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**Calculation of micropitting load capacity  
of cylindrical spur and helical gears —**

Part 1:

**Introduction and basic principles**

*Calcul de la capacité de charge aux micropiqûres des engrenages  
cylindriques à dentures droite et hélicoïdale —*

*Partie 1: Introduction et principes fondamentaux*

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## Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of technical committees is to prepare International Standards. Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

In exceptional circumstances, when a technical committee has collected data of a different kind from that which is normally published as an International Standard ("state of the art", for example), it may decide by a simple majority vote of its participating members to publish a Technical Report. A Technical Report is entirely informative in nature and does not have to be reviewed until the data it provides are considered to be no longer valid or useful.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

ISO/TR 15144-1 was prepared by Technical Committee ISO/TC 60, *Gears*, Subcommittee SC 2, *Gear capacity calculation*.

ISO/TR 15144 consists of the following parts, under the general title *Calculation of micropitting load capacity of cylindrical spur and helical gears*:

— *Part 1: Introduction and basic principles*

## Introduction

This part of ISO/TR 15144 provides principles for the calculation of the micropitting load capacity of cylindrical involute spur and helical gears with external teeth.

The basis for the calculation of the micropitting load capacity of a gear set is the model of the minimum operating specific lubricant film thickness in the contact zone. There are many influence parameters, such as surface topology, contact stress level, and lubricant chemistry. Whilst these parameters are known to affect the performance of micropitting for a gear set, it must be stated that the subject area remains a topic of research and, as such, the science has not yet developed to allow these specific parameters to be included directly in the calculation methods. Furthermore, the correct application of tip and root relief (involute modification) has been found to greatly influence micropitting; the suitable values should therefore be applied. Surface finish is another crucial parameter. At present  $R_a$  is used, but other aspects such as  $R_z$  or skewness have been observed to have significant effects which could be reflected in the finishing process applied.

Although the calculation of specific lubricant film thickness does not provide a direct method for assessing micropitting load capacity, it can serve as an evaluation criterion when applied as part of a suitable comparative procedure based on known gear performance.

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# Calculation of micropitting load capacity of cylindrical spur and helical gears —

## Part 1: Introduction and basic principles

### 1 Scope

This part of ISO/TR 15144 describes a procedure for the calculation of the micropitting load capacity of cylindrical gears with external teeth. It has been developed on the basis of testing and observation of oil-lubricated gear transmissions with modules between 3 mm and 11 mm and pitch line velocities of 8 m/s to 60 m/s. However, the procedure is applicable to any gear pair where suitable reference data is available, providing the criteria specified below are satisfied.

The formulae specified are applicable for driving as well as for driven cylindrical gears with tooth profiles in accordance with the basic rack specified in ISO 53. They are also applicable for teeth conjugate to other basic racks where the virtual contact ratio is less than  $\varepsilon_{\alpha n} = 2,5$ . The results are in good agreement with other methods for normal working pressure angles up to  $25^\circ$  reference helix angles up to  $25^\circ$  and in cases where pitch line velocity is higher than 2 m/s.

This part of ISO/TR 15144 is not applicable for the assessment of types of gear tooth surface damage other than micropitting.

### 2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 53:1998, *Cylindrical gears for general and heavy engineering — Standard basic rack tooth profile*

ISO 1122-1:1998, *Vocabulary of gear terms — Part 1: Definitions related to geometry*

ISO 1328-1:1995, *Cylindrical gears — ISO system of accuracy — Part 1: Definitions and allowable values of deviations relevant to corresponding flanks of gear teeth*

ISO 6336-1:2006, *Calculation of load capacity of spur and helical gears — Part 1: Basic principles, introduction and general influence factors*

ISO 6336-2:2006, *Calculation of load capacity of spur and helical gears — Part 2: Calculation of surface durability (pitting)*

ISO 21771:2007, *Gears — Cylindrical involute gears and gear pairs — Concepts and geometry*

ISO/TR 13989-1:2000, *Calculation of scuffing load capacity of cylindrical, bevel and hypoid gears — Part 1: Flash temperature method*

ISO/TR 13989-2:2000, *Calculation of scuffing load capacity of cylindrical, bevel and hypoid gears — Part 2: Integral temperature method*

### 3 Terms, definitions, symbols and units

#### 3.1 Terms and definitions

For the purposes of this document, the terms and definitions given in ISO 1122-1, ISO 6336-1 and ISO 6336-2 apply.

#### 3.2 Symbols and units

The symbols used in this document are given in Table 1. The units of length metre, millimetre and micrometre are chosen in accordance with common practice. The conversions of the units are already included in the given equations.

Table 1 — Symbols and units

Symbol	Description	Unit
$a$	centre distance	mm
$B_{M1}$	thermal contact coefficient of pinion	$N/(m \cdot s^{0.5} \cdot K)$
$B_{M2}$	thermal contact coefficient of wheel	$N/(m \cdot s^{0.5} \cdot K)$
$b$	face width	mm
$C_{a1}$	tip relief of pinion	$\mu m$
$C_{a2}$	tip relief of wheel	$\mu m$
$C_{eff}$	effective tip relief	$\mu m$
$c_{M1}$	specific heat per unit mass of pinion	$J/(kg \cdot K)$
$c_{M2}$	specific heat per unit mass of wheel	$J/(kg \cdot K)$
$c'$	maximum tooth stiffness per unit face width (single stiffness) of a tooth pair	$N/(mm \cdot \mu m)$
$c_{\gamma\alpha}$	mean value of mesh stiffness per unit face width	$N/(mm \cdot \mu m)$
$d_{a1}$	tip diameter of pinion	mm
$d_{a2}$	tip diameter of wheel	mm
$d_{b1}$	base diameter of pinion	mm
$d_{b2}$	base diameter of wheel	mm
$d_{w1}$	pitch diameter of pinion	mm
$d_{w2}$	pitch diameter of wheel	mm
$d_{Y1}$	Y-circle diameter of pinion	mm
$d_{Y2}$	Y-circle diameter of wheel	mm
$E_r$	reduced modulus of elasticity	$N/mm^2$
$E_1$	modulus of elasticity of pinion	$N/mm^2$
$E_2$	modulus of elasticity of wheel	$N/mm^2$
$F_{bt}$	nominal transverse load in plane of action (base tangent plane)	N
$F_t$	(nominal) transverse tangential load at reference cylinder per mesh	N
$G_M$	material parameter	—
$g_Y$	parameter on the path of contact (distance of point Y from point A)	mm
$g_\alpha$	length of path of contact	mm
$H_v$	load losses factor	—

Table 1 (continued)

Symbol	Description	Unit
$h_Y$	local lubricant film thickness	$\mu\text{m}$
$K_A$	application factor	–
$K_{H\alpha}$	transverse load factor	–
$K_{H\beta}$	face load factor	–
$K_V$	dynamic factor	–
$n_1$	rotation speed of pinion	$\text{min}^{-1}$
$P$	transmitted power	kW
$p_{et}$	transverse base pitch on the path of contact	mm
$p_{dyn,Y}$	local Hertzian contact stress including the load factors K	$\text{N/mm}^2$
$p_{H,Y}$	local nominal Hertzian contact stress	$\text{N/mm}^2$
$R_a$	effective arithmetic mean roughness value	$\mu\text{m}$
$R_{a1}$	arithmetic mean roughness value of pinion	$\mu\text{m}$
$R_{a2}$	arithmetic mean roughness value of wheel	$\mu\text{m}$
$S_{GF,Y}$	local sliding parameter	–
$S_\lambda$	safety factor against micropitting	–
$S_{\lambda,min}$	minimum required safety factor against micropitting	–
$T_1$	nominal torque at the pinion	Nm
$U_Y$	local velocity parameter	–
$u$	gear ratio	–
$v_{g,Y}$	local sliding velocity	m/s
$v_{r1,Y}$	local tangential velocity on pinion	m/s
$v_{r2,Y}$	local tangential velocity on wheel	m/s
$v_{\Sigma,C}$	sum of tangential velocities at pitch point	m/s
$v_{\Sigma,Y}$	sum of tangential velocities at point Y	m/s
$W_W$	material factor	–
$W_Y$	local load parameter	–
$X_{but,Y}$	local buttressing factor	–
$X_{Ca}$	tip relief factor	–
$X_L$	lubricant factor	–
$X_R$	roughness factor	–
$X_S$	lubrication factor	–
$X_Y$	local load sharing factor	–
$Z_E$	elasticity factor	$(\text{N/mm}^2)^{0.5}$
$z_1$	number of teeth of pinion	–
$z_2$	number of teeth of wheel	–
$\alpha_t$	transverse pressure angle	$^\circ$
$\alpha_{wt}$	pressure angle at the pitch cylinder	$^\circ$
$\alpha_{\theta B,Y}$	pressure-viscosity coefficient at local contact temperature	$\text{m}^2/\text{N}$
$\alpha_{\theta M}$	pressure-viscosity coefficient at bulk temperature	$\text{m}^2/\text{N}$
$\alpha_{38}$	pressure-viscosity coefficient at 38 °C	$\text{m}^2/\text{N}$
$\beta_b$	base helix angle	$^\circ$

Table 1 (continued)

Symbol	Description	Unit
$\varepsilon_{\max}$	maximum addendum contact ratio	—
$\varepsilon_{\alpha}$	transverse contact ratio	—
$\varepsilon_{\alpha n}$	virtual contact ratio, transverse contact ratio of a virtual spur gear	—
$\varepsilon_{\beta}$	overlap ratio	—
$\varepsilon_{\gamma}$	total contact ratio	—
$\varepsilon_1$	addendum contact ratio of the pinion	—
$\varepsilon_2$	addendum contact ratio of the wheel	—
$\eta_{\theta B,Y}$	dynamic viscosity at local contact temperature	N·s/m <sup>2</sup>
$\eta_{\theta M}$	dynamic viscosity at bulk temperature	N·s/m <sup>2</sup>
$\eta_{\theta oil}$	dynamic viscosity at oil inlet/sump temperature	N·s/m <sup>2</sup>
$\eta_{38}$	dynamic viscosity at 38 °C	N·s/m <sup>2</sup>
$\theta_{B,Y}$	local contact temperature	°C
$\theta_{fl,Y}$	local flash temperature	°C
$\theta_M$	bulk temperature	°C
$\theta_{oil}$	oil inlet/sump temperature	°C
$\lambda_{GF,min}$	minimum specific lubricant film thickness in the contact area	—
$\lambda_{GF,Y}$	local specific lubricant film thickness	—
$\lambda_{GFP}$	permissible specific lubricant film thickness	—
$\lambda_{GFT}$	limiting specific lubricant film thickness of the test gears	—
$\lambda_{M1}$	specific heat conductivity of pinion	W/(m·K)
$\lambda_{M2}$	specific heat conductivity of wheel	W/(m·K)
$\mu_m$	mean coefficient of friction	—
$\nu_{\theta B,Y}$	kinematic viscosity at local contact temperature	mm <sup>2</sup> /s
$\nu_{\theta M}$	kinematic viscosity at bulk temperature	mm <sup>2</sup> /s
$\nu_1$	Poisson's ratio of pinion	—
$\nu_2$	Poisson's ratio of wheel	—
$\nu_{100}$	kinematic viscosity at 100 °C	mm <sup>2</sup> /s
$\nu_{40}$	kinematic viscosity at 40 °C	mm <sup>2</sup> /s
$\rho_{M1}$	density of pinion	kg/m <sup>3</sup>
$\rho_{M2}$	density of wheel	kg/m <sup>3</sup>
$\rho_{n,C}$	normal radius of relative curvature at pitch diameter	mm
$\rho_{n,Y}$	normal radius of relative curvature at point Y	mm
$\rho_{t,Y}$	transverse radius of relative curvature at point Y	mm
$\rho_{t1,Y}$	transverse radius of curvature of pinion at point Y	mm
$\rho_{t2,Y}$	transverse radius of curvature of wheel at point Y	mm
$\rho_{\theta B,Y}$	density of lubricant at local contact temperature	kg/m <sup>3</sup>
$\rho_{\theta M}$	density of lubricant at bulk temperature	kg/m <sup>3</sup>
$\rho_{15}$	density of lubricant at 15 °C	kg/m <sup>3</sup>

**Subscripts to symbols**

parameter for any contact point Y in the contact area for Method A and on the path of contact for Method B; (all parameters subscript Y have to be calculated with local values)

## 4 Definition of micropitting

Micropitting is a phenomenon that occurs in Hertzian type of rolling and sliding contact that operates in elastohydrodynamic or boundary lubrication regimes. Micropitting is influenced by operating conditions such as load, speed, sliding, temperature, surface topography, specific lubricant film thickness and chemical composition of the lubricant. Micropitting is more commonly observed on materials with a high surface hardness.

Micropitting is the generation of numerous surface cracks. The cracks grow at a shallow angle to the surface forming micropits. The micropits are small relative to the size of the contact zone, typically of the order 10 - 20  $\mu\text{m}$  deep. The micropits can coalesce to produce a continuous fractured surface which appears as a dull, matte surface during unmagnified visual inspection.

Micropitting is the preferred name for this phenomenon, but it has also been referred to as grey staining, grey flecking, frosting and peeling. Illustrations of micropitting can be found in ISO 10825 [8].

Micropitting may arrest. However, if micropitting continues to progress, it may result in reduced gear tooth accuracy, increased dynamic loads and noise. If it does not arrest and continues to propagate it can develop into macropitting and other modes of gear failure.

## 5 Basic formulae

### 5.1 General

The calculation of micropitting load capacity is based on the local specific lubricant film thickness  $\lambda_{GF,Y}$  in the contact area and the permissible specific lubricant film thickness  $\lambda_{GFP}$  [11]. It is assumed that micropitting can occur, when the minimum specific lubricant film thickness  $\lambda_{GF,min}$  is lower than a corresponding critical value  $\lambda_{GFP}$ . Both values  $\lambda_{GF,min}$  and  $\lambda_{GFP}$  shall be calculated separately for pinion and wheel in the contact area. It has to be recognized that the determination of the minimum specific lubricant film thickness and the permissible specific lubricant film thickness have to be based on the operating parameters.

The micropitting load capacity can be determined by comparing the minimum specific lubricant film thickness with the corresponding limiting value derived from gears in service or from specific gear testing. This comparison will be expressed by the safety factor  $S_\lambda$  which shall be equal or higher than a minimum safety factor against micropitting  $S_{\lambda,min}$ .

Micropitting mainly occurs in areas of negative specific sliding. Negative specific sliding is to be found along the path of contact (see Figure 1) between point A and C on the driving gear and between point C and E on the driven gear. Considering the influences of lubricant, surface roughness, geometry of the gears and operating conditions the specific lubricant film thickness  $\lambda_{GF,Y}$  can be calculated for every point in the field of contact.

### 5.2 Safety factor against micropitting $S_\lambda$

To account for the micropitting load capacity the safety factor  $S_\lambda$  according to equation (1) is defined.

$$S_\lambda = \frac{\lambda_{GF,min}}{\lambda_{GFP}} \geq S_{\lambda,min} \quad (1)$$

where

$\lambda_{GF,min} = \min(\lambda_{GF,Y})$  is the minimum specific lubricant film thickness in the contact area;

$\lambda_{GF,Y}$  is the local specific lubricant film thickness (see 5.3);

$\lambda_{GFP}$  is the permissible specific lubricant film thickness (see 5.4);

$S_{\lambda,min}$  is the minimum required safety factor (see 5.5).

The minimum specific lubricant film thickness is determined from all calculated local values of the specific lubricant film thickness  $\lambda_{GF,Y}$  obtained by equation (2).

