INTERNATIONAL STANDARD

ISO/IEC 24707

Second edition
2018-07

Information technology — Common Logic (CL) — A framework for a family of logic-based languages

Technologies de l'information — Logique Commune (CL) — Cadre pour une famille des langages logique-basés

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Foreword

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The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular the different approval criteria needed for the different types of ISO documents should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2 (see www.iso.org/directives).

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For an explanation on the voluntary nature of standards, the meaning of ISO specific terms and expressions related to conformity assessment, as well as information about ISO's adherence to the World Trade Organization (WTO) principles in the Technical Barriers to Trade (TBT) see the following URL: www.iso.org/iso/foreword.html.

This document was prepared by Technical Committee ISO/IEC JTC 1, *Information technology*, SC 32, *Data management and interchange.*

This second edition cancels and replaces the first edition (ISO/IEC 24707:2007), which has been technically revised.

The main changes compared to the previous edition are as follows:

— the list of syntactic errors that have already been identified in the Defect Report has been fixed;

— the XML syntax in Annex C has been corrected and completed;

— a more general approach to annotation of CL-texts has been made;

— semantics has been modified to allow the existence of definitional extensions in CL;

— support for circular imports;

— semantics of CL-module have been clarified;

— clarification of the distinction between segregated and non-segregated dialects;

— clarification of conformance conditions has been made.

Any feedback or questions on this document should be directed to the user's national standards body. A complete listing of these bodies can be found at www.iso.org/members.html.

Introduction

Common Logic is a logic framework intended for information exchange and transmission. The framework allows for a variety of different syntactic forms, called dialects, all translatable by a semantics-preserving transformation to a common XML-based syntax.

Common Logic has some novel features, chief among them being a syntax which permits "higher-order" constructions, such as quantification over classes or relations while preserving a first-order model theory, and a semantics which allows theories to describe intentional entities such as classes or properties. It also has provision for the use of datatypes and for naming, importing and transmitting content on the World Wide Web using XML.

Information technology — Common Logic (CL) — A framework for a family of logic-based languages

1 Scope

This document specifies a family of logic languages designed for use in the representation and interchange of information and data among disparate computer systems.

The following features are essential to the design of this document.

— Languages in the family have declarative semantics. It is possible to understand the meaning of expressions in these languages without appeal to an interpreter for manipulating those expressions.

— Languages in the family are logically comprehensive – at its most general, they provide for the expression of arbitrary first-order logical sentences.

— Languages in the family are translatable by a semantics-preserving transformation to a common XML-based syntax, facilitating interchange of information among heterogeneous computer systems.

The following are within the scope of this document:

— representation of information in ontologies and knowledge bases;

— specification of expressions that are the input or output of inference engines;

— formal interpretations of the symbols in the language.

The following are outside the scope of this document:

— specification of proof theory or inference rules;

— specification of translators between the notations of heterogeneous computer systems;

— computer-based operational methods of providing relationships between symbols in the logical "universe of discourse" and individuals in the "real world".

This document describes Common Logic's syntax and semantics.

This document defines an abstract syntax and an associated model-theoretic semantics for a specific extension of first-order logic. The intent is that the content of any system using first-order logic can be represented in this document. The purpose is to facilitate interchange of first-order logic-based information between systems.

Issues relating to computability using this document (including efficiency, optimization, etc.) are not addressed.

2 Normative references

The following documents are referred to in the text in such a way that some or all of their content constitutes requirements of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO/IEC 2382:2015, *Information technology — Vocabulary*

ISO/IEC 10646:2014, *Information technology — Universal Coded Character Set (UCS)*

ISO/IEC 14977:1996, *Information technology — Syntactic metalanguage — Extended BNF*

3   Terms and definitions

For the purposes of this document, the following terms and definitions apply.

ISO and IEC maintain terminological databases for use in standardization at the following addresses:

— IEC Electropedia: available at http://www.electropedia.org/

— ISO Online browsing platform: available at https://www.iso.org/obp

3.1
axiom
any *sentence* (3.15), statement or text which is assumed to be true, or from which others are derived, or by which they are entailed

Note 1 to entry: In a computational setting, an axiom is a sentence which is never posed as a goal to be proved, but only used to prove other sentences.

3.2
conceptual graph
CG
graphical or textual display of symbols arranged according to the style of *conceptual graph theory* (3.3)

3.3
conceptual graph theory
form of first-order logic which represents existential quantification and conjunction via the assertion of logical constructs called concepts and relations which are arranged in an abstract or visually displayed graph

3.4
CLIF
text-based first-order formalism using a LISP-like list notation

Note 1 to entry: This is one of the concrete syntaxes for Common Logic (described in Annex A).

