0,02/0,02	0,35/0,36	0,47/0,46	0,25/0,11	1,20/1,87

- ✓ Failure mode was extruded cushion seal.
- ✓ Threshold level of minimum operating pressure : < 1,2 bar

The same test was repeated with another two cylinders, but using steps of 10 000 cycles (Table G.2). This demonstrates that failure is sensitive to the length of time at a stress level – the longer the interval, the lower is the destructive stress. For the 10 000 cycle step test, the minimum operating pressure was less than the 1,2 bar threshold level, at 25 bar operating pressure. Thus, it was determined that the failure occurred at 25 bar.

Table G.2 — 10 000 cycle pressure step stress data for company A

Pressure Testing Results for company A (step size: 10000 cycles)

Cycles	Pressure bar	Leakage dm ³ /h (Unit 1/2)	Stroke Time sec		Min. Operating Pressure, bar	
			Extend (Unit 1/2)	Retract (Unit 1/2)	Extend (Unit 1/2)	Retract (Unit 1/2)
10 000	12	0,14/0,07	0,44/0,37	0,53/0,44	0,15/0,21	0,43/0,56
20 000	15	0,19/0,21	0,49/0,47	0,47/0,47	0,13/0,18	0,45/0,49
30 000	18	0,23/0,14	0,38/0,48	0,45/0,47	0,16/0,18	0,47/0,45
40 000	21	0,23/0,14	0,39/0,39	0,45/0,43	0,18/0,23	0,56/0,52
50 000	25	0,37/0,30	0,87/0,89	0,53/0,51	0,25/0,14	2,16/0,55
60 000	30	0,29/0,16	0,36/0,35	0,44/0,44	0,14/0,13	1,61/3,19
70 000	34	0,14/0,12	0,35/0,34	0,40/0,42	0,26/0,19	1,66/2,19

- ✓ Failure mode was extruded cushion seal.
- ✓ Threshold level of minimum operating pressure : < 1,2 bar