### 5.3 Local specific lubricant film thickness $\lambda_{GF,Y}$

For the determination of the safety factor  $S_\lambda$  the local lubricant film thickness  $h_Y$  according to Dowson/Higginson [5] in the field of contact has to be known and compared with the effective surface roughness.

$$\lambda_{GF,Y} = \frac{h_Y}{Ra} \quad (2)$$

where

$$Ra = 0,5 \cdot (Ra_1 + Ra_2) \quad (3)$$

$$h_Y = 1600 \cdot \rho_{n,Y} \cdot G_M^{0,6} \cdot U_Y^{0,7} \cdot W_Y^{-0,13} \cdot S_{GF,Y}^{0,22} \quad (4)$$

- $Ra$  is the effective arithmetic mean roughness value;
- $Ra_1$  is the arithmetic mean roughness value of pinion (compare ISO 6336-2);
- $Ra_2$  is the arithmetic mean roughness value of wheel (compare ISO 6336-2);
- $h_Y$  is the local lubricant film thickness;
- $\rho_{n,Y}$  is the normal radius of relative curvature at point Y (see clause 10);
- $G_M$  is the material parameter (see clause 6);
- $U_Y$  is the local velocity parameter (see clause 7);
- $W_Y$  is the local load parameter (see clause 8);
- $S_{GF,Y}$  is the local sliding parameter (see clause 9).

Equation (4) should be calculated in the case of Method B at the seven local points (Y) defined in 5.3 b) using the values for  $\rho_{n,Y}$ ,  $U_Y$ ,  $W_Y$  and  $S_{GF,Y}$  that exists at each point Y. The minimum of the seven  $h_Y$  ( $\lambda_{GF,Y}$ ) values shall be used in equation (1).

An example calculation is presented in Annex B.

#### a) Method A

The local specific lubricant film thickness can be determined in the complete contact area by any appropriate gear computing program. In order to determine the local specific lubricant film thickness, the load distribution, the influence of normal and sliding velocity with changes of meshing phase and the actual service conditions shall be taken into consideration.

#### b) Method B

This method involves the assumption that the determinant local specific lubricant film thickness occurs on the tooth flank in the area of negative sliding. For simplification the calculation of the local specific lubricant film thickness is limited to certain points on the path of contact. For this purpose the lower point A and upper point E on the path of contact, the lower point B and upper point D of single pair tooth contact, the midway point AB between A and B, the midway point DE between D and E as well as the pitch point C are surveyed.

#### 5.4 Permissible specific lubricant film thickness $\lambda_{\text{GFP}}$

For the determination of the permissible specific lubricant film thickness  $\lambda_{\text{GFP}}$  different procedures are applicable.

##### a) Method A

For Method A experimental investigations or service experience relating to micropitting on real gears are used.

Running real gears under conditions where micropitting just occurs the minimum specific lubricant film thickness can be calculated according to 5.3 a). This value is equivalent to the limiting specific lubricant film thickness which is used to calculate the micropitting load capacity.

Such experimental investigations may be performed on gears having the same design as the actual gear pair. In this case the gear manufacturing, gear accuracy, operating conditions, lubricant and operating temperature have to be appropriate for the actual gear box.

The cost required for this method is in general only justifiable for the development of new products as well as for gear boxes where failure would have serious consequences.

Otherwise the permissible specific lubricant film thickness  $\lambda_{\text{GFP}}$  may be derived from consideration of dimensions, service conditions and performance of carefully monitored reference gears operated with the respective lubricant. The more closely the dimensions and service conditions of the actual gears resemble those of the reference gears, the more effective will be the application of such values for the purpose of design ratings or calculation checks.

##### b) Method B

The method adapted is validated by carrying out careful comparative studies of well-documented histories of a number of test gears applicable to the type, quality and manufacture of gearing under consideration. The permissible specific lubricant film thickness  $\lambda_{\text{GFP}}$  is calculated from the critical specific lubricant film thickness  $\lambda_{\text{GFT}}$  which is the result of any standardised test method applicable to evaluate the micropitting load capacity of lubricants or materials by means of defined test gears operated under specified test conditions.  $\lambda_{\text{GFT}}$  is a function of the temperature, oil viscosity, base oil and additive chemistry and can be calculated according to equation (2) in the contact point of the defined test gears where the minimum specific lubricant film thickness is to be found and for the test conditions where the failure limit concerning micropitting in the standardised test procedure has been reached.

The test gears as well as the test conditions (for example the test temperature) have to be appropriate for the real gears in consideration.

Any standardised test can be used to determine the data. Where a specific test procedure is not available or required, a number of internationally available standardised test methods for the evaluation of micropitting performance of gears, lubricants and materials are currently available. Some widely used test procedures are the FVA-FZG-micropitting test [7], Flender micropitting test [12], BGA-DU micropitting test [2] and the micropitting test according to [3]. Annex A provides some generalised test data (for reference only) that have been produced using the test procedure according to FVA-Information Sheet 54/7 [7] where a value for  $\lambda_{\text{GFP}}$  can be calculated for a generalised reference allowable using equation A.1.

#### 5.5 Recommendation for the minimum safety factor against micropitting $S_{\lambda, \text{min}}$

For a given application, adequate micropitting load capacity is demonstrated by the computed value of  $S_{\lambda}$  and being greater than or equal to the value  $S_{\lambda, \text{min}}$ , respectively.

Certain minimum values for the safety factor shall be determined. Recommendations concerning these minimum values are made in the following, but values are not proposed.

An appropriate probability of failure and the safety factor shall be carefully chosen to meet the required reliability at a justifiable cost. If the performance of the gears can be accurately appraised through testing of the actual unit under actual load conditions, a lower safety factor and more economical manufacturing procedures may be permissible:

$$\text{Safety factor} = \frac{\text{Calculated minimum specific film thickness}}{\text{Permissible specific film thickness}}$$

In addition to the general requirements mentioned and the special requirements for specific lubricant film thickness, the safety factor shall be chosen after careful consideration of the following influences.

- reliability of load values used for calculation: If loads or the response of the system to vibration, are estimated rather than measured, a larger safety factor should be used.
- variations in gear geometry and surface texture due to manufacturing tolerances,
- variations in alignment,
- variations in material due to process variations in chemistry, cleanliness and microstructure (material quality and heat treatment),
- variations in lubrication and its maintenance over the service life of the gears.

Depending on the reliability of the assumptions on which the calculations are based (for example load assumptions) and according to the reliability requirements (consequences of occurrence), a corresponding safety factor is to be chosen.

Where gears are produced according to a specification or a request for proposal (quotation), in which the gear supplier is to provide gears or assembled gear drives having specified calculated capacities (ratings) in accordance with this technical report, the value of the safety factor for micropitting is to be agreed upon between the parties.

## 6 Material parameter $G_M$

The material parameter  $G_M$  accounts for the influence of the reduced modulus of elasticity  $E_r$  and the pressure-viscosity coefficient of the lubricant at bulk temperature  $\alpha_{\theta M}$ .

$$G_M = 10^6 \cdot \alpha_{\theta M} \cdot E_r \tag{5}$$

where

$E_r$  is the reduced modulus of elasticity (see 6.1);

$\alpha_{\theta M}$  is the pressure-viscosity coefficient at bulk temperature (see 6.2).

### 6.1 Reduced modulus of elasticity $E_r$

For mating gears of different material and modulus of elasticity  $E_1$  and  $E_2$ , the reduced modulus of elasticity  $E_r$  can be determined by equation (6). For mating gears of the same material  $E = E_1 = E_2$  equation (7) may be used.

$$E_r = 2 \cdot \left( \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2} \right)^{-1} \tag{6}$$

$$E_r = \frac{E}{1-\nu^2} \quad \text{for } E_1 = E_2 = E \text{ and } \nu_1 = \nu_2 = \nu \quad (7)$$

where

$E_1$  is the modulus of elasticity of pinion (for steel:  $E = 206000 \text{ N/mm}^2$ );

$E_2$  is the modulus of elasticity of wheel (for steel:  $E = 206000 \text{ N/mm}^2$ );

$\nu_1$  is the Poisson's ratio of pinion (for steel:  $\nu = 0,3$ );

$\nu_2$  is the Poisson's ratio of wheel (for steel:  $\nu = 0,3$ ).

## 6.2 Pressure-viscosity coefficient at bulk temperature $\alpha_{\theta M}$

If the data for the pressure-viscosity coefficient at bulk temperature  $\alpha_{\theta M}$  for the specific lubricant is not available, it can be approximated by equation (8) (see [9]).

$$\alpha_{\theta M} = \alpha_{38} \cdot \left[ 1 + 516 \cdot \left( \frac{1}{\theta_M + 273} - \frac{1}{311} \right) \right] \quad (8)$$

where

$\alpha_{38}$  is the pressure-viscosity coefficient of the lubricant at  $38 \text{ }^\circ\text{C}$ ;

$\theta_M$  is the bulk temperature (see clause 14).

If no values for  $\alpha_{38}$  are available then the following approximated values [1] can be used.

$$\alpha_{38} = 2,657 \cdot 10^{-8} \cdot \eta_{38}^{0,1348} \quad \text{for mineral oil} \quad (9)$$

$$\alpha_{38} = 1,466 \cdot 10^{-8} \cdot \eta_{38}^{0,0507} \quad \text{for PAO - based synthetic non-VI improved oil} \quad (10)$$

$$\alpha_{38} = 1,392 \cdot 10^{-8} \cdot \eta_{38}^{0,1572} \quad \text{for PAG - based synthetic oil} \quad (11)$$

where

$\eta_{38}$  is the dynamic viscosity of the lubricant at  $38 \text{ }^\circ\text{C}$ .

## 7 Velocity parameter $U_Y$

The velocity parameter  $U_Y$  describes the proportional increase of the specific lubricant film thickness with increasing dynamic viscosity  $\eta_{\theta M}$  of the lubricant at bulk temperature and sum of the tangential velocities  $v_{\Sigma, Y}$ .

$$U_Y = \eta_{\theta M} \cdot \frac{v_{\Sigma, Y}}{2000 \cdot E_r \cdot \rho_{n, Y}} \quad (12)$$

where

$\eta_{\theta M}$  is the dynamic viscosity of the lubricant at bulk temperature (see 7.2);

$v_{\Sigma, Y}$  is the sum of the tangential velocities (see 7.1);

$E_r$  is the reduced modulus of elasticity (see 6.1);

$\rho_{n, Y}$  is the local normal radius of relative curvature (see clause 10).

### 7.1 Sum of tangential velocities $v_{\Sigma,Y}$

The sum of the tangential velocities at a mesh point Y is calculated according to equation (13). The velocity for pinion  $v_{r1,Y}$  and wheel  $v_{r2,Y}$  in a certain contact point Y on the tooth flank depends on the diameter at pinion  $d_{Y1}$  and the diameter at wheel  $d_{Y2}$  of point Y.

$$v_{\Sigma,Y} = v_{r1,Y} + v_{r2,Y} \quad (13)$$

where

$$v_{r1,Y} = 2 \cdot \pi \cdot \frac{n_1}{60} \cdot \frac{d_{w1}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{Y1}^2 - d_{b1}^2}{d_{w1}^2 - d_{b1}^2}} \quad (14)$$

$$v_{r2,Y} = 2 \cdot \pi \cdot \frac{n_1}{u \cdot 60} \cdot \frac{d_{w2}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{Y2}^2 - d_{b2}^2}{d_{w2}^2 - d_{b2}^2}} \quad (15)$$

- $v_{r1,Y}$  is the tangential velocity on pinion (see Figure 1);
- $v_{r2,Y}$  is the tangential velocity on wheel (see Figure 1);
- $d_{b1}$  is the base diameter of pinion;
- $d_{b2}$  is the base diameter of wheel;
- $d_{w1}$  is the pitch diameter of pinion;
- $d_{w2}$  is the pitch diameter of wheel;
- $d_{Y1}$  is the Y-circle diameter of pinion (see Figure 1 and clause 10);
- $d_{Y2}$  is the Y-circle diameter of wheel (see Figure 1 and clause 10);
- $n_1$  is the rotation speed of pinion;
- $u = z_2/z_1$  is the gear ratio;
- $\alpha_{wt}$  is the pressure angle at the pitch cylinder.

### 7.2 Dynamic viscosity at bulk temperature $\eta_{\theta M}$

The dynamic viscosity at bulk temperature  $\eta_{\theta M}$  can be calculated according to equation (16).

$$\eta_{\theta M} = 10^6 \cdot \nu_{\theta M} \cdot \rho_{\theta M} \quad (16)$$

where

- $\nu_{\theta M}$  is the kinematic viscosity of the lubricant at bulk temperature (see 7.2.1);
- $\rho_{\theta M}$  is the density of the lubricant at bulk temperature (see 7.2.2).

#### 7.2.1 Kinematic viscosity at bulk temperature $\nu_{\theta M}$

The kinematic viscosity at bulk temperature  $\nu_{\theta M}$  can be calculated from the kinematic viscosity  $\nu_{40}$  at 40 °C and the kinematic viscosity  $\nu_{100}$  at 100 °C on the basis of equation (17). Extrapolation for temperature higher than 140 °C should be confirmed by measurement.

$$\log[\log(\nu_{\theta_M} + 0,7)] = A \cdot \log(\theta_M + 273) + B \quad (17)$$

where

$$A = \frac{\log[\log(\nu_{40} + 0,7)/\log(\nu_{100} + 0,7)]}{\log(313/373)} \quad (18)$$

$$B = \log[\log(\nu_{40} + 0,7)] - A \cdot \log(313) \quad (19)$$

$\theta_M$  is the bulk temperature (see clause 14);

$\nu_{40}$  is the kinematic viscosity of the lubricant at 40 °C;

$\nu_{100}$  is the kinematic viscosity of the lubricant at 100 °C.

### 7.2.2 Density of the lubricant at bulk temperature $\rho_{\theta_M}$

If the density of the lubricant at bulk temperature  $\rho_{\theta_M}$  is not available, it can be approximated based on the density of the lubricant at 15 °C according to equation (20).

$$\rho_{\theta_M} = \rho_{15} \cdot \left[ 1 - 0,7 \cdot \frac{(\theta_M + 273) - 289}{\rho_{15}} \right] \quad (20)$$

where

$\rho_{15}$  is the density of the lubricant at 15 °C according to the lubricant data sheet;

$\theta_M$  is the bulk temperature (see clause 14).

If no data for  $\rho_{15}$  is available then equation (21) may be used for approximation of mineral oils.

$$\rho_{15} = 43,37 \cdot \log \nu_{40} + 805,5 \quad (21)$$

$\nu_{40}$  is the kinematic viscosity of the lubricant at 40 °C.

## 8 Load parameter $W_Y$

The load parameter  $W_Y$  can be determined using the local Hertzian contact stress  $p_{\text{dyn},Y}$  and the reduced modulus of elasticity  $E_r$ .

$$W_Y = \frac{2 \cdot \pi \cdot p_{\text{dyn},Y}^2}{E_r^2} \quad (22)$$

where

$\pi_{\text{dyn},Y}$  is the local Hertzian contact stress according to Method A (see 8.1) or according to Method B (see 8.2);

$E_r$  is the reduced modulus of elasticity (see 6.1).

### 8.1 Local Hertzian contact stress $p_{\text{dyn},Y,A}$ according to Method A

The local Hertzian contact stress  $p_{\text{dyn},Y,A}$  according to Method A should be determined by means of a 3D mesh contact and load distribution analysis procedure. The local nominal Hertzian contact stress determined from the elastic mesh contact model  $p_{H,Y,A}$  is applied to equation (23) to obtain the local Hertzian contact stress  $p_{\text{dyn},Y,A}$ .

$$p_{\text{dyn},Y,A} = p_{H,Y,A} \cdot \sqrt{K_A \cdot K_v} \quad (23)$$

where

$p_{H,Y,A}$  is the local nominal Hertzian contact stress, calculated with a 3D load distribution program;

$K_A$  is the application factor (according to ISO 6336-1);

$K_v$  is the dynamic factor (according to ISO 6336-1).

NOTE Where either  $K_A$  or  $K_v$  influences are already considered in the 3D elastic mesh contact model either or both  $K_A$  and  $K_v$  should be set as 1,0 in equation (23).