Note 2 to entry: CLIF is a KIF-based syntax that is used for illustration purposes in this document. KIF, introduced by Mike Genesereth[3], originated with the Knowledge Sharing Effort sponsored by the U.S. DARPA. The name "KIF" is not used for this syntax in order to distinguish it from the commonly used KIF dialects. No assumptions are made in this document with respect to KIF semantics; in particular, no equivalence between CLIF and KIF is intended.

Note 3 to entry: Historically, CLIF was an acronym for Common Logic Interchange Format. However, CLIF does not hold a privileged position among *Common Logic dialects* (3.7), as the expanded name suggests. Further, XCL is the recommended interchange format on the Web.

3.5
Conceptual Graph Interchange Format
CGIF
text version of *conceptual graphs* (3.2)

Note 1 to entry: Sometimes, this may refer to an example of a character string that conforms to Annex B, intended to convey exactly the same structure and semantics as an equivalent conceptual graph.

3.6
denotation
relationship holding between a name or expression and the thing to which it refers

Note 1 to entry: Also used with "of" to mean the thing being named, i.e. the referent of a name or expression.

3.7
Common Logic dialect
concrete instance of Common Logic syntax that shares (at least some of) the uniform semantics of Common Logic

Note 1 to entry: A dialect may be textual or graphical or possibly some other form. A dialect, by definition, is also a conforming language (see 7.1 for further details).

3.8
eXtensible Common Logic Markup Language
XCL
XML-based syntax for Common Logic

3.9
individual
<of an interpretation> one element of the *universe of discourse* (3.17) of an *interpretation* (3.12)

Note 1 to entry: The universe of discourse of an interpretation is the set of all of its individuals.

3.10
internationalized resource identifier
IRI
string of Unicode characters intended for use as an Internet network identifier syntax which can accommodate a wide variety of international character forms

3.11
inscription
structure of symbols that may be either linear or graphic

3.12
interpretation
formal specification of the meanings of the names in a vocabulary of a *Common Logic dialect* (3.7) in terms of a *universe of reference* (3.18)

Note 1 to entry: A Common Logic interpretation, in turn, determines the semantic values of all complex expressions of the dialect, in particular, the truth values of its *sentences* (3.15), statements and texts.

Note 2 to entry: See 6.2 for a more precise description of how an interpretation is defined.

3.13
operator
distinguished syntactic role played by a specified component within a functional *term* (3.16)

Note 1 to entry: The *denotation* (3.6) of a functional term in an *interpretation* (3.12) is determined by the functional extension of the denotation of the operator together with the denotations of the arguments.

3.14
predicate
<Common Logic> distinguished syntactic role played by exactly one component within a simple *sentence* (3.15)

Note 1 to entry: The truth value of a simple sentence in an *interpretation* (3.12) is determined by the relational extension of the *denotation* (3.6) of the predicate together with the denotations of the arguments.

3.15
sentence
<Common Logic> expression in the syntactic form of a traditional first-order logical formula

EXAMPLE   A simple sentence (see 6.1.1.15), Boolean sentence (see 6.1.1.14) or quantification (see 6.1.1.13).

3.16
term
<Common Logic> expression which denotes an *individual* ([3.9](#)), consisting of either a name or, recursively, a functional term applied to a sequence of arguments, which are themselves terms

Note 1 to entry: Languages for traditional first-order logic specifically exclude *predicate* ([3.14](#)) quantifiers and the use of the same name in both predicate and argument position in simple *sentences* ([3.15](#)), both of which are permitted (though not required) in Common Logic. Languages for traditional first-order logic fall within the category of presupposing CL dialect, with a discourse presupposition of "non-discourse" for all names used as function *operators* ([3.13](#)) or predicates, and "discourse" for all names used as the arguments of functional terms or simple sentences or as bindings.

3.17
universe of discourse
domain of discourse
set of all the *individuals* ([3.9](#)) in an *interpretation* ([3.12](#)), i.e. the set over which the quantifiers range

Note 1 to entry: Required to be a subset of the *universe of reference* ([3.18](#)) and may be identical to it.

3.18
universe of reference
set of all the things needed to define the meanings of logical expressions in an *interpretation* ([3.12](#))

Note 1 to entry: Required to be a superset of the *universe of discourse* ([3.17](#)) and may be identical to it.