### 8.2 Local Hertzian contact stress $p_{\text{dyn},Y,B}$ according to Method B

The local Hertzian contact stress  $p_{\text{dyn},Y,B}$  according to Method B is calculated according to equation (24). The required nominal Hertzian contact stress  $p_{H,Y,B}$  is obtained by equation (25), see 8.2.1. The total load in the case of drive trains with multiple transmission paths or planetary gear systems is not quite evenly distributed over the individual meshes. This is to be taken into consideration by inserting a distribution factor  $K_\gamma$  to follow  $K_A$  in equation (24), to adjust the average load per mesh as necessary.

$$p_{\text{dyn},Y,B} = p_{H,Y,B} \cdot \sqrt{K_A \cdot K_v \cdot K_{H\alpha} \cdot K_{H\beta}} \quad (24)$$

where

$p_{H,Y,B}$  is the local nominal Hertzian contact stress (see 8.2.1);

$K_A$  is the application factor (according to ISO 6336-1);

$K_v$  is the dynamic factor (according to ISO 6336-1);

$K_{H\alpha}$  is the transverse load factor (according to ISO 6336-1). Profile modifications are considered in the factor  $X_\gamma$ , see clause 11.

$K_{H\beta}$  is the face load factor (according to ISO 6336-1). Lead modifications are considered in this factor.

NOTE Gears with a total contact ratio  $\varepsilon_t > 2$  can only be calculated according to Method A.

#### 8.2.1 Nominal Hertzian contact stress $p_{H,Y,B}$

The nominal Hertzian contact stress  $p_{H,Y,B}$  is used to determine the local Hertzian contact stress  $p_{\text{dyn},Y,B}$  (see 8.1). To take the influence of different profile modifications into account the load sharing factor  $X_\gamma$  is introduced. For the calculation of the local nominal Hertzian contact stress the local nominal radius of relative curvature is used.

$$p_{H,Y,B} = Z_E \cdot \sqrt{\frac{F_t \cdot X_\gamma}{b \cdot \rho_{n,Y} \cdot \cos \alpha_t \cdot \cos \beta_b}} \quad (25)$$

where

$$Z_E = \sqrt{\frac{E_r}{2\pi}} \quad (26)$$

- $Z_E$  is the elasticity factor (according to ISO 6336-2);
- $b$  is the face width;
- $F_t$  is the transverse tangential load at reference cylinder;
- $X_Y$  is the load sharing factor (see clause 11);
- $E_r$  is the reduced modulus of elasticity (see 6.1);
- $\alpha_t$  is the transverse pressure angle;
- $\beta_b$  is the base helix angle;
- $\rho_{n,Y}$  is the local normal radius of relative curvature (see clause 10).

## 9 Sliding parameter $S_{GF,Y}$

The sliding parameter  $S_{GF,Y}$  accounts for the influence of local sliding on the local temperature. This temperature influences both the local pressure-viscosity coefficient and the local dynamic viscosity and hence the local lubricant film thickness [6]. The indices “ $\theta_{B,Y}$ ” for local contact temperature and “ $\theta_M$ ” for bulk temperature are used. The local contact temperature  $\theta_{B,Y}$  is the sum of the local flash  $\theta_{h,Y}$  and the bulk temperature  $\theta_M$ .

$$S_{GF,Y} = \frac{\alpha_{\theta_{B,Y}} \cdot \eta_{\theta_{B,Y}}}{\alpha_{\theta_M} \cdot \eta_{\theta_M}} \quad (27)$$

where

- $\alpha_{\theta_{B,Y}}$  is the pressure-viscosity coefficient at local contact temperature (see 9.1);
- $\eta_{\theta_{B,Y}}$  is the dynamic viscosity at local contact temperature (see 9.2);
- $\alpha_{\theta_M}$  is the pressure-viscosity coefficient at bulk temperature (see 6.2);
- $\eta_{\theta_M}$  is the dynamic viscosity at bulk temperature (see 7.2).

### 9.1 Pressure-viscosity coefficient at local contact temperature $\alpha_{\theta_{B,Y}}$

If the data for the pressure-viscosity coefficient at local contact temperature  $\alpha_{\theta_{B,Y}}$  for the specific lubricant is not available, it can be approximated by equation (28) (see [9]).

$$\alpha_{\theta_{B,Y}} = \alpha_{38} \cdot \left[ 1 + 516 \cdot \left( \frac{1}{\theta_{B,Y} + 273} - \frac{1}{311} \right) \right] \quad (28)$$

where

- $\alpha_{38}$  is the pressure-viscosity coefficient of the lubricant at 38 °C (see also 6.2);
- $\theta_{B,Y}$  is the local contact temperature (see clause 12).

## 9.2 Dynamic viscosity at local contact temperature $\eta_{\theta_{B,Y}}$

The dynamic viscosity at local contact temperature  $\eta_{\theta_{B,Y}}$  is determined by equation (29).

$$\eta_{\theta_{B,Y}} = 10^{-6} \cdot \nu_{\theta_{B,Y}} \cdot \rho_{\theta_{B,Y}} \quad (29)$$

where

$\nu_{\theta_{B,Y}}$  is the kinematic viscosity at local contact temperature (see 9.2.1);

$\rho_{\theta_{B,Y}}$  is the density of the lubricant at local contact temperature (see 9.2.2).

### 9.2.1 Kinematic viscosity at local contact temperature $\nu_{\theta_{B,Y}}$

The kinematic viscosity at local contact temperature  $\nu_{\theta_{B,Y}}$  can be calculated from the kinematic viscosity  $\nu_{40}$  at 40 °C and the kinematic viscosity  $\nu_{100}$  at 100 °C on the basis of equation (30). Extrapolation for temperature higher than 140 °C should be confirmed by measurement.

$$\log[\log(\nu_{\theta_{B,Y}} + 0,7)] = A \cdot \log(\theta_{B,Y} + 273) + B \quad (30)$$

where

$$A = \frac{\log[\log(\nu_{40} + 0,7) / \log(\nu_{100} + 0,7)]}{\log(313 / 373)} \quad (31)$$

$$B = \log[\log(\nu_{40} + 0,7)] - A \cdot \log(313) \quad (32)$$

$\theta_{B,Y}$  is the local contact temperature (see clause 12);

$\nu_{40}$  is the kinematic viscosity of the lubricant at 40 °C;

$\nu_{100}$  is the kinematic viscosity of the lubricant at 100 °C.

### 9.2.2 Density of the lubricant at local contact temperature $\rho_{\theta_{B,Y}}$

If the density of the lubricant at local contact temperature  $\rho_{\theta_{B,Y}}$  is not available, it can be approximated based on the density of the lubricant at 15 °C according to equation (33).

$$\rho_{\theta_{B,Y}} = \rho_{15} \cdot \left[ 1 - 0,7 \cdot \frac{(\theta_{B,Y} + 273) - 289}{\rho_{15}} \right] \quad (33)$$

where

$\rho_{15}$  is the density of the lubricant at 15 °C according to the lubricant data sheet (see also 7.2.2);

$\theta_{B,Y}$  is the local contact temperature (see clause 12).

## 10 Definition of contact point Y on the path of contact

Contact point Y is located between the SAP (contact point A) and EAP (contact point E) on the path of contact according to Figure 1. It describes the actual contact point between pinion and wheel in a certain meshing position  $g_Y$ .

According to 5.3, Method B the calculation has to be done for the following contact points:

Y =

- **A**  $g_Y = g_A = 0$  mm the lower point on the path of contact (34)
- **AB**  $g_Y = g_{AB} = (g_\alpha - p_{et}) / 2$  the midway point between A and B (35)
- **B**  $g_Y = g_B = g_\alpha - p_{et}$  the lower point of single pair tooth contact (36)
- **C**  $g_Y = g_C = \frac{d_{b1}}{2} \cdot \tan \alpha_{wt} - \sqrt{\frac{d_{a1}^2}{4} - \frac{d_{b1}^2}{4}} + g_\alpha$  the pitch point (37)
- **D**  $g_Y = g_D = p_{et}$  the upper point of single pair tooth contact (38)
- **DE**  $g_Y = g_{DE} = (g_\alpha - p_{et}) / 2 + p_{et}$  the midway point between D and E (39)
- **E**  $g_Y = g_E = g_\alpha$  the upper point on the path of contact (40)

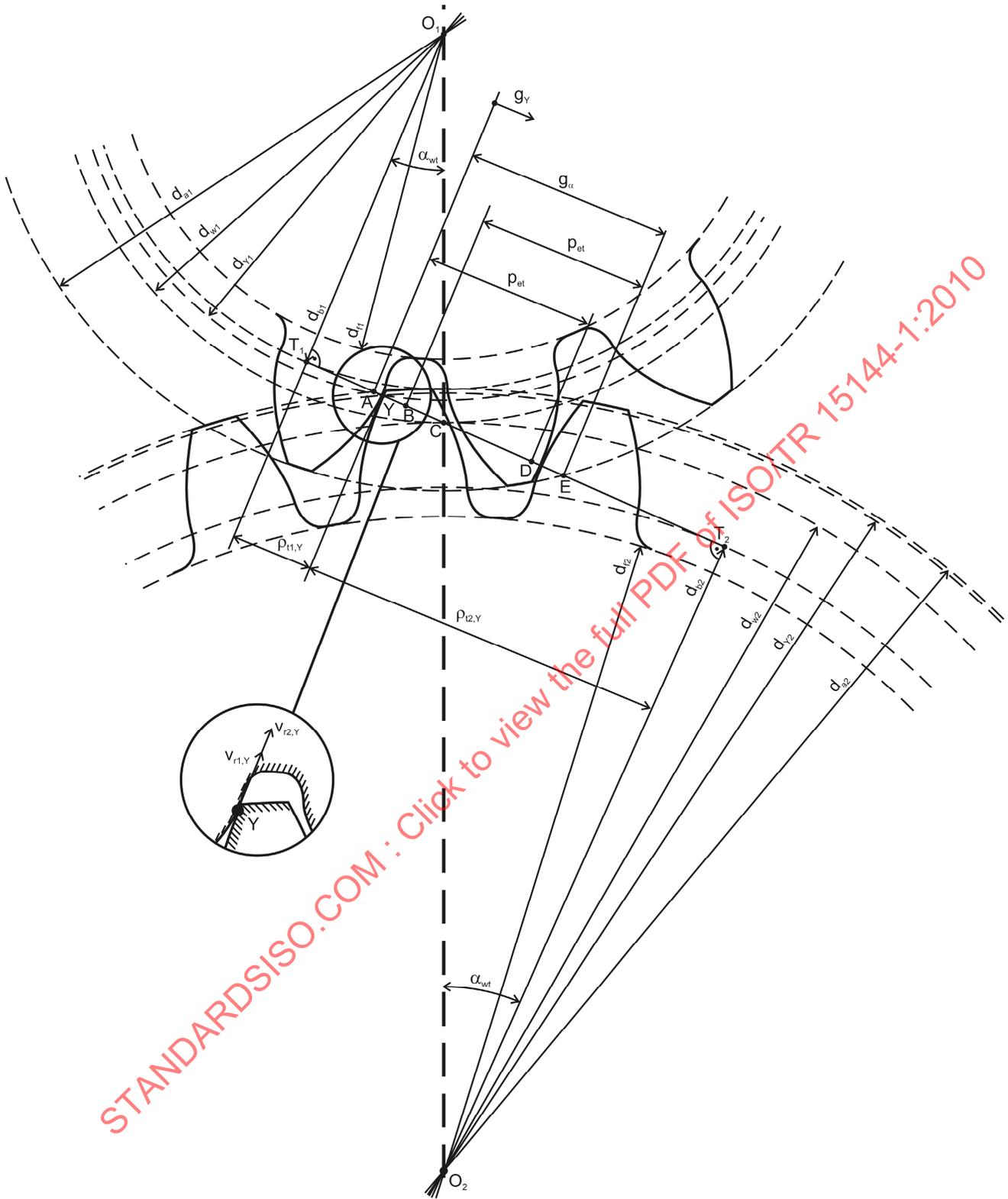


Figure 1 — Definition of contact point Y on the line of action

The Y-circle diameter of pinion  $d_{Y1}$  and wheel  $d_{Y2}$  are dependent on the location of contact point Y on the path of contact  $g_Y$  and can be calculated according to equation (41) and equation (42).

$$d_{Y1} = 2 \cdot \sqrt{\frac{d_{b1}^2}{4} + \left( \sqrt{\frac{d_{a1}^2}{4} - \frac{d_{b1}^2}{4}} - g_\alpha + g_Y \right)^2} \quad (41)$$

$$d_{Y2} = 2 \cdot \sqrt{\frac{d_{b2}^2}{4} + \left( \sqrt{\frac{d_{a2}^2}{4} - \frac{d_{b2}^2}{4}} - g_Y \right)^2} \quad (42)$$

where

$d_{a1}$  is the tip diameter of pinion (see Figure 1);

$d_{a2}$  is the tip diameter of wheel (see Figure 1);

$d_{b1}$  is the base diameter of pinion (see Figure 1);

$d_{b2}$  is the base diameter of wheel (see Figure 1);

$g_Y$  is the parameter on the path of contact (see Figure 1);

$g_\alpha$  is the length of path of contact (see Figure 1).

The transverse radius of relative curvature  $\rho_{t,Y}$  can be determined according to equation (43).

$$\rho_{t,Y} = \frac{\rho_{t1,Y} \cdot \rho_{t2,Y}}{\rho_{t1,Y} + \rho_{t2,Y}} \quad (43)$$

where

$$\rho_{t1,2,Y} = \sqrt{\frac{d_{Y1,2}^2 - d_{b1,2}^2}{4}} \quad (44)$$

$\rho_{t1,2,Y}$  is the transverse radius of curvature of pinion/ wheel at point Y (see Figure 1);

$d_{b1,2}$  is the base diameter of pinion/ wheel (see Figure 1);

$d_{Y1,2}$  is the Y-circle diameter of pinion/ wheel (see above and Figure 1).

The normal radius of relative curvature  $\rho_{n,Y}$  can be calculated according to equation (45).

$$\rho_{n,Y} = \frac{\rho_{t,Y}}{\cos \beta_b} \quad (45)$$

where

$\rho_{t,Y}$  is the transverse relative radius of curvature (see above);

$\beta_b$  is the base helix angle.

### 11 Load sharing factor $X_Y$

The load sharing factor  $X_Y$  accounts for the load sharing of succeeding pairs of meshing teeth. The load sharing factor is presented as a function of the linear parameter  $g_Y$  on the path of contact [4].

Due to inaccuracies a preceding pair of meshing teeth may cause an instantaneous increase or decrease of the theoretical load sharing factor, independent of the instantaneous increase or decrease caused by inaccuracies of a succeeding pair of meshing teeth at a later time. The value of  $X_Y$  does not exceed 1,0 (for cylindrical gears), which means full transverse single tooth contact. The region of transverse single tooth contact may be extended by an irregularly varying location of a dynamic load.

The load sharing factor  $X_Y$  depends on the type of gear transmission and on the profile modification. In case of buttressing of helical teeth (no profile modification) the load sharing factor is combined with a buttressing factor  $X_{but,Y}$  [4].

#### 11.1 Spur gears with unmodified profiles

The load sharing factor for a spur gear with unmodified profile is conventionally supposed to have a discontinuous trapezoidal shape; see Figure 2. However, due to manufacturing inaccuracies, in each path of double contact the load sharing factor will increase for protruding flanks and decrease for other flanks. The representative load sharing factor is an envelope of possible curves; see Figure 3.

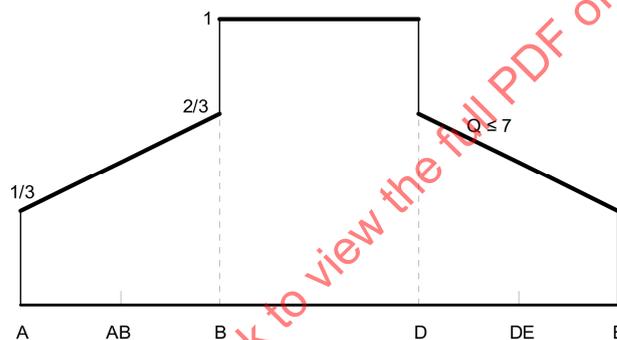


Figure 2 — Load sharing factor for cylindrical spur gears with unmodified profiles and quality grade  $\leq 7$

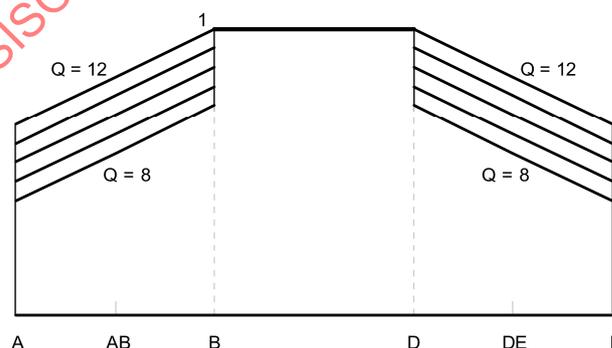


Figure 3 — Load sharing factor for cylindrical spur gears with unmodified profiles and quality grade  $\geq 8$

$$X_Y = \frac{Q-2}{15} + \frac{1}{3} \cdot \frac{g_Y}{g_B} \quad \text{for } g_A \leq g_Y < g_B \quad (46)$$

$$X_Y = 1,0 \quad \text{for } g_B \leq g_Y \leq g_D \quad (47)$$

$$X_Y = \frac{Q-2}{15} + \frac{1}{3} \cdot \frac{g_a - g_Y}{g_a - g_D} \quad \text{for } g_D < g_Y \leq g_E \quad (48)$$

where

Q = 7 for quality grade  $\leq 7$ ;

Q = equals quality grade for grade  $\geq 8$ .

## 11.2 Spur gears with profile modification

See Figure 4, Figure 5 and Figure 6.

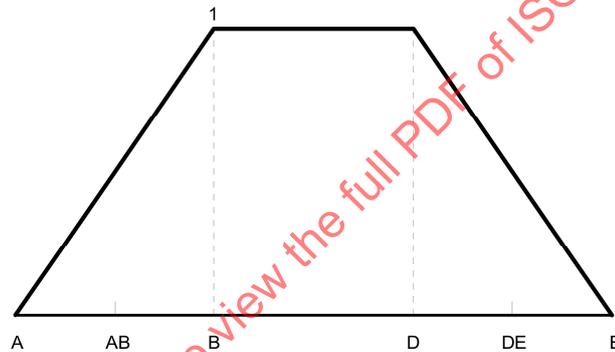


Figure 4 — Load sharing factor for cylindrical spur gears with optimum profile modification

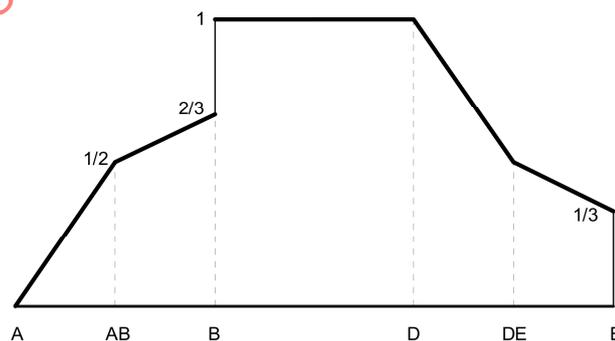
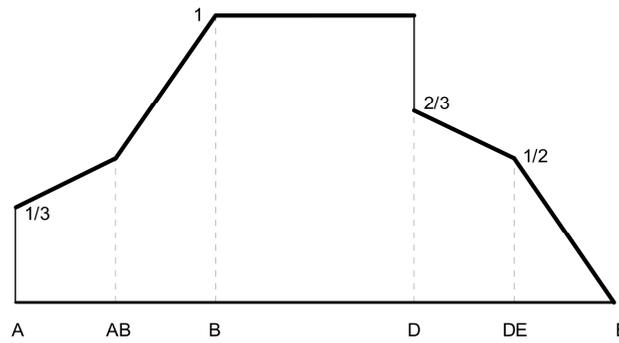


Figure 5 — Load sharing factor for cylindrical spur gears with optimum profile modification on the addendum of the driven gear and/or the dedendum of the driving gear



**Figure 6 — Load sharing factor for cylindrical spur gears with optimum profile modification on the addendum of the driving gear and/or the dedendum of the driven gear**

Linear interpolation between the values is possible.

$$X_Y = \frac{1}{3} + \frac{1}{3} \cdot \frac{g_Y}{g_B} \quad \text{for } g_A \leq g_Y \leq g_{AB} \quad \text{if } C_{a2} = 0 \mu\text{m} \quad (49)$$

$$X_Y = \frac{g_Y}{g_B} \quad \text{for } g_A \leq g_Y \leq g_{AB} \quad \text{if } C_{a2} = C_{\text{eff}} \text{ (see 14.3)} \quad (50)$$

$$X_Y = \frac{1}{3} + \frac{1}{3} \cdot \frac{g_Y}{g_B} \quad \text{for } g_{AB} \leq g_Y \leq g_B \quad \text{if } C_{a1} = 0 \mu\text{m} \quad (51)$$

$$X_Y = \frac{g_Y}{g_B} \quad \text{for } g_{AB} \leq g_Y \leq g_B \quad \text{if } C_{a1} = C_{\text{eff}} \quad (52)$$

$$X_Y = 1,0 \quad \text{for } g_B \leq g_Y \leq g_D \quad (53)$$

$$X_Y = \frac{1}{3} + \frac{1}{3} \cdot \frac{g_\alpha - g_Y}{g_\alpha - g_D} \quad \text{for } g_D \leq g_Y \leq g_{DE} \quad \text{if } C_{a2} = 0 \mu\text{m} \quad (54)$$

$$X_Y = \frac{g_\alpha - g_Y}{g_\alpha - g_D} \quad \text{for } g_D \leq g_Y \leq g_{DE} \quad \text{if } C_{a2} = C_{\text{eff}} \quad (55)$$

$$X_Y = \frac{1}{3} + \frac{1}{3} \cdot \frac{g_\alpha - g_Y}{g_\alpha - g_D} \quad \text{for } g_{DE} \leq g_Y \leq g_E \quad \text{if } C_{a1} = 0 \mu\text{m} \quad (56)$$

$$X_Y = \frac{g_\alpha - g_Y}{g_\alpha - g_D} \quad \text{for } g_{DE} \leq g_Y \leq g_E \quad \text{if } C_{a1} = C_{\text{eff}} \quad (57)$$

### 11.3 Buttressing factor $X_{\text{but},Y}$

Helical gears may have a buttressing effect near the end points A and E of the path of contact, due to the oblique contact lines. This applies to cylindrical helical gears with no profile modification.



Figure 7 — Buttringing factor,  $X_{but,Y}$

The buttringing is expressed by means of a factor  $X_{but,Y}$ ; see Figure 7, marked by the following values.

$$g_{AU} - g_A = g_E - g_{EU} = 0,2 \text{ mm} \cdot \sin \beta_b \quad (58)$$

with

$$g_A = 0 \text{ mm} ;$$

$$g_E = g_\alpha \quad (\text{see Figure 1}).$$

$$X_{but,A} = X_{but,E} = 1,3 \quad \text{if } \varepsilon_\beta \geq 1,0 \quad (59)$$

$$X_{but,A} = X_{but,E} = 1 + 0,3 \cdot \varepsilon_\beta \quad \text{if } \varepsilon_\beta < 1,0 \quad (60)$$

$$X_{but,AU} = X_{but,EU} = 1,0 \quad (61)$$

$$X_{but,Y} = X_{but,A} - \frac{g_Y}{0,2 \text{ mm} \cdot \sin \beta_b} \cdot (X_{but,A} - 1) \quad \text{for } g_A \leq g_Y < g_{AU} \quad (62)$$

$$X_{but,Y} = 1,0 \quad \text{for } g_{AU} \leq g_Y \leq g_{EU} \quad (63)$$

$$X_{but,Y} = X_{but,E} - \frac{g_\alpha - g_Y}{0,2 \text{ mm} \cdot \sin \beta_b} \cdot (X_{but,E} - 1) \quad \text{for } g_{EU} < g_Y \leq g_E \quad (64)$$

where

$\varepsilon_\beta$  is the overlap ratio.

#### 11.4 Helical gears with $\varepsilon_\beta < 1$ and unmodified profiles

Helical gears with a contact ratio  $\varepsilon_\alpha \geq 1$  and overlap ratio  $\varepsilon_\beta < 1$ , have still poor single contact of tooth pairs. Hence, they can be treated similar to spur gears, considering the geometry in the transverse plane, as well as the buttringing effect. See Figure 8.

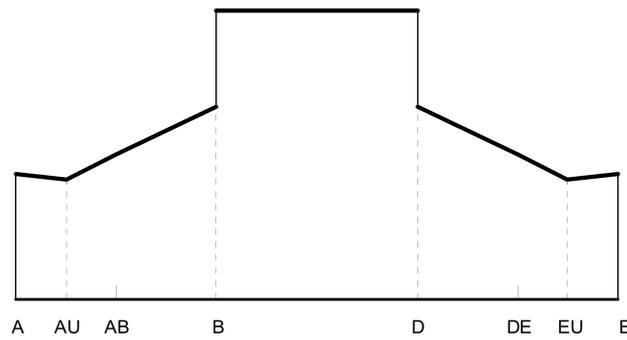


Figure 8 — Load sharing factor for cylindrical helical gears with  $\epsilon_\beta < 1$  and unmodified profiles, including the buttressing effect

The load sharing factor is obtained by multiplying the  $X_Y$  in 11.1 with the buttressing factor  $X_{but,Y}$  in 11.3.

### 11.5 Helical gears with $\epsilon_\beta < 1$ and profile modification

Helical gears with a contact ratio  $\epsilon_\alpha \geq 1$  and overlap ratio  $\epsilon_\beta < 1$ , have still poor single contact of tooth pairs. Hence, they can be treated similar to spur gears, considering the geometry in the transverse plane. See Figure 9, Figure 10 and Figure 11.

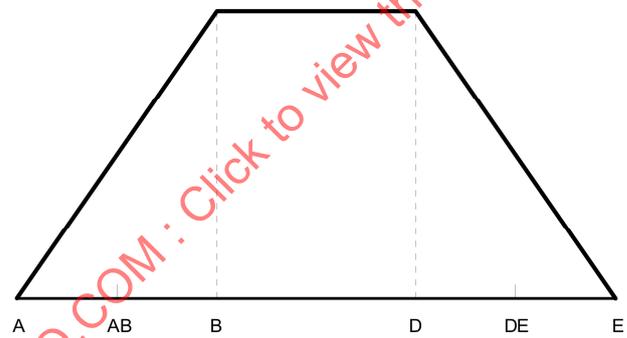


Figure 9 — Load sharing factor for cylindrical helical gears with  $\epsilon_\beta < 1$  and optimum profile modification

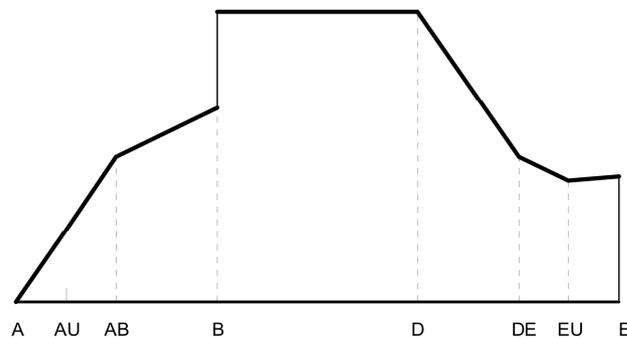
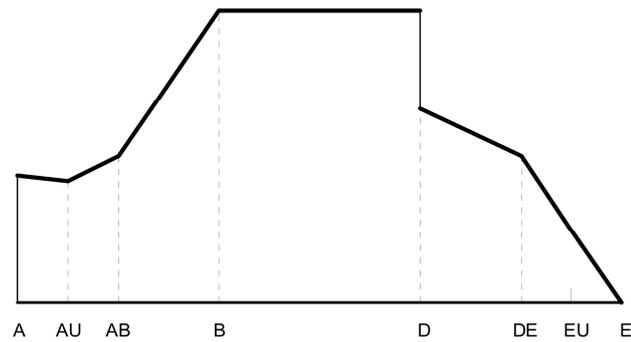


Figure 10 — Load sharing factor for cylindrical helical gears with  $\epsilon_\beta < 1$  and optimum profile modification on the addendum of the driven gear and/or the dedendum of the driving gear

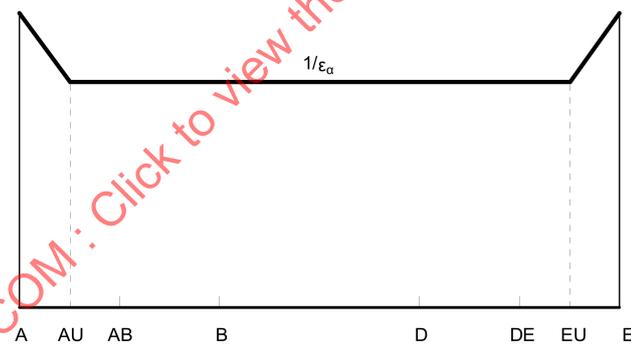


**Figure 11** — Load sharing factor for cylindrical helical gears with  $\varepsilon_{\beta} < 1$  and optimum profile modification on the addendum of the driving gear and/or the dedendum of the driven gear

The load sharing factor is obtained by multiplying the  $X_Y$  in 11.2 with the buttressing factor  $X_{\text{but},Y}$  in 11.3.

### 11.6 Helical gears with $\varepsilon_{\beta} \geq 1$ and unmodified profiles

The buttressing effect of local high mesh stiffness at the end of oblique contact lines for helical gears with  $\varepsilon_{\alpha} \geq 1$  and  $\varepsilon_{\beta} \geq 1$ , is assumed to act near the ends A and E along the helix teeth over a constant length, which corresponds to a transverse relative distance  $0,2 \text{ mm} \cdot \sin \beta_b$ ; see Figure 12. See also 11.3 and Figure 7.



**Figure 12** — Load sharing factor for cylindrical helical gears with  $\varepsilon_{\beta} \geq 1$  and unmodified profiles

The load sharing factor is obtained by multiplying the value  $1/\varepsilon_{\alpha}$ , representing the mean load, with the buttressing factor  $X_{\text{but},Y}$ .

$$X_Y = \frac{1}{\varepsilon_{\alpha}} \cdot X_{\text{but},Y} \quad (65)$$

where

$\varepsilon_{\alpha}$  is the transverse contact ratio.

11.7 Helical gears with  $\epsilon_\beta \geq 1$  and profile modification

Tip relief on the pinion (respectively wheel) reduces  $X_Y$  in the range DE-E (respectively A-AB) and increases  $X_Y$  in the range AB-DE, see Figure 13, Figure 14 and Figure 15. The extensions of tip relief at both ends A-AB and DE-E of the path of contact are assumed to be equal and to result in a contact ratio  $\epsilon_\alpha = 1$  for unloaded gears; see Figure 13.