4   Symbols and abbreviated terms

4.1   Symbols

fun$_I$	mapping from UR$_I$ to functions from UD$_I$* to UD$_I$
I	interpretation in the model-theoretic sense
int$_I$	mapping from names in a vocabulary V to UR$_I$; informally, a means of associating names in V to referents in UR$_I$
rel$_I$	mapping from UR$_I$ to subsets of UD$_I$*
seq$_I$	mapping from sequence markers in V to UD$_I$*
λ	lexicon, which consists of a vocabulary, a set of sequence markers (Smark), and a set of titles (Ttl)
V	vocabulary, which is a set of names
Smark	set of sequence markers
Ttl	set of titles
UD$_I$	universe of discourse; a non-empty set of individuals that an interpretation *I* is "about" and over which the quantifiers are understood to range
UR$_I$	universe of reference, i.e. the set of all referents of names in an interpretation *I*
X*	set of finite sequences of the elements of X, for any set X. Thus, X* = {<x$_1$,...,x$_n$> | x$_1$,...,x$_n$ ∈ X}, for any *n* ≥ 0. Note that the empty sequence is in X*, for any X.

4.2 Abbreviated terms

CL Common Logic

DF display form

EBNF Extended Backus-Naur Format (as in ISO/IEC 14977)

FO first-order

KIF Knowledge Interchange Format

OWL Web Ontology Language

RDF Resource Description Framework

RDFS Resource Description Framework Schema

TFOL traditional first-order logic

XML eXtensible Markup Language

5 Requirements and design overview

5.1 Requirements

5.1.1 Common Logic should include full first-order logic with equality

Common Logic abstract syntax and semantics shall provide for the full range of first-order syntactic forms with their usual meanings. Any traditional first-order syntax will be directly translatable into Common Logic without loss of information or alteration of meaning.

5.1.2 Common Logic should provide a general-purpose syntax for communicating logical expressions

a) There should be a single XML syntax for communicating Common Logic content on the Web.

b) Common Logic languages should be able to express various commonly used "syntactic sugarings" for logical forms or commonly used patterns of logical sentences.

c) The Common Logic abstract syntax should relate to existing conventions; in particular, it should be capable of rendering any content expressible in RDF, RDFS or OWL.

d) There should be at least one human-readable presentation syntax defined which can be used to express the entire language.

5.1.3 Common Logic should be easy and natural for use on the Web

a) The XML syntax should be compatible with the published specifications for XML, IRI syntax, XML Schema, Unicode and other conventions relevant to transmission of information on the Web.

b) IRIs should be usable as names in the language.

c) IRIs should be usable to title texts and label expressions, in order to facilitate Web operations such as retrieval, importation and cross-reference.

5.1.4   Common Logic should support open networks

a)   Transmission of content between Common Logic-aware agents should not require negotiation about syntactic roles of symbols or translations between syntactic roles.

b)   Any piece of Common Logic text should have the same meaning, and support the same entailments, everywhere on the network. Every name should have the same logical meaning at every node of the network.

c)   No agent should be able to limit the ability of another agent to refer to anything or to make assertions about anything.

d)   The language should support ways to refer to a local universe of discourse and be able to relate it to other such universes.

e)   Users of Common Logic should be free to invent new names and use them in published Common Logic content.

5.1.5   Common Logic should not make arbitrary assumptions about semantics

a)   Common Logic does not make gratuitous or arbitrary assumptions about logical relationships between different expressions.

b)   If possible, Common Logic agents should express these assumptions in Common Logic directly.

5.2   A family of languages

This subclause describes what is meant by a "family" of languages and gives some of the rationale behind the development of Common Logic.

Following the convention whereby any language has a grammar, then Common Logic is a family of languages rather than a single language. Different Common Logic languages, referred to in this document as dialects, may differ sharply in their surface syntax, but they have a single uniform semantics and can all be transcribed into the common abstract syntax. Membership in the family is defined by being inter-translatable with the other dialects while preserving meaning, rather than by having any particular syntactic form. Several existing logical notations and languages, therefore, can be considered to be Common Logic dialects.

A Common Logic dialect called CLIF based on KIF (see Annex A) is used in giving examples throughout this document. CLIF can be considered an updated and simplified form of KIF 3.0[3] and hence a separate language in its own right. Conceptual graphs[1] are also a well-known form of first-order logic for machine processing; the CGIF language is specified in Annex B. An exactly conformant XML Dialect, called XCL, is specified in Annex C, for the purpose of satisfying requirements 5.1.2 a) and 5.1.3 a).

6   Common Logic abstract syntax and semantics

6.1   Common Logic abstract syntax

6.1.1   Abstract syntax categories

6.1.1.1   Terms, sequence markers, sentences, statements and texts are well-formed expressions.

6.1.1.2   A text is a text construction, domain restriction, or importation.

6.1.1.3   A text construction contains a set, list or bag of sentences, statements and/or texts. A Common Logic text may be a sequence, a set or a bag of sentences, statements and/or texts; dialects may specify which is intended or leave this undefined. Re-orderings and repetitions of arguments of a text

construction are semantically irrelevant. However, applications which transmit or re-publish Common Logic text shall preserve the structure of text constructions, since other applications are allowed to utilize the structure for other purposes, such as indexing. If a dialect imposes conditions on text constructions, then these conditions shall be preserved by conforming applications. A text construction may be empty.