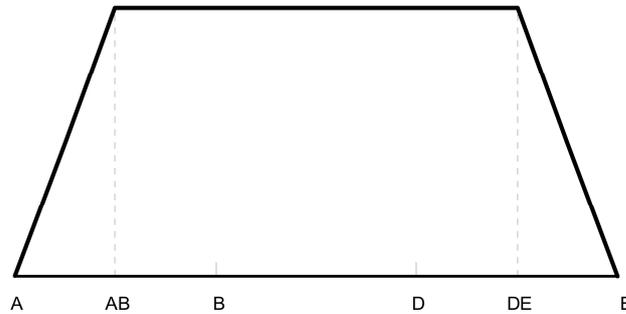


Figure 13 — Load sharing factor for cylindrical helical gears with  $\epsilon_\beta \geq 1$  and optimum profile modification

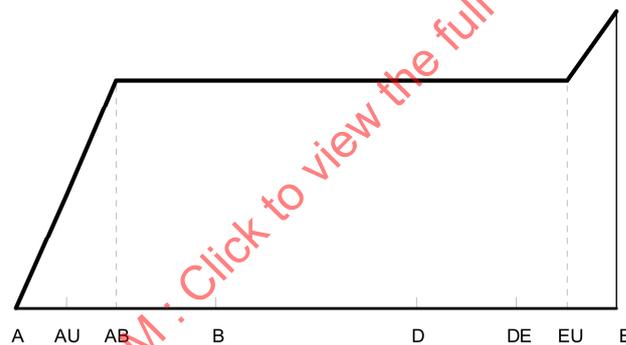


Figure 14 — Load sharing factor for cylindrical helical gears with  $\epsilon_\beta \geq 1$  and optimum profile modification on the addendum of the driven gear and/or the dedendum of the driving gear

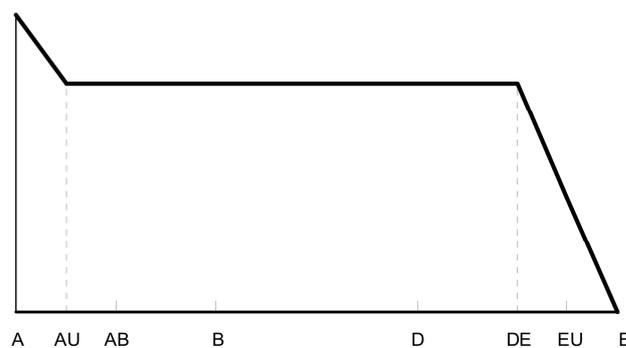


Figure 15 — Load sharing factor for cylindrical helical gears with  $\epsilon_\beta \geq 1$  and optimum profile modification on the addendum of the driving gear and/or the dedendum of the driven gear

The ranges are marked by the following values. Linear interpolation between these values is possible.

$$X_Y = \left[ \frac{1}{\varepsilon_\alpha} + \frac{(\varepsilon_\alpha - 1)}{2 \cdot \varepsilon_\alpha \cdot (\varepsilon_\alpha + 1)} \right] \cdot X_{\text{but},Y} \quad \text{for } g_A \leq g_Y \leq g_{AB} \quad \text{if } C_{a1} = C_{\text{eff}} \text{ and } C_{a2} = 0 \mu\text{m} \quad (66)$$

$$X_Y = \left[ \frac{1}{\varepsilon_\alpha} + \frac{(\varepsilon_\alpha - 1)}{2 \cdot \varepsilon_\alpha \cdot (\varepsilon_\alpha + 1)} \right] \cdot \frac{g_Y}{g_{AB}} \quad \text{for } g_A \leq g_Y \leq g_{AB} \quad \text{if } C_{a1} = 0 \mu\text{m} \text{ and } C_{a2} = C_{\text{eff}} \quad (67)$$

$$X_Y = \left[ \frac{1}{\varepsilon_\alpha} + \frac{(\varepsilon_\alpha - 1)}{\varepsilon_\alpha \cdot (\varepsilon_\alpha + 1)} \right] \cdot \frac{g_Y}{g_{AB}} \quad \text{for } g_A \leq g_Y \leq g_{AB} \quad \text{if } C_{a1} = C_{a2} = C_{\text{eff}} \quad (68)$$

$$X_Y = \frac{1}{\varepsilon_\alpha} + \frac{(\varepsilon_\alpha - 1)}{2 \cdot \varepsilon_\alpha \cdot (\varepsilon_\alpha + 1)} \quad \text{for } g_{AB} \leq g_Y \leq g_{DE} \quad \text{if } C_{a1} = 0 \mu\text{m} \text{ and } C_{a2} = C_{\text{eff}} \quad (69)$$

if  $C_{a1} = C_{\text{eff}}$  and  $C_{a2} = 0 \mu\text{m}$

$$X_Y = \frac{1}{\varepsilon_\alpha} + \frac{(\varepsilon_\alpha - 1)}{\varepsilon_\alpha \cdot (\varepsilon_\alpha + 1)} \quad \text{for } g_{AB} \leq g_Y \leq g_{DE} \quad \text{if } C_{a1} = C_{a2} = C_{\text{eff}} \quad (70)$$

$$X_Y = \left[ \frac{1}{\varepsilon_\alpha} + \frac{(\varepsilon_\alpha - 1)}{2 \cdot \varepsilon_\alpha \cdot (\varepsilon_\alpha + 1)} \right] \cdot \frac{g_\alpha - g_Y}{g_\alpha - g_{DE}} \quad \text{for } g_{DE} \leq g_Y \leq g_E \quad \text{if } C_{a1} = C_{\text{eff}} \text{ and } C_{a2} = 0 \mu\text{m} \quad (71)$$

$$X_Y = \left[ \frac{1}{\varepsilon_\alpha} + \frac{(\varepsilon_\alpha - 1)}{2 \cdot \varepsilon_\alpha \cdot (\varepsilon_\alpha + 1)} \right] \cdot X_{\text{but},Y} \quad \text{for } g_{DE} \leq g_Y \leq g_E \quad \text{if } C_{a1} = 0 \mu\text{m} \text{ and } C_{a2} = C_{\text{eff}} \quad (72)$$

$$X_Y = \left[ \frac{1}{\varepsilon_\alpha} + \frac{(\varepsilon_\alpha - 1)}{\varepsilon_\alpha \cdot (\varepsilon_\alpha + 1)} \right] \cdot \frac{g_\alpha - g_Y}{g_\alpha - g_{DE}} \quad \text{for } g_{DE} \leq g_Y \leq g_E \quad \text{if } C_{a1} = C_{a2} = C_{\text{eff}} \quad (73)$$

## 12 Contact temperature $\theta_{B,Y}$

The local contact temperature  $\theta_{B,Y}$  is defined as the sum of bulk temperature  $\theta_M$  and local flash temperature  $\theta_{fl,Y}$ . As a result of friction in the teeth mesh, the flash temperature  $\theta_{fl,Y}$  varies along the path of contact. Hence the local flash temperature  $\theta_{fl,Y}$  has to be determined for every desired point Y in the field of contact. For simplification the bulk temperature  $\theta_M$  is assumed as constant.

$$\theta_{B,Y} = \theta_M + \theta_{fl,Y} \quad (74)$$

where

$\theta_{fl,Y}$  is the local flash temperature (see clause 13);

$\theta_M$  is the bulk temperature (see clause 14).

## 13 Flash temperature $\theta_{fl,Y}$

The flash temperature  $\theta_{fl,Y}$  of the gear flanks is rapidly fluctuating in contact. In every mesh position different rolling and sliding conditions occur. Furthermore the local contact load varies along the path of contact. These conditions cause a continuous variation of the flash temperature which can be calculated according to Blok [13] by equation (75).

$$\theta_{fl,Y} = \frac{\sqrt{\pi}}{2} \cdot \frac{\mu_m \cdot \rho_{dyn,Y} \cdot 10^6 \cdot |V_{g,Y}|}{B_{M1} \cdot \sqrt{V_{r1,Y}} + B_{M2} \cdot \sqrt{V_{r2,Y}}} \cdot \sqrt{8 \cdot \rho_{n,Y} \cdot \frac{\rho_{dyn,Y}}{1000 \cdot E_r}} \quad (75)$$

where

$$V_{g,Y} = V_{r1,Y} - V_{r2,Y} \quad (76)$$

$$B_{M1} = \sqrt{\rho_{M1} \cdot c_{M1} \cdot \lambda_{M1}} \quad (77)$$

$$B_{M2} = \sqrt{\rho_{M2} \cdot c_{M2} \cdot \lambda_{M2}} \quad (78)$$

- $V_{g,Y}$  is the local sliding velocity;
- $B_{M1}$  is the thermal contact coefficient of pinion (see Table 2);
- $B_{M2}$  is the thermal contact coefficient of wheel (see Table 2);
- $\mu_m$  is the mean coefficient of friction (see 14.1);
- $\rho_{dyn,Y}$  is the local Hertzian contact stress (see 8.1 and 8.2);
- $V_{r1,Y}$  is the local tangential velocity on pinion (see 7.1);
- $V_{r2,Y}$  is the local tangential velocity on wheel (see 7.1);
- $\rho_{n,Y}$  is the local normal radius of relative curvature (see clause 10);
- $E_r$  is the reduced modulus of elasticity (see 6.1).

**Table 2 — Material properties of steel**

material	density $\rho_M$ [kg/m <sup>3</sup> ]	specific heat capacity $c_M$ [J/(kg·K)]	specific heat conductivity $\lambda_M$ [W/(m·K)]
steel	7800	440	45

## 14 Bulk temperature $\theta_M$

The bulk temperature  $\theta_M$  is the equilibrium temperature of the surface of the gear teeth before they enter the contact zone. The bulk temperature  $\theta_M$  should be measured or calculated by an adequate method. If this is not possible  $\theta_M$  can be approximated according to equation (79) (compare [10]).

$$\theta_M = \theta_{oil} + 7400 \cdot \left( \frac{P \cdot \mu_m \cdot H_v}{a \cdot b} \right)^{0,72} \cdot \frac{X_S}{1,2 \cdot X_{Ca}} \quad (79)$$

where

$$P = 2 \cdot \pi \cdot \frac{n_1}{60} \cdot \frac{T_1}{1000} \quad (80)$$

$P$  is the transmitted power;

- $a$  is the centre distance;
- $b$  is the face width;
- $\theta_{oil}$  is the lubricant inlet or oil sump temperature;
- $\mu_m$  is the mean coefficient of friction (see 14.1);
- $H_v$  is the load losses factor (see 14.2);
- $X_{Ca}$  is the tip relief factor (see 14.3);
- $X_S$  is the lubricant factor (see 14.4).

#### 14.1 Mean coefficient of friction $\mu_m$

The mean coefficient of friction  $\mu_m$  depends on the gear geometry, the surface roughness, the tangential velocity, the tangential load and the dynamic viscosity of the lubricant. It can be approximated by equation (81).

$$\mu_m = 0,045 \cdot \left( \frac{K_A \cdot K_V \cdot K_{H\alpha} \cdot K_{H\beta} \cdot F_{bt} \cdot K_{By}}{b \cdot v_{\Sigma,C} \cdot \rho_{n,C}} \right)^{0,2} \cdot (10^3 \cdot \eta_{\theta oil})^{-0,05} \cdot X_R \cdot X_L \quad (81)$$

where

$$X_R = 2,2 \cdot \left( \frac{Ra}{\rho_{n,C}} \right)^{0,25} \quad (82)$$

- $X_R$  is the roughness factor;
- $b$  is the face width;
- $F_{bt}$  is the nominal transverse load in plane of action;
- $K_A$  is the application factor (according to ISO 6336-1);
- $K_{By}$  is the helical load factor (see below);
- $K_{H\alpha}$  is the transverse load factor (according to ISO 6336-1);
- $K_{H\beta}$  is the face load factor (according to ISO 6336-1);
- $K_V$  is the dynamic factor (according to ISO 6336-1);
- $v_{\Sigma,C}$  is the sum of the tangential velocities at the pitch point (see 7.1);
- $\eta_{\theta oil}$  is the dynamic viscosity at inlet or oil sump temperature;
- $\rho_{n,C}$  is the normal radius of relative curvature at the pitch diameter;
- $Ra$  is the effective arithmetic mean roughness value (see 5.3);
- $X_L$  is the lubricant factor (see Table 3).

The helical load factor  $K_{By}$  takes into account an increasing friction for increasing total contact ratio (see Figure 16).

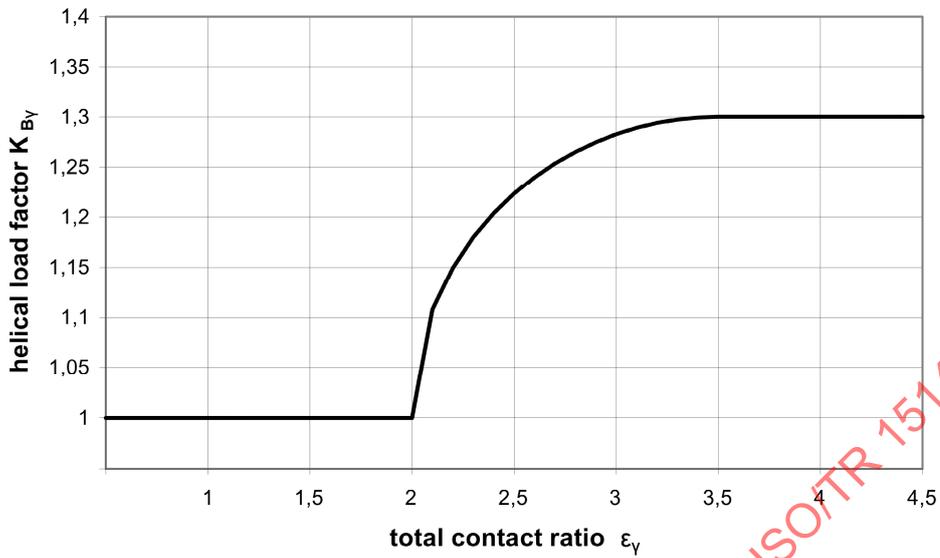


Figure 16 — Helical load factor  $K_{By}$

$$K_{By} = 1,0 \quad \text{if } \epsilon_v \leq 2 \quad (83)$$

$$K_{By} = 1 + 0,2 \cdot \sqrt{(\epsilon_v - 2) \cdot (5 - \epsilon_v)} \quad \text{if } 2 < \epsilon_v < 3,5 \quad (84)$$

$$K_{By} = 1,3 \quad \text{if } \epsilon_v \geq 3,5 \quad (85)$$

Table 3 — Lubricant factor,  $X_L$

oil type	$X_L$
mineral oil	1,0
polyalphaolefin	0,8
non water-soluble polyglycols	0,7
water-soluble polyglycols	0,6
traction fluid	1,5
phosphate ester	1,3

#### 14.2 Load losses factor $H_v$

The load losses factor  $H_v$  is calculated according to equation (86) and (87).

$$H_v = (\epsilon_1^2 + \epsilon_2^2 + 1 - \epsilon_\alpha) \cdot \left( \frac{1}{z_1} + \frac{1}{z_2} \right) \cdot \frac{\pi}{\cos \beta_b} \quad \text{if } \epsilon_\alpha < 2 \quad (86)$$

$$H_v = 0,5 \cdot \varepsilon_\alpha \cdot \left( \frac{1}{z_1} + \frac{1}{z_2} \right) \cdot \frac{\pi}{\cos \beta_b} \quad \text{if } \varepsilon_\alpha \geq 2 \quad (87)$$

where

- $z_1$  is the number of teeth of pinion;  
 $z_2$  is the number of teeth of wheel;  
 $\beta_b$  is the base helix angle;  
 $\varepsilon_1$  is the addendum contact ratio of the pinion;  
 $\varepsilon_2$  is the addendum contact ratio of the wheel;  
 $\varepsilon_\alpha$  is the transverse contact ratio.

### 14.3 Tip relief factor $X_{Ca}$

The elastic deformation of the meshing teeth results in overload on the tip in the area of high sliding. The tip relief factor  $X_{Ca}$  according to Figure 17 considers the positive influence of the profile modification on this overload.  $X_{Ca}$  is a relative tip relief factor which depends on the actual values of tip relief  $C_{a1}$ ,  $C_{a2}$ , the effective tip relief  $C_{eff}$ , the ratio of addendum contact ratios and the direction of power flow.