6.1.1.4   A <u>domain restriction</u> consists of a term and a text called the <u>*body text*</u>. The term indicates the "local" universe of discourse in which the text is understood.

6.1.1.5   An <u>importation</u> contains a title. The intention is that the title provides an identifier to an external Common Logic text, and that the importation re-asserts that external text in the importing text.

6.1.1.6   An axiom is a statement, sentence or text.

6.1.1.7   A <u>statement</u> is either a <u>discourse statement or a titling</u>.

6.1.1.8   A discourse statement is either an out-of-discourse statement or an in-discourse statement.

6.1.1.9   An out-of-discourse statement contains a sequence of terms.

6.1.1.10 An in-discourse statement contains a sequence of terms.

6.1.1.11 A <u>titling</u> contains a name and a text. The titling assigns a title to a text. Titles are often IRIs, which identify the text as resource.

6.1.1.12 A <u>sentence</u> is either a quantified sentence or a Boolean sentence or a simple sentence.

6.1.1.13 A <u>quantified sentence</u> has (i) a type, called a *quantifier*, (ii) a finite, nonrepeating sequence of interpretable names called the *binding sequence*, each element of which is called a *binding* of the quantified sentence, and (iii) a sentence called the *body* of the quantified sentence. The abstract syntax distinguishes the *universal* and the *existential* types of quantified sentence. A name which occurs in the binding sequence is said to be *bound in* the body. Any name or sequence marker which is not bound in the body is said to be *free in* the body.

6.1.1.14 A <u>Boolean sentence</u> has a type, called a *connective*, and a number of sentences called the *components* of the Boolean sentence. The number depends on the particular type. The abstract syntax distinguishes five types of Boolean sentences: *conjunctions* and *disjunctions,* which have any number of components, *implications* and *biconditionals*, which have exactly two components, and *negations*, which have exactly one component. The two components of an implication fill different roles; one is the antecedent and the other is the consequent.

6.1.1.15 A <u>simple sentence</u> is either an <u>*equation*</u> containing two *arguments*, which are terms, or is an <u>atomic sentence</u>, which consists of a term, called the *predicate*, and a term sequence called the *argument sequence*, the elements of which are called *arguments* of the atomic sentence.

6.1.1.16 A <u>term</u> is either a name or a functional term. A term may have an attached comment. Further, every name is a term.

6.1.1.17 A <u>functional term</u> consists of a term, called the *operator*, and a term sequence called the *argument sequence*, the elements of which are called *arguments* of the functional term.

6.1.1.18 A <u>term sequence</u> is a finite sequence of terms and/or sequence markers. Term sequences may be empty, but a functional term with an empty argument sequence shall not be identified with its operator, and an atomic sentence with an empty argument sequence shall not be identified with its predicate.

6.1.1.19 A *lexicon* is a set of names (i.e. the vocabulary of the lexicon), a set of sequence markers, and a set of titles.

6.1.1.20 Irregular sentences in a concrete syntax are parsed into the abstract syntax as propositions (i.e. nullary atomic sentences) with a new name for the predicate. In this way, irregular sentences can be nested within texts, statement and (otherwise) regular compound sentences, and the semantics of the resulting expressions is determined as usual from Table 2.

6.1.1.21 A <u>comment</u> is a piece of data. Any number of comments may be attached to well-formed expressions that are texts, statements, sentences or functional terms, but not to names, sequence markers or other comments. No particular restrictions are placed on the nature of Common Logic comments; in particular, a comment may be Common Logic text. Particular dialects may impose conditions on the form of comments.

6.1 completely describes the abstract syntactic structure of Common Logic. Any fully conformant Common Logic dialect **shall** provide an unambiguous syntactic representation for each of the above types of well-formed expressions.

Sentence types are commonly indicated by the inclusion of explicit text strings, such as "forall" for universal sentence and "and" for conjunction. However, no conditions are imposed on how the various syntactic categories are represented in the surface forms of a dialect. In particular, expressions in a dialect are not required to consist of character strings.