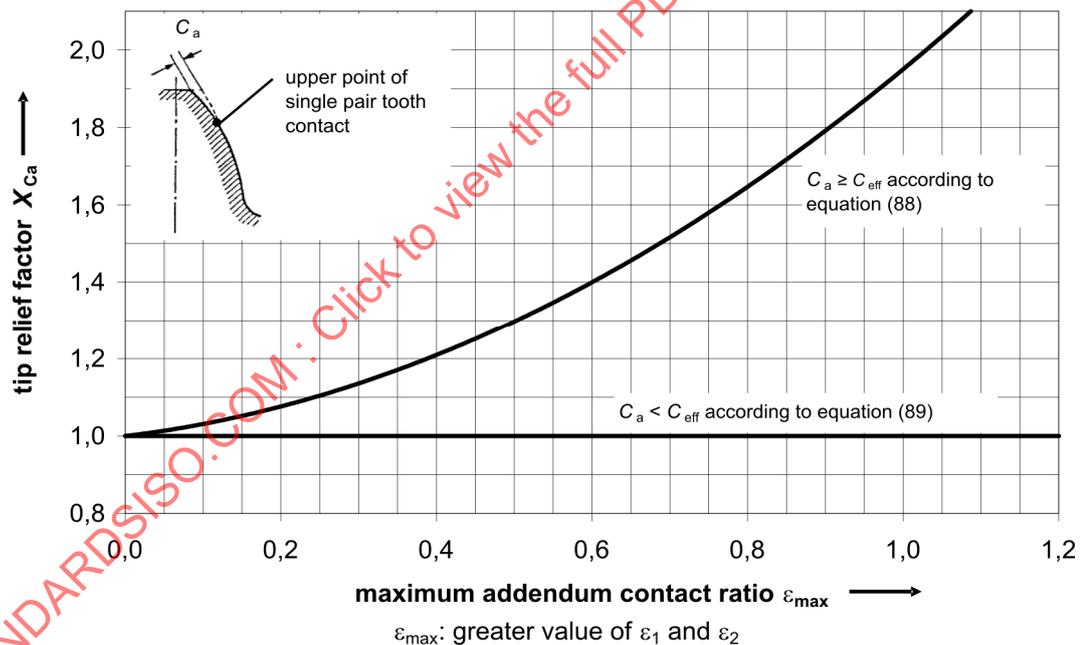


Figure 17 — Tip relief factor  $X_{Ca}$

The curves in Figure 17 can be approximated by the following equations:

$$X_{Ca} = 1 + 0,24 \cdot \varepsilon_{max} + 0,71 \cdot \varepsilon_{max}^2 \quad \begin{array}{l} \text{if pinion drives wheel and } \varepsilon_1 > 1,5 \cdot \varepsilon_2 \text{ and } C_{a1} \geq C_{eff} \\ \text{if pinion drives wheel and } \varepsilon_1 \leq 1,5 \cdot \varepsilon_2 \text{ and } C_{a2} \geq C_{eff} \\ \text{if wheel drives pinion and } \varepsilon_1 > (2/3) \cdot \varepsilon_2 \text{ and } C_{a1} \geq C_{eff} \\ \text{if wheel drives pinion and } \varepsilon_1 \leq (2/3) \cdot \varepsilon_2 \text{ and } C_{a2} \geq C_{eff} \end{array} \quad (88)$$

$$X_{Ca} = 1,0 \quad \text{in all other cases} \quad (89)$$

where

$C_{eff}$  is the effective tip relief (see below);

$\varepsilon_{max}$  is the maximum value,  $\varepsilon_1$  or  $\varepsilon_2$ .

$C_{eff}$  is the effective tip relief, that amount of tip relief which compensates for the elastic deformation of the teeth in single pair contact.

$$C_{eff} = \frac{K_A \cdot F_t}{b \cdot c'} \quad \text{for spur gears} \quad (90)$$

$$C_{eff} = \frac{K_A \cdot F_t}{b \cdot c_{\gamma\alpha}} \quad \text{for helical gears} \quad (91)$$

where

$b$  is the face width;

$c'$  is the single stiffness of a tooth pair per unit face width (according to ISO 6336-1);

$c_{\gamma\alpha}$  is the mean value of mesh stiffness per unit face width (according to ISO 6336-1);

$F_t$  is the transverse tangential load at reference cylinder;

$K_A$  is the application factor (according to ISO 6336-1).

Tip relief factor as described above applies to gears of ISO accuracy grade  $\leq 6$ , in accordance with ISO 1328-1. For less accurate gears,  $X_{Ca}$  is to be set equal to 1; see also ISO 6336-1.

#### 14.4 Lubrication factor $X_S$

The lubrication factor takes into account a better heat transfer for dip lubrication than for injection lubrication. The following values apply.

$X_S = 1,2$  for injection lubrication;

$X_S = 1,0$  for dip lubrication;

$X_S = 0,2$  for gears submerged in oil.

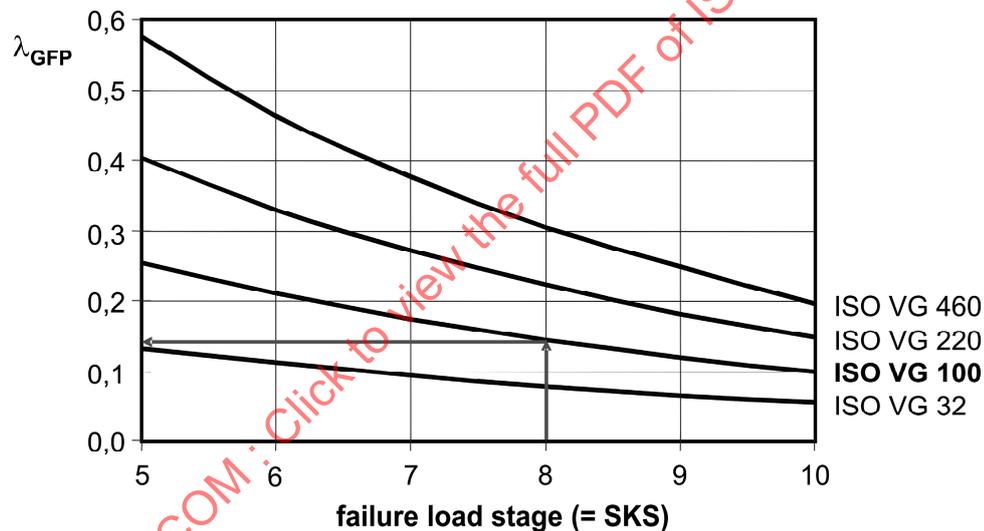
## Annex A (informative)

### Calculation of the permissible specific lubricant film thickness $\lambda_{GFP}$ for oils with a micropitting test result according to FVA-Information Sheet 54/7

The following information in this annex is provided as reference only and should not be interpreted as generalised part of the procedure defined in this Technical Report.

One test procedure used to evaluate the micropitting load capacity of gear lubricants is the FVA-FZG-micropitting test according to FVA-Information Sheet 54/7 [7].

For mineral oils investigated in this test procedure  $\lambda_{GFP}$  can be taken from Figure A.1 depending on the nominal oil viscosity and the failure load stage SKS reached in the test C-GF/8,3/90. Interpolation between the stated values is possible.



**Figure A.1 — Minimum permissible specific lubricant film thickness for mineral oils as function of nominal lubricant viscosity and failure load stage SKS of the FVA-FZG micropitting test C-GF/8,3/90 with  $R_a = 0,50 \mu\text{m}$**

For other test conditions or different lubricants than presented in Figure A.1 the critical specific lubricant film thickness  $\lambda_{GFT}$  in contact point A of the specified test gears type C-GF is calculated at the reached failure load stage according to equation (2). The required gear geometry of the test gears type C-GF is specified in FVA-Information Sheet 54/7. In this case the permissible specific lubricant film thickness  $\lambda_{GFP}$  is defined according to equation (A.1). The material factor  $W_W$  takes into account the influence of gear material different from the case carburised standardised test gears type C-GF.

$$\lambda_{GFP} = 1,4 \cdot W_W \cdot \lambda_{GFT} \quad (\text{A.1})$$

where

$W_W$  is the material factor (see Table A.1);

$\lambda_{GFT}$  is the specific lubricant film thickness ascertained by tests (see 5.3).

NOTE If no value for the failure load stage SKS of the lubricant is available, use the value  $\lambda_{GFP}$  of the lubricant for failure load stage SKS 5.

**Table A.1 — Material factor,  $W_w$**

Material	Material factor, $W_w$
Case carburised steel, with austenite content: - less than 25 % - greater than 25 %	1,0 0,95
Gas nitrided steel (HV > 850)	1,5
Induction, flame hardened steel	0,65
Through hardened steel	0,5

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## Annex B (informative)

### Example calculation

In the following annex an example calculation is presented. The calculation sequence has been provided to follow a logical approach with relation to the input data.

The example calculates the safety factor  $S_\lambda$  of a specific gear set when compared to an allowable  $\lambda_{\text{GFP}}$  value. Whilst any suitable test method can be used to determine the allowable  $\lambda_{\text{GFP}}$  value the calculation provided uses a  $\lambda_{\text{GFP}}$  established by the FVA-FZG micropitting test (Method B) as outlined in Annex A.

The result of this example is confirmed by experimental investigations. The gears were obviously micropitted and had profile deviations of approximately 10  $\mu\text{m}$ .

#### B.1 Input

##### B.1.1 Input of gear data

number of teeth of pinion:	$z_1 = 18$
number of teeth of wheel:	$z_2 = 18$
normal module:	$m_n = 10,93 \text{ mm}$
tip diameter of pinion:	$d_{a1} = 221,4 \text{ mm}$
tip diameter of wheel:	$d_{a2} = 221,4 \text{ mm}$
addendum modification factor of pinion:	$x_1 = 0,158$
addendum modification factor of wheel:	$x_2 = 0,158$
face width:	$b = 21,4 \text{ mm}$
helix angle:	$\beta = 0^\circ$
normal pressure angle:	$\alpha_n = 20^\circ$
centre distance:	$a = 200 \text{ mm}$
gear quality:	$Q = 5$
arithmetic mean roughness value of pinion:	$Ra_1 = 0,90 \mu\text{m}$
arithmetic mean roughness value of wheel:	$Ra_2 = 0,90 \mu\text{m}$
tooth flank modifications:	no modifications

**B.1.2 Input of material data**

modulus of elasticity of pinion:	$E_1 = 206000 \text{ N/mm}^2$
modulus of elasticity of wheel:	$E_2 = 206000 \text{ N/mm}^2$
Poisson's ratio of pinion:	$\nu_1 = 0,3$
Poisson's ratio of wheel:	$\nu_2 = 0,3$
specific heat conductivity of pinion:	$\lambda_{M1} = 45 \text{ W/(mK)}$
specific heat conductivity of wheel:	$\lambda_{M2} = 45 \text{ W/(mK)}$
specific heat per unit mass of pinion:	$c_{M1} = 440 \text{ J/(kgK)}$
specific heat per unit mass of wheel:	$c_{M2} = 440 \text{ J/(kgK)}$
density of pinion:	$\rho_{M1} = 7800 \text{ kg/m}^3$
density of wheel:	$\rho_{M2} = 7800 \text{ kg/m}^3$
material factor according to Table A.1: (for matching case carburised/ case carburised)	$W_W = 1,0$

**B.1.3 Input of operating data**

nominal torque at the pinion:	$T_1 = 1878 \text{ Nm}$
rotation speed of the pinion:	$n_1 = 3000 \text{ min}^{-1}$
application factor:	$K_A = 1,0$
dynamic factor:	$K_V = 1,15$
transverse load factor:	$K_{H\alpha} = 1,0$
face load factor:	$K_{H\beta} = 1,10$

**B.1.4 Input of lubricant data**

oil inlet temperature (injection lubrication):	$\theta_{oil} = 90 \text{ }^\circ\text{C}$
kinematic viscosity at 40 °C:	$\nu_{40} = 210 \text{ mm}^2/\text{s}$
kinematic viscosity at 100 °C:	$\nu_{100} = 18,5 \text{ mm}^2/\text{s}$
density of the lubricant at 15 °C:	$\rho_{15} = 895 \text{ kg/m}^3$
oil type:	mineral oil
failure load stage at operating temperature according to FVA 54/7:	SKS 8

## B.2 Calculation of the current specific lubricant film thickness

### B.2.1 Calculation of gear geometry (according to ISO 21771)

basic values:

$$m_t = \frac{m_n}{\cos \beta} \quad m_t = 10,93 \text{ mm}$$

$$d_1 = z_1 \cdot m_t \quad d_1 = 196,74 \text{ mm}$$

$$d_2 = z_2 \cdot m_t \quad d_2 = 196,74 \text{ mm}$$

$$u = \frac{z_2}{z_1} \quad u = 1$$

$$\alpha_t = \arctan\left(\frac{\tan \alpha_n}{\cos \beta}\right) \quad \alpha_t = 20^\circ$$

$$d_{b1} = d_1 \cdot \cos \alpha_t \quad d_{b1} = 184,875 \text{ mm}$$

$$d_{b2} = d_2 \cdot \cos \alpha_t \quad d_{b2} = 184,875 \text{ mm}$$

$$d_{w1} = \frac{2 \cdot a}{u + 1} \quad d_{w1} = 200 \text{ mm}$$

$$d_{w2} = 2 \cdot a - d_{w1} \quad d_{w2} = 200 \text{ mm}$$

$$\alpha_{wt} = \arccos\left[\frac{(z_1 + z_2) \cdot m_t \cdot \cos \alpha_t}{2 \cdot a}\right] \quad \alpha_{wt} = 22,426^\circ$$

$$\beta_b = \arcsin(\sin \beta \cdot \cos \alpha_n) \quad \beta_b = 0^\circ$$

$$\rho_{et} = m_t \cdot \pi \cdot \cos \alpha_t \quad \rho_{et} = 32,267 \text{ mm}$$

$$\varepsilon_1 = \frac{z_1}{2 \cdot \pi} \cdot \left[ \sqrt{\left(\frac{d_{a1}}{d_{b1}}\right)^2} - 1 - \tan \alpha_{wt} \right] \quad \varepsilon_1 = 0,705$$

$$\varepsilon_2 = \frac{z_2}{2 \cdot \pi} \cdot \left[ \sqrt{\left(\frac{d_{a2}}{d_{b2}}\right)^2} - 1 - \tan \alpha_{wt} \right] \quad \varepsilon_2 = 0,705$$

$$\varepsilon_\alpha = \frac{1}{\rho_{et}} \cdot \left( \sqrt{\frac{d_{a1}^2}{4} - \frac{d_{b1}^2}{4}} + \sqrt{\frac{d_{a2}^2}{4} - \frac{d_{b2}^2}{4}} - a \cdot \sin \alpha_{wt} \right) \quad \varepsilon_\alpha = 1,411$$

$$\varepsilon_\beta = \frac{b \cdot \sin \beta}{m_n \cdot \pi} \quad \varepsilon_\beta = 0$$

$$\varepsilon_V = \varepsilon_\alpha + \varepsilon_\beta$$

$$\varepsilon_V = 1,411$$

$$g_\alpha = 0,5 \cdot \left( \sqrt{d_{a1}^2 - d_{b1}^2} + \sqrt{d_{a2}^2 - d_{b2}^2} \right) - a \cdot \sin \alpha_{wt}$$

$$g_\alpha = 45,519 \text{ mm}$$

coordinates of the basic points (A, AB, B, C, D, DE, E) on the line of action (see clause 10):

$$g_A = 0 \text{ mm}$$

$$g_A = 0 \text{ mm}$$

$$g_{AB} = \frac{g_\alpha - p_{et}}{2}$$

$$g_{AB} = 6,626 \text{ mm}$$

$$g_B = g_\alpha - p_{et}$$

$$g_B = 13,253 \text{ mm}$$

$$g_C = \frac{d_{b1}}{2} \cdot \tan \alpha_{wt} - \sqrt{\frac{d_{a1}^2}{4} - \frac{d_{b1}^2}{4}} + g_\alpha$$