6.1.2 Metamodel of the Common Logic abstract syntax

6.1.2.1 Names and sequence markers

The class of names and sequence markers of a Common Logic language is the classes obtained from strings using the following operators:

— *Voc* : *String → V*

— *Seqmark* : *String → Smark*

— *Titling* : *String → Ttl*

— *Binder = V ∪ Smark*

6.1.2.2 Terms and term sequences

The class of terms of a Common Logic language is the class Term that includes all names in V and all functional terms. The class of functional terms of a Common Logic language is the class FunctionalTerm obtained by the recursive application of the operator *Func* to pairs made up of one term and one term sequence. The class of term sequences of a Common Logic language is the class TermSequence that includes all finite sequences of terms and/or sequence markers.

— *Func:Term × TermSequence → FunctionalTerm*

— *Term = V ∪ FunctionalTerm*

— *TSeq:*(*Term ∪ Smark*) × … × (*Term ∪ Smark*) → *TermSequence*

6.1.2.3 Sentences

The class of sentences of a Common Logic language is the class Sentence that includes all simple sentences (including equations, if applicable) formed by the application of the operation(s) Atomic (and Id) from well-formed terms and term sequences and all compound sentences formed by the recursive

application of the set of operations Neg, Conj, Disj, Cond, BiCond, EQuant, and UQuant that satisfy the following conditions:

— each operation is one-to-one;

— the range of the operations is pairwise disjoint and disjoint from the set of terms of λ.

— *Atomic*:*Term × TermSequence → Sentence*

— *Id*:*Term × Term → Sentence*

— *Neg*:*Sentence → Sentence*

— *Conj* : *Sentence × ... × Sentence → Sentence*

— *Disj* : *Sentence × ... × Sentence → Sentence*

— *Cond* : *Sentence × Sentence → Sentence*

— *BiCond*:*Sentence × Sentence → Sentence*

— *EQuant*:*Binder × ... × Binder × Sentence → Sentence*, $n \geq 0$

— *UQuant*:*Binder × ... × Binder × Sentence → Sentence*, $n \geq 0$
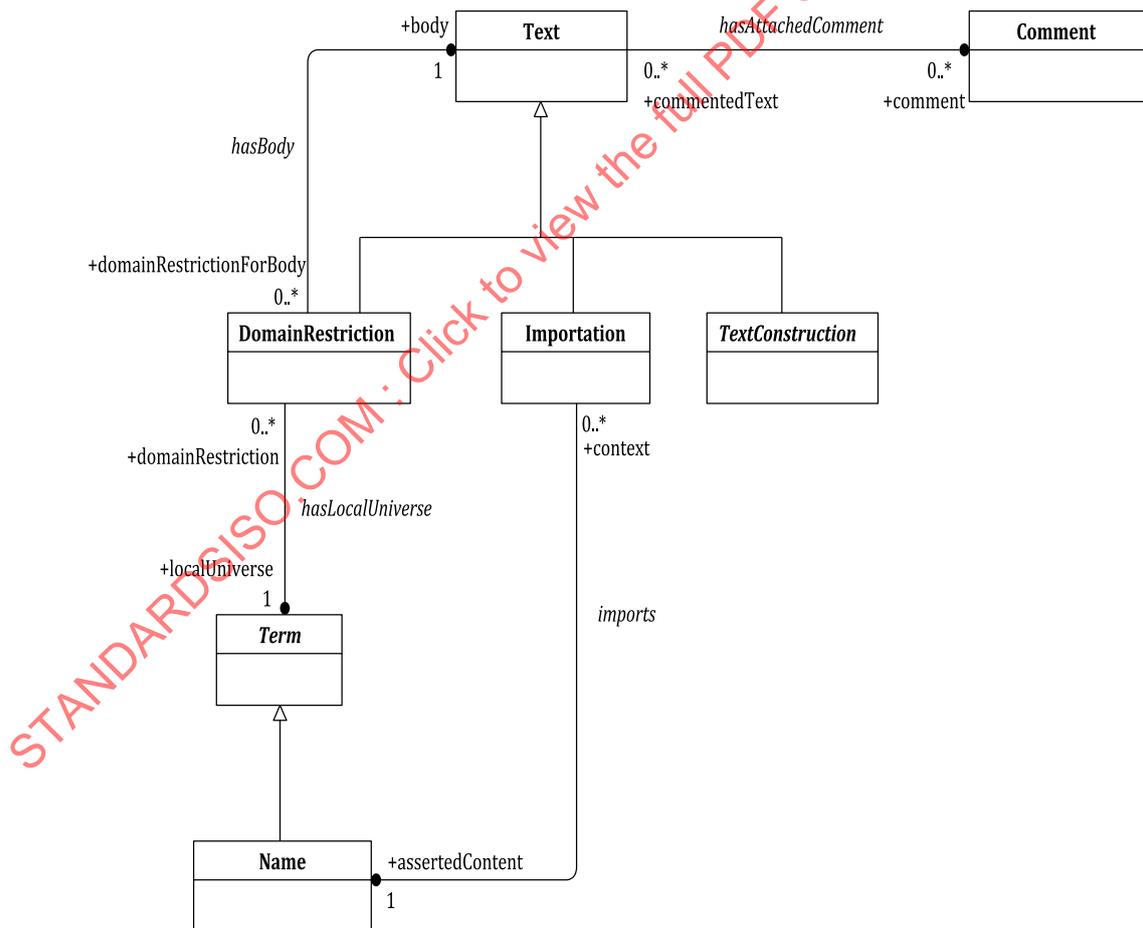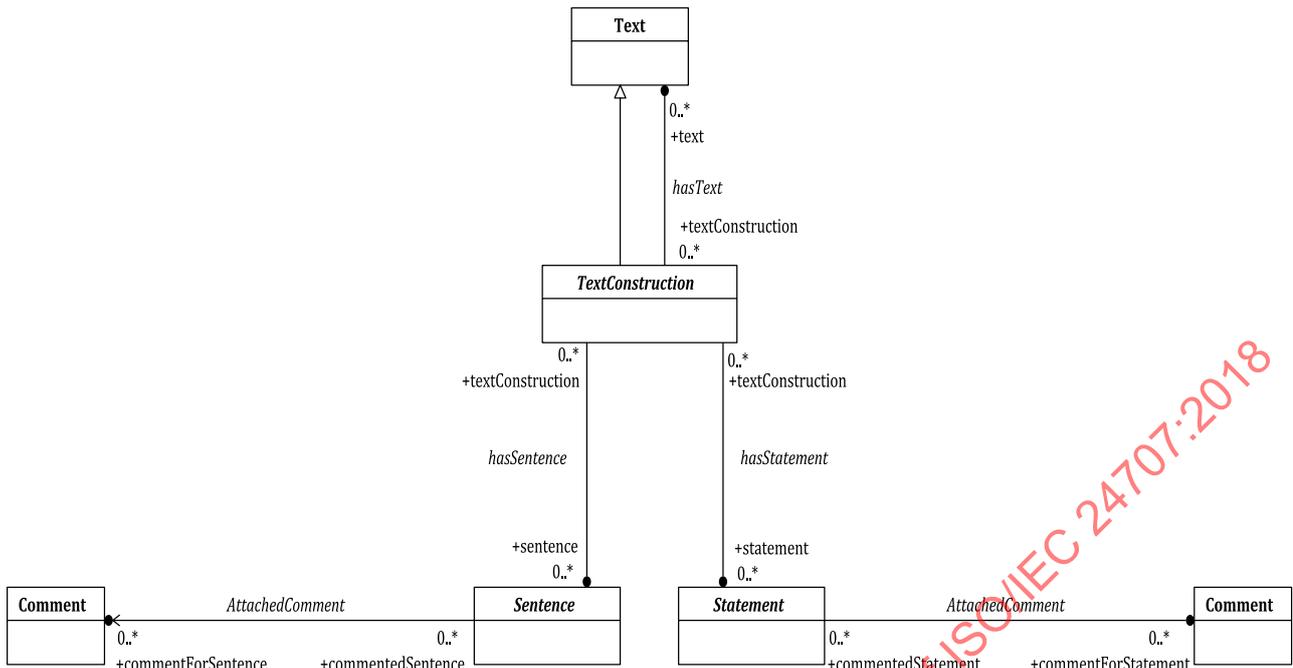