$$g_C = 22,760 \text{ mm}$$

$$g_D = p_{et}$$

$$g_D = 32,267 \text{ mm}$$

$$g_{DE} = \frac{g_\alpha - p_{et}}{2} + p_{et}$$

$$g_{DE} = 38,893 \text{ mm}$$

$$g_E = g_\alpha$$

$$g_E = 45,519 \text{ mm}$$

$$d_{A1} = 2 \cdot \sqrt{\frac{d_{b1}^2}{4} + \left( \sqrt{\frac{d_{a1}^2}{4} - \frac{d_{b1}^2}{4}} - g_\alpha + g_A \right)^2}$$

$$d_{A1} = 187,419 \text{ mm}$$

$$d_{AB1} = 2 \cdot \sqrt{\frac{d_{b1}^2}{4} + \left( \sqrt{\frac{d_{a1}^2}{4} - \frac{d_{b1}^2}{4}} - g_\alpha + g_{AB} \right)^2}$$

$$d_{AB1} = 190,046 \text{ mm}$$

$$d_{B1} = 2 \cdot \sqrt{\frac{d_{b1}^2}{4} + \left( \sqrt{\frac{d_{a1}^2}{4} - \frac{d_{b1}^2}{4}} - g_\alpha + g_B \right)^2}$$

$$d_{B1} = 193,546 \text{ mm}$$

$$d_{C1} = 2 \cdot \sqrt{\frac{d_{b1}^2}{4} + \left( \sqrt{\frac{d_{a1}^2}{4} - \frac{d_{b1}^2}{4}} - g_\alpha + g_C \right)^2}$$

$$d_{C1} = 200,000 \text{ mm}$$

$$d_{D1} = 2 \cdot \sqrt{\frac{d_{b1}^2}{4} + \left( \sqrt{\frac{d_{a1}^2}{4} - \frac{d_{b1}^2}{4}} - g_\alpha + g_D \right)^2}$$

$$d_{D1} = 207,998 \text{ mm}$$

$$d_{DE1} = 2 \cdot \sqrt{\frac{d_{b1}^2}{4} + \left( \sqrt{\frac{d_{a1}^2}{4} - \frac{d_{b1}^2}{4}} - g_\alpha + g_{DE} \right)^2}$$

$$d_{DE1} = 214,394 \text{ mm}$$

$$d_{E1} = 2 \cdot \sqrt{\frac{d_{b1}^2}{4} + \left( \sqrt{\frac{d_{a1}^2}{4} - \frac{d_{b1}^2}{4}} - g_a + g_E \right)^2}$$

$$d_{E1} = 221,400 \text{ mm}$$

$$d_{A2} = 2 \cdot \sqrt{\frac{d_{b2}^2}{4} + \left( \sqrt{\frac{d_{a2}^2}{4} - \frac{d_{b2}^2}{4}} - g_A \right)^2}$$

$$d_{A2} = 221,400 \text{ mm}$$

$$d_{AB2} = 2 \cdot \sqrt{\frac{d_{b2}^2}{4} + \left( \sqrt{\frac{d_{a2}^2}{4} - \frac{d_{b2}^2}{4}} - g_{AB} \right)^2}$$

$$d_{AB2} = 214,394 \text{ mm}$$

$$d_{B2} = 2 \cdot \sqrt{\frac{d_{b2}^2}{4} + \left( \sqrt{\frac{d_{a2}^2}{4} - \frac{d_{b2}^2}{4}} - g_B \right)^2}$$

$$d_{B2} = 207,998 \text{ mm}$$

$$d_{C2} = 2 \cdot \sqrt{\frac{d_{b2}^2}{4} + \left( \sqrt{\frac{d_{a2}^2}{4} - \frac{d_{b2}^2}{4}} - g_C \right)^2}$$

$$d_{C2} = 200,000 \text{ mm}$$

$$d_{D2} = 2 \cdot \sqrt{\frac{d_{b2}^2}{4} + \left( \sqrt{\frac{d_{a2}^2}{4} - \frac{d_{b2}^2}{4}} - g_D \right)^2}$$

$$d_{D2} = 193,546 \text{ mm}$$

$$d_{DE2} = 2 \cdot \sqrt{\frac{d_{b2}^2}{4} + \left( \sqrt{\frac{d_{a2}^2}{4} - \frac{d_{b2}^2}{4}} - g_{DE} \right)^2}$$

$$d_{DE2} = 190,046 \text{ mm}$$

$$d_{E2} = 2 \cdot \sqrt{\frac{d_{b2}^2}{4} + \left( \sqrt{\frac{d_{a2}^2}{4} - \frac{d_{b2}^2}{4}} - g_E \right)^2}$$

$$d_{E2} = 187,419 \text{ mm}$$

transverse radius of relative curvature:

$$\rho_{t1,A} = \sqrt{\frac{d_{A1}^2 - d_{b1}^2}{4}}$$

$$\rho_{t1,A} = 15,389 \text{ mm}$$

$$\rho_{t1,AB} = \sqrt{\frac{d_{AB1}^2 - d_{b1}^2}{4}}$$

$$\rho_{t1,AB} = 22,015 \text{ mm}$$

$$\rho_{t1,B} = \sqrt{\frac{d_{B1}^2 - d_{b1}^2}{4}}$$

$$\rho_{t1,B} = 28,641 \text{ mm}$$

$$\rho_{t1,C} = \sqrt{\frac{d_{C1}^2 - d_{b1}^2}{4}}$$

$$\rho_{t1,C} = 38,148 \text{ mm}$$

$$\rho_{t1,D} = \sqrt{\frac{d_{D1}^2 - d_{b1}^2}{4}}$$

$$\rho_{1,D} = 47,655 \text{ mm}$$

$$\rho_{t1,DE} = \sqrt{\frac{d_{DE1}^2 - d_{b1}^2}{4}}$$

$$\rho_{1,DE} = 54,282 \text{ mm}$$

$$\rho_{t1,E} = \sqrt{\frac{d_{E1}^2 - d_{b1}^2}{4}}$$

$$\rho_{1,E} = 60,908 \text{ mm}$$

$$\rho_{t2,A} = \sqrt{\frac{d_{A2}^2 - d_{b2}^2}{4}}$$

$$\rho_{2,A} = 60,908 \text{ mm}$$

$$\rho_{t2,AB} = \sqrt{\frac{d_{AB2}^2 - d_{b2}^2}{4}}$$

$$\rho_{2,AB} = 54,282 \text{ mm}$$

$$\rho_{t2,B} = \sqrt{\frac{d_{B2}^2 - d_{b2}^2}{4}}$$

$$\rho_{2,B} = 47,655 \text{ mm}$$

$$\rho_{t2,C} = \sqrt{\frac{d_{C2}^2 - d_{b2}^2}{4}}$$

$$\rho_{2,C} = 38,148 \text{ mm}$$

$$\rho_{t2,D} = \sqrt{\frac{d_{D2}^2 - d_{b2}^2}{4}}$$

$$\rho_{2,D} = 28,641 \text{ mm}$$

$$\rho_{t2,DE} = \sqrt{\frac{d_{DE2}^2 - d_{b2}^2}{4}}$$

$$\rho_{2,DE} = 22,015 \text{ mm}$$

$$\rho_{t2,E} = \sqrt{\frac{d_{E2}^2 - d_{b2}^2}{4}}$$

$$\rho_{2,E} = 15,389 \text{ mm}$$

$$\rho_{t,A} = \frac{\rho_{t1,A} \cdot \rho_{t2,A}}{\rho_{t1,A} + \rho_{t2,A}}$$

$$\rho_{t,A} = 12,285 \text{ mm}$$

$$\rho_{t,AB} = \frac{\rho_{t1,AB} \cdot \rho_{t2,AB}}{\rho_{t1,AB} + \rho_{t2,AB}}$$

$$\rho_{t,AB} = 15,663 \text{ mm}$$

$$\rho_{t,B} = \frac{\rho_{t1,B} \cdot \rho_{t2,B}}{\rho_{t1,B} + \rho_{t2,B}}$$

$$\rho_{t,B} = 17,890 \text{ mm}$$

$$\rho_{t,C} = \frac{\rho_{t1,C} \cdot \rho_{t2,C}}{\rho_{t1,C} + \rho_{t2,C}}$$

$$\rho_{t,C} = 19,074 \text{ mm}$$

$$\rho_{t,D} = \frac{\rho_{t1,D} \cdot \rho_{t2,D}}{\rho_{t1,D} + \rho_{t2,D}}$$

$$\rho_{t,D} = 17,890 \text{ mm}$$

$$\rho_{t,DE} = \frac{\rho_{t1,DE} \cdot \rho_{t2,DE}}{\rho_{t1,DE} + \rho_{t2,DE}}$$

$$\rho_{t,DE} = 15,663 \text{ mm}$$

$$\rho_{t,E} = \frac{\rho_{t1,E} \cdot \rho_{t2,E}}{\rho_{t1,E} + \rho_{t2,E}}$$

$$\rho_{t,E} = 12,285 \text{ mm}$$

normal radius of relative curvature:

$$\rho_{n,A} = \frac{\rho_{t,A}}{\cos \beta_b}$$

$$\rho_{n,A} = 12,285 \text{ mm}$$

$$\rho_{n,AB} = \frac{\rho_{t,AB}}{\cos \beta_b}$$

$$\rho_{n,AB} = 15,663 \text{ mm}$$

$$\rho_{n,B} = \frac{\rho_{t,B}}{\cos \beta_b}$$

$$\rho_{n,B} = 17,890 \text{ mm}$$

$$\rho_{n,C} = \frac{\rho_{t,C}}{\cos \beta_b}$$

$$\rho_{n,C} = 19,074 \text{ mm}$$

$$\rho_{n,D} = \frac{\rho_{t,D}}{\cos \beta_b}$$

$$\rho_{n,D} = 17,890 \text{ mm}$$

$$\rho_{n,DE} = \frac{\rho_{t,DE}}{\cos \beta_b}$$

$$\rho_{n,DE} = 15,663 \text{ mm}$$

$$\rho_{n,E} = \frac{\rho_{t,E}}{\cos \beta_b}$$

$$\rho_{n,E} = 12,285 \text{ mm}$$

## B.2.2 Calculation of material data

$$E_r = 2 \cdot \left( \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2} \right)^{-1}$$

$$E_r = 226374 \text{ N/mm}^2$$

$$B_{M1} = \sqrt{\lambda_{M1} \cdot \rho_{M1} \cdot c_{M1}}$$

$$B_{M1} = 12427,4 \text{ N/(ms}^{0,5}\text{K)}$$

$$B_{M2} = \sqrt{\lambda_{M2} \cdot \rho_{M2} \cdot c_{M2}}$$

$$B_{M2} = 12427,4 \text{ N/(ms}^{0,5}\text{K)}$$

## B.2.3 Calculation of operating conditions

loading:

$$P = 2 \cdot \pi \cdot \frac{n_1}{60} \cdot \frac{T_1}{1000}$$

$$P = 590 \text{ kW}$$

$$F_t = 2000 \cdot \frac{T_1}{d_1}$$

$$F_t = 19091 \text{ N}$$

$$F_{bt} = 2000 \cdot \frac{T_1}{d_{b1}}$$

$$F_{bt} = 20316 \text{ N}$$

local load sharing factor:

(no tooth flank modification, spur gears, gear quality  $\leq 7 \rightarrow$  see Figure 2)

$$X_A = \frac{1}{3} + \frac{1}{3} \cdot \frac{g_A}{g_B}$$

$$X_A = 0,333$$

$$X_{AB} = \frac{1}{3} + \frac{1}{3} \cdot \frac{g_{AB}}{g_B}$$

$$X_{AB} = 0,5$$

$$X_B = 1,0$$

$$X_B = 1,0$$

$$X_C = 1,0$$

$$X_C = 1,0$$

$$X_D = 1,0$$

$$X_D = 1,0$$

$$X_{DE} = \frac{1}{3} + \frac{1}{3} \cdot \frac{g_\alpha - g_{DE}}{g_\alpha - g_D}$$

$$X_{DE} = 0,5$$

$$X_E = \frac{1}{3} + \frac{1}{3} \cdot \frac{g_\alpha - g_E}{g_\alpha - g_D}$$

$$X_E = 0,333$$

elasticity factor:

$$Z_E = \sqrt{\frac{E_r}{2 \cdot \pi}}$$

$$Z_E = 189,812 \text{ (N/mm}^2\text{)}^{0,5}$$

local Hertzian contact stress:

$$\rho_{H,A,B} = Z_E \cdot \sqrt{\frac{F_t \cdot X_A}{b \cdot \rho_{n,A} \cdot \cos \alpha_t \cdot \cos \beta_b}}$$

$$\rho_{H,A,B} = 963 \text{ N/mm}^2$$

$$\rho_{H,AB,B} = Z_E \cdot \sqrt{\frac{F_t \cdot X_{AB}}{b \cdot \rho_{n,AB} \cdot \cos \alpha_t \cdot \cos \beta_b}}$$

$$\rho_{H,AB,B} = 1045 \text{ N/mm}^2$$

$$\rho_{H,B,B} = Z_E \cdot \sqrt{\frac{F_t \cdot X_B}{b \cdot \rho_{n,B} \cdot \cos \alpha_t \cdot \cos \beta_b}}$$

$$\rho_{H,B,B} = 1383 \text{ N/mm}^2$$

$$\rho_{H,C,B} = Z_E \cdot \sqrt{\frac{F_t \cdot X_C}{b \cdot \rho_{n,C} \cdot \cos \alpha_t \cdot \cos \beta_b}}$$

$$\rho_{H,C,B} = 1339 \text{ N/mm}^2$$

$$\rho_{H,D,B} = Z_E \cdot \sqrt{\frac{F_t \cdot X_D}{b \cdot \rho_{n,D} \cdot \cos \alpha_t \cdot \cos \beta_b}} \quad \rho_{H,D,B} = 1383 \text{ N/mm}^2$$

$$\rho_{H,DE,B} = Z_E \cdot \sqrt{\frac{F_t \cdot X_{DE}}{b \cdot \rho_{n,DE} \cdot \cos \alpha_t \cdot \cos \beta_b}} \quad \rho_{H,DE,B} = 1045 \text{ N/mm}^2$$

$$\rho_{H,E,B} = Z_E \cdot \sqrt{\frac{F_t \cdot X_E}{b \cdot \rho_{n,E} \cdot \cos \alpha_t \cdot \cos \beta_b}} \quad \rho_{H,E,B} = 963 \text{ N/mm}^2$$

$$\rho_{\text{dyn},A,B} = \rho_{H,A,B} \cdot \sqrt{K_A \cdot K_V \cdot K_{H\alpha} \cdot K_{H\beta}} \quad \rho_{\text{dyn},A,B} = 1084 \text{ N/mm}^2$$

$$\rho_{\text{dyn},AB,B} = \rho_{H,AB,B} \cdot \sqrt{K_A \cdot K_V \cdot K_{H\alpha} \cdot K_{H\beta}} \quad \rho_{\text{dyn},AB,B} = 1175 \text{ N/mm}^2$$

$$\rho_{\text{dyn},B,B} = \rho_{H,B,B} \cdot \sqrt{K_A \cdot K_V \cdot K_{H\alpha} \cdot K_{H\beta}} \quad \rho_{\text{dyn},B,B} = 1555 \text{ N/mm}^2$$

$$\rho_{\text{dyn},C,B} = \rho_{H,C,B} \cdot \sqrt{K_A \cdot K_V \cdot K_{H\alpha} \cdot K_{H\beta}} \quad \rho_{\text{dyn},C,B} = 1506 \text{ N/mm}^2$$

$$\rho_{\text{dyn},D,B} = \rho_{H,D,B} \cdot \sqrt{K_A \cdot K_V \cdot K_{H\alpha} \cdot K_{H\beta}} \quad \rho_{\text{dyn},D,B} = 1555 \text{ N/mm}^2$$