Figure 1 — Abstract syntax of texts

Figure 2 — Abstract syntax of text constructions
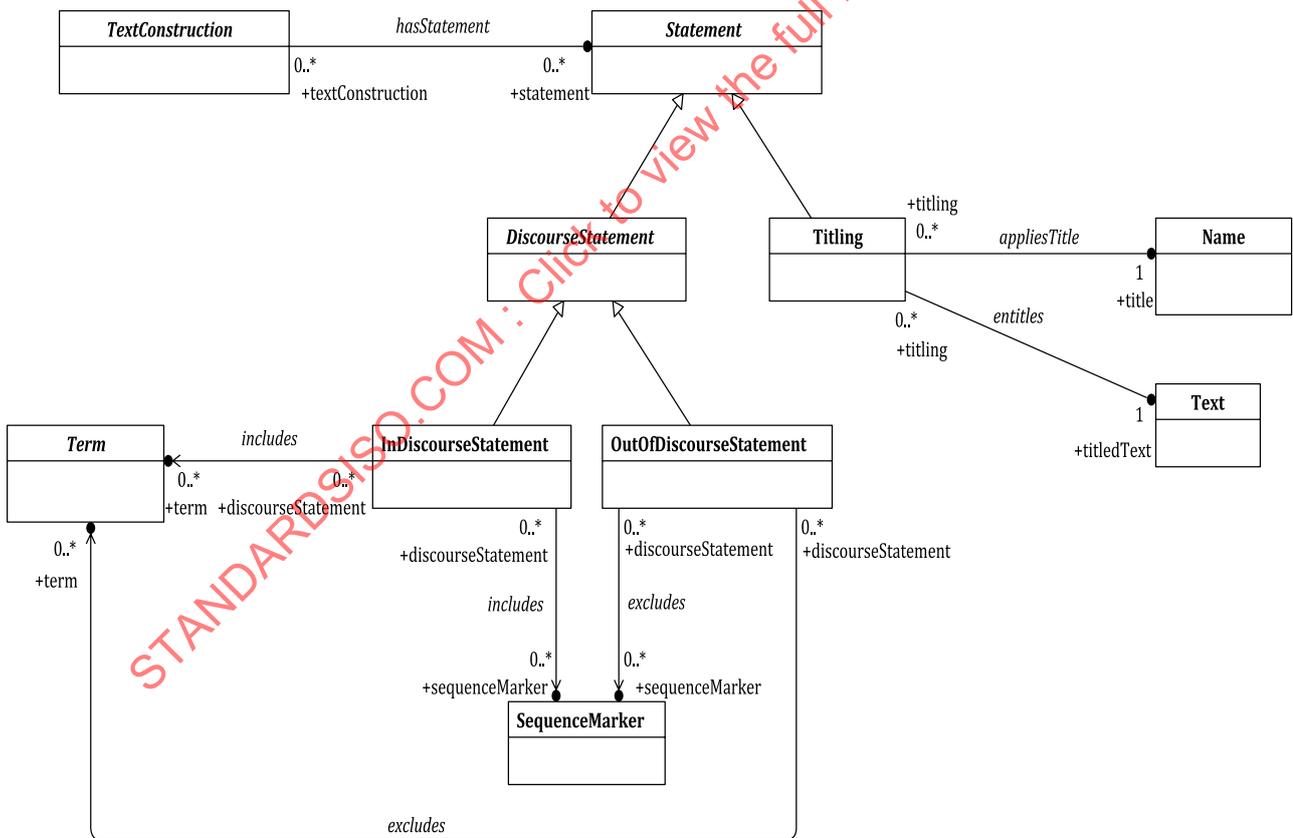
Figure 3 — Abstract syntax of statements
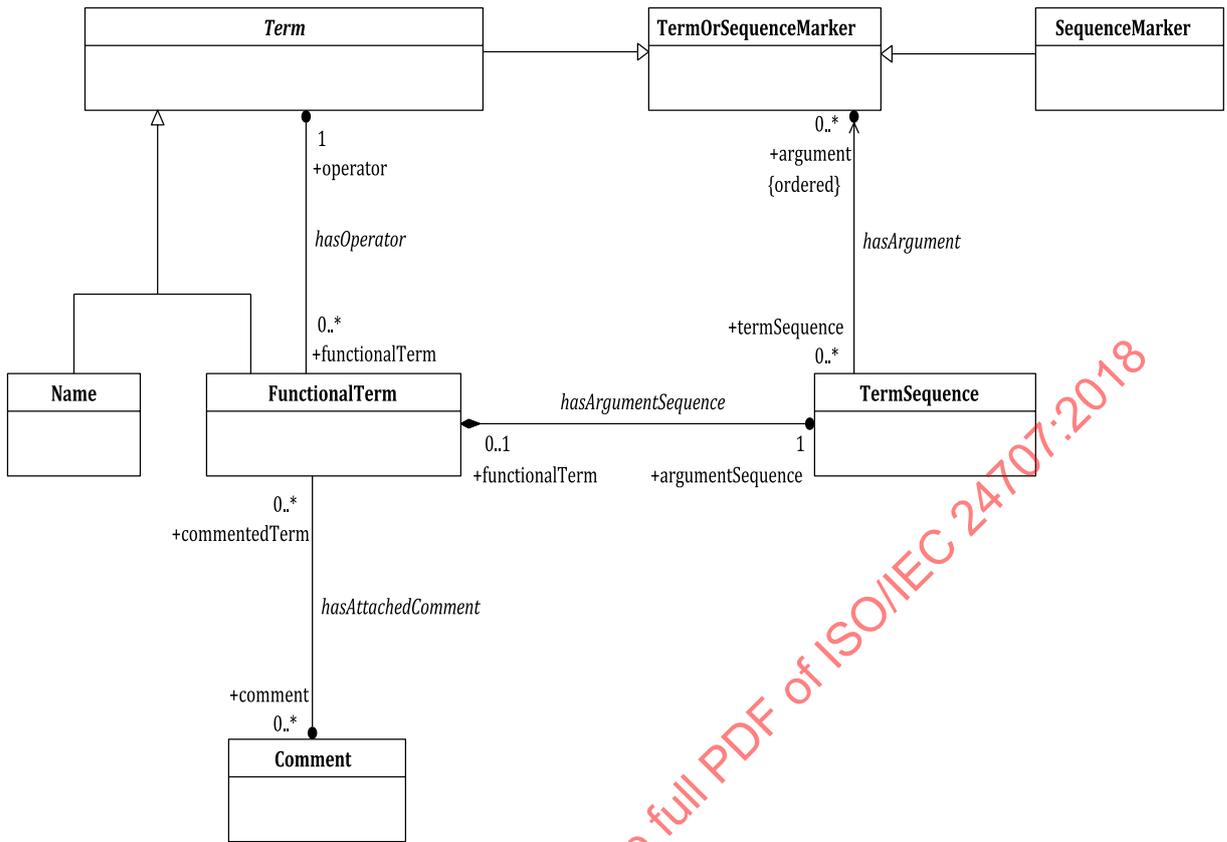
Figure 4 — Abstract syntax of terms
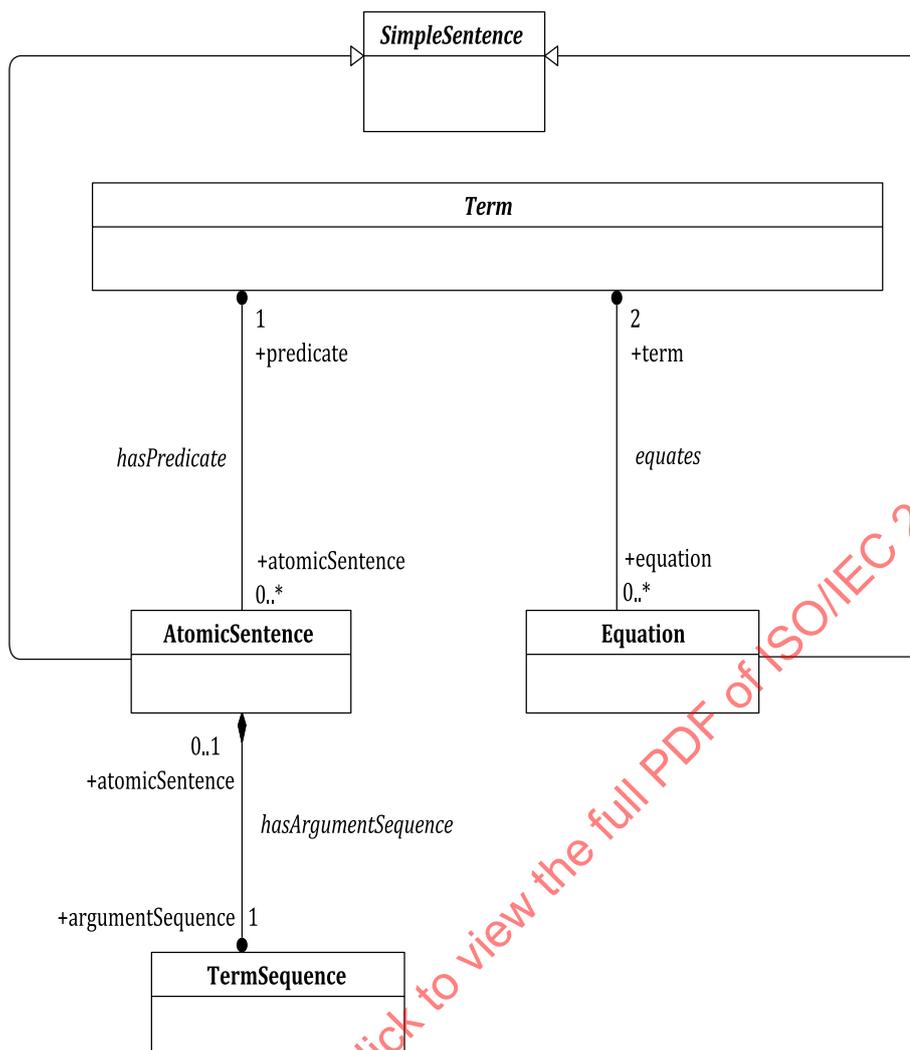
Figure 5 — Abstract syntax of a simple sentence