$$\rho_{\text{dyn},DE,B} = \rho_{H,DE,B} \cdot \sqrt{K_A \cdot K_V \cdot K_{H\alpha} \cdot K_{H\beta}} \quad \rho_{\text{dyn},DE,B} = 1175 \text{ N/mm}^2$$

$$\rho_{\text{dyn},E,B} = \rho_{H,E,B} \cdot \sqrt{K_A \cdot K_V \cdot K_{H\alpha} \cdot K_{H\beta}} \quad \rho_{\text{dyn},E,B} = 1084 \text{ N/mm}^2$$

velocity:

$$v_{r1,A} = 2 \cdot \pi \cdot \frac{n_1}{60} \cdot \frac{d_{w1}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{A1}^2 - d_{b1}^2}{d_{w1}^2 - d_{b1}^2}} \quad v_{r1,A} = 4,834 \text{ m/s}$$

$$v_{r1,AB} = 2 \cdot \pi \cdot \frac{n_1}{60} \cdot \frac{d_{w1}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{AB1}^2 - d_{b1}^2}{d_{w1}^2 - d_{b1}^2}} \quad v_{r1,AB} = 6,916 \text{ m/s}$$

$$v_{r1,B} = 2 \cdot \pi \cdot \frac{n_1}{60} \cdot \frac{d_{w1}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{B1}^2 - d_{b1}^2}{d_{w1}^2 - d_{b1}^2}} \quad v_{r1,B} = 8,998 \text{ m/s}$$

$$v_{r1,C} = 2 \cdot \pi \cdot \frac{n_1}{60} \cdot \frac{d_{w1}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{C1}^2 - d_{b1}^2}{d_{w1}^2 - d_{b1}^2}} \quad v_{r1,C} = 11,985 \text{ m/s}$$

$$v_{r1,D} = 2 \cdot \pi \cdot \frac{n_1}{60} \cdot \frac{d_{w1}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{D1}^2 - d_{b1}^2}{d_{w1}^2 - d_{b1}^2}} \quad v_{r1,D} = 14,971 \text{ m/s}$$

$$v_{r1,DE} = 2 \cdot \pi \cdot \frac{n_1}{60} \cdot \frac{d_{w1}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{DE1}^2 - d_{b1}^2}{d_{w1}^2 - d_{b1}^2}} \quad v_{r1,DE} = 17,053 \text{ m/s}$$

$$v_{r1,E} = 2 \cdot \pi \cdot \frac{n_1}{60} \cdot \frac{d_{w1}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{E1}^2 - d_{b1}^2}{d_{w1}^2 - d_{b1}^2}} \quad v_{r1,E} = 19,135 \text{ m/s}$$

$$v_{r2,A} = 2 \cdot \pi \cdot \frac{n_1}{60 \cdot u} \cdot \frac{d_{w2}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{A2}^2 - d_{b2}^2}{d_{w2}^2 - d_{b2}^2}} \quad v_{r2,A} = 19,135 \text{ m/s}$$

$$v_{r2,AB} = 2 \cdot \pi \cdot \frac{n_1}{60 \cdot u} \cdot \frac{d_{w2}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{AB2}^2 - d_{b2}^2}{d_{w2}^2 - d_{b2}^2}} \quad v_{r2,AB} = 17,053 \text{ m/s}$$

$$v_{r2,B} = 2 \cdot \pi \cdot \frac{n_1}{60 \cdot u} \cdot \frac{d_{w2}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{B2}^2 - d_{b2}^2}{d_{w2}^2 - d_{b2}^2}} \quad v_{r2,B} = 14,971 \text{ m/s}$$

$$v_{r2,C} = 2 \cdot \pi \cdot \frac{n_1}{60 \cdot u} \cdot \frac{d_{w2}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{C2}^2 - d_{b2}^2}{d_{w2}^2 - d_{b2}^2}} \quad v_{r2,C} = 11,985 \text{ m/s}$$

$$v_{r2,D} = 2 \cdot \pi \cdot \frac{n_1}{60 \cdot u} \cdot \frac{d_{w2}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{D2}^2 - d_{b2}^2}{d_{w2}^2 - d_{b2}^2}} \quad v_{r2,D} = 8,998 \text{ m/s}$$

$$v_{r2,DE} = 2 \cdot \pi \cdot \frac{n_1}{60 \cdot u} \cdot \frac{d_{w2}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{DE2}^2 - d_{b2}^2}{d_{w2}^2 - d_{b2}^2}} \quad v_{r2,DE} = 6,916 \text{ m/s}$$

$$v_{r2,E} = 2 \cdot \pi \cdot \frac{n_1}{60 \cdot u} \cdot \frac{d_{w2}}{2000} \cdot \sin \alpha_{wt} \cdot \sqrt{\frac{d_{E2}^2 - d_{b2}^2}{d_{w2}^2 - d_{b2}^2}} \quad v_{r2,E} = 4,834 \text{ m/s}$$

$$v_{g,A} = v_{r1,A} - v_{r2,A} \quad v_{g,A} = -14,300 \text{ m/s}$$

$$v_{g,AB} = v_{r1,AB} - v_{r2,AB} \quad v_{g,AB} = -10,137 \text{ m/s}$$

$$v_{g,B} = v_{r1,B} - v_{r2,B} \quad v_{g,B} = -5,974 \text{ m/s}$$

$$v_{g,C} = v_{r1,C} - v_{r2,C} \quad v_{g,C} = 0 \text{ m/s}$$

$$v_{g,D} = v_{r1,D} - v_{r2,D} \quad v_{g,D} = 5,974 \text{ m/s}$$

$$v_{g,DE} = v_{r1,DE} - v_{r2,DE} \quad v_{g,DE} = 10,137 \text{ m/s}$$

$$v_{g,E} = v_{r1,E} - v_{r2,E} \quad v_{g,E} = 14,300 \text{ m/s}$$

$$v_{\Sigma,A} = v_{r1,A} + v_{r2,A} \quad v_{\Sigma,A} = 23,969 \text{ m/s}$$

$$v_{\Sigma,AB} = v_{r1,AB} + v_{r2,AB} \quad v_{\Sigma,AB} = 23,969 \text{ m/s}$$

$$v_{\Sigma,B} = v_{r1,B} + v_{r2,B} \quad v_{\Sigma,B} = 23,969 \text{ m/s}$$

$$V_{\Sigma,C} = V_{r1,C} + V_{r2,C}$$

$$V_{\Sigma,C} = 23,969 \text{ m/s}$$

$$V_{\Sigma,D} = V_{r1,D} + V_{r2,D}$$

$$V_{\Sigma,D} = 23,969 \text{ m/s}$$

$$V_{\Sigma,DE} = V_{r1,DE} + V_{r2,DE}$$

$$V_{\Sigma,DE} = 23,969 \text{ m/s}$$

$$V_{\Sigma,E} = V_{r1,E} + V_{r2,E}$$

$$V_{\Sigma,E} = 23,969 \text{ m/s}$$

effective arithmetic mean roughness value:

$$Ra = 0,5 \cdot (Ra_1 + Ra_2)$$

$$Ra = 0,90 \text{ } \mu\text{m}$$

## B.2.4 Calculation of lubricant data

$$A = \frac{\log[\log(v_{40} + 0,7) / \log(v_{100} + 0,7)]}{\log(313/373)}$$

$$A = -3,385$$

$$B = \log[\log(v_{40} + 0,7)] - A \cdot \log(313)$$

$$B = 8,815$$

$$\log[\log(v_{\theta\text{oil}} + 0,7)] = A \cdot \log(\theta_{\text{oil}} + 273) + B$$

$$v_{\theta\text{oil}} = 24,825 \text{ mm}^2/\text{s}$$

$$\rho_{\theta\text{oil}} = \rho_{15} \cdot \left[ 1 - 0,7 \cdot \frac{(\theta_{\text{oil}} + 273) - 289}{\rho_{15}} \right]$$

$$\rho_{\theta\text{oil}} = 843,2 \text{ kg/m}^3$$

$$\eta_{\theta\text{oil}} = 10^{-6} \cdot v_{\text{oil}} \cdot \rho_{\text{oil}}$$

$$\eta_{\theta\text{oil}} = 0,021 \text{ N}\cdot\text{s/m}^2$$

$X_L = 1,0$  for mineral oil (see Table 3)

$$\log[\log(v_{38} + 0,7)] = A \cdot \log(38 + 273) + B$$

$$v_{38} = 236,242 \text{ mm}^2/\text{s}$$

$$\rho_{38} = \rho_{15} \cdot \left[ 1 - 0,7 \cdot \frac{(38 + 273) - 289}{\rho_{15}} \right]$$

$$\rho_{38} = 879,6 \text{ kg/m}^3$$

$$\eta_{38} = 10^{-6} \cdot v_{38} \cdot \rho_{38}$$

$$\eta_{38} = 0,208 \text{ N}\cdot\text{s/m}^2$$

$$\alpha_{38} = 2,657 \cdot 10^{-8} \cdot \eta_{38}^{0,1348}$$

$$\alpha_{38} = 2,15 \cdot 10^{-8} \text{ m}^2/\text{N}$$

$X_S = 1,2$  for injection lubrication

## B.2.5 Calculation of the material parameter

mean coefficient of friction:

$$X_R = 2,2 \cdot \left( \frac{Ra}{\rho_{n,C}} \right)^{0,25}$$

$$X_R = 1,025$$

$$K_{By} = 1,0 \quad \text{for } \varepsilon_y < 2$$

$$\mu_m = 0,045 \cdot \left( \frac{K_A \cdot K_v \cdot K_{H\alpha} \cdot K_{H\beta} \cdot F_{bt} \cdot K_{By}}{b \cdot v_{\Sigma,C} \cdot \rho_{n,C}} \right)^{0,2} \cdot (10^3 \cdot \eta_{oil})^{-0,05} \cdot X_R \cdot X_L \quad \mu_m = 0,048$$

bulk temperature:

$$H_v = (\varepsilon_1^2 + \varepsilon_2^2 + 1 - \varepsilon_\alpha) \cdot \left( \frac{1}{z_1} + \frac{1}{z_2} \right) \cdot \frac{\pi}{\cos \beta_b} \quad \text{for } \varepsilon_\alpha < 2 \quad H_v = 0,204$$

$$\varepsilon_{max} = \varepsilon_1 = \varepsilon_2$$

$$X_{Ca} = 1,0 \quad \text{for no profile modification}$$

$$\theta_M = \theta_{oil} + 7400 \cdot \left( \frac{P \cdot \mu_m \cdot H_v}{a \cdot b} \right)^{0,72} \cdot \frac{X_S}{1,2 \cdot X_{Ca}} \quad \theta_M = 153,6 \text{ }^\circ\text{C}$$

material parameter:

$$\log[\log(v_{\theta M} + 0,7)] = A \cdot \log(\theta_M + 273) + B \quad v_{\theta M} = 5,824 \text{ mm}^2/\text{s}$$

$$\rho_{\theta M} = \rho_{15} \cdot \left[ 1 - 0,7 \cdot \frac{(\theta_M + 273) - 289}{\rho_{15}} \right] \quad \rho_{\theta M} = 798,7 \text{ kg/m}^3$$

$$\eta_{\theta M} = 10^{-6} \cdot v_{\theta M} \cdot \rho_{\theta M} \quad \eta_{\theta M} = 0,005 \text{ N}\cdot\text{s/m}^2$$

$$\alpha_{\theta M} = \alpha_{38} \cdot \left[ 1 + 516 \cdot \left( \frac{1}{\theta_M + 273} - \frac{1}{311} \right) \right] \quad \alpha_{\theta M} = 1,183 \cdot 10^{-8} \text{ m}^2/\text{N}$$

$$G_M = 10^6 \cdot \alpha_{\theta M} \cdot E_r \quad G_M = 2678,6$$

### B.2.6 Calculation of the velocity parameter

$$U_A = \eta_{\theta M} \cdot \frac{v_{\Sigma,A}}{2000 \cdot E_r \cdot \rho_{n,A}} \quad U_A = 2,005 \cdot 10^{-11}$$

$$U_{AB} = \eta_{\theta M} \cdot \frac{v_{\Sigma,AB}}{2000 \cdot E_r \cdot \rho_{n,AB}} \quad U_{AB} = 1,572 \cdot 10^{-11}$$

$$U_B = \eta_{\theta M} \cdot \frac{v_{\Sigma,B}}{2000 \cdot E_r \cdot \rho_{n,B}} \quad U_B = 1,377 \cdot 10^{-11}$$

$$U_C = \eta_{\theta M} \cdot \frac{v_{\Sigma,C}}{2000 \cdot E_r \cdot \rho_{n,C}} \quad U_C = 1,291 \cdot 10^{-11}$$

$$U_D = \eta_{\theta M} \cdot \frac{V_{\Sigma,D}}{2000 \cdot E_r \cdot \rho_{n,D}} \quad U_D = 1,377 \cdot 10^{-11}$$

$$U_{DE} = \eta_{\theta M} \cdot \frac{V_{\Sigma,DE}}{2000 \cdot E_r \cdot \rho_{n,DE}} \quad U_{DE} = 1,572 \cdot 10^{-11}$$

$$U_E = \eta_{\theta M} \cdot \frac{V_{\Sigma,E}}{2000 \cdot E_r \cdot \rho_{n,E}} \quad U_E = 2,005 \cdot 10^{-11}$$

### B.2.7 Calculation of the load parameter

$$W_A = \frac{\rho_{\text{dyn},A}^2 \cdot 2 \cdot \pi}{E_r^2} \quad W_A = 1,439 \cdot 10^{-4}$$

$$W_{AB} = \frac{\rho_{\text{dyn},AB}^2 \cdot 2 \cdot \pi}{E_r^2} \quad W_{AB} = 1,694 \cdot 10^{-4}$$

$$W_B = \frac{\rho_{\text{dyn},B}^2 \cdot 2 \cdot \pi}{E_r^2} \quad W_B = 2,966 \cdot 10^{-4}$$

$$W_C = \frac{\rho_{\text{dyn},C}^2 \cdot 2 \cdot \pi}{E_r^2} \quad W_C = 2,781 \cdot 10^{-4}$$

$$W_D = \frac{\rho_{\text{dyn},D}^2 \cdot 2 \cdot \pi}{E_r^2} \quad W_D = 2,966 \cdot 10^{-4}$$

$$W_{DE} = \frac{\rho_{\text{dyn},DE}^2 \cdot 2 \cdot \pi}{E_r^2} \quad W_{DE} = 1,694 \cdot 10^{-4}$$

$$W_E = \frac{\rho_{\text{dyn},E}^2 \cdot 2 \cdot \pi}{E_r^2} \quad W_E = 1,439 \cdot 10^{-4}$$

### B.2.8 Calculation of the sliding parameter

local flash temperature:

$$\theta_{fl,A} = \frac{\sqrt{\pi}}{2} \cdot \frac{10^6 \cdot \mu_m \cdot \rho_{\text{dyn},A} \cdot |v_{g,A}|}{B_{M1} \sqrt{v_{r1,A}} + B_{M2} \sqrt{v_{r2,A}}} \cdot \sqrt{8 \cdot \rho_{n,A} \cdot \frac{\rho_{\text{dyn},A}}{1000 \cdot E_r}} \quad \theta_{fl,A} = 175,3 \text{ } ^\circ\text{C}$$

$$\theta_{fl,AB} = \frac{\sqrt{\pi}}{2} \cdot \frac{10^6 \cdot \mu_m \cdot \rho_{\text{dyn},AB} \cdot |v_{g,AB}|}{B_{M1} \sqrt{v_{r1,AB}} + B_{M2} \sqrt{v_{r2,AB}}} \cdot \sqrt{8 \cdot \rho_{n,AB} \cdot \frac{\rho_{\text{dyn},AB}}{1000 \cdot E_r}} \quad \theta_{fl,AB} = 154,1 \text{ } ^\circ\text{C}$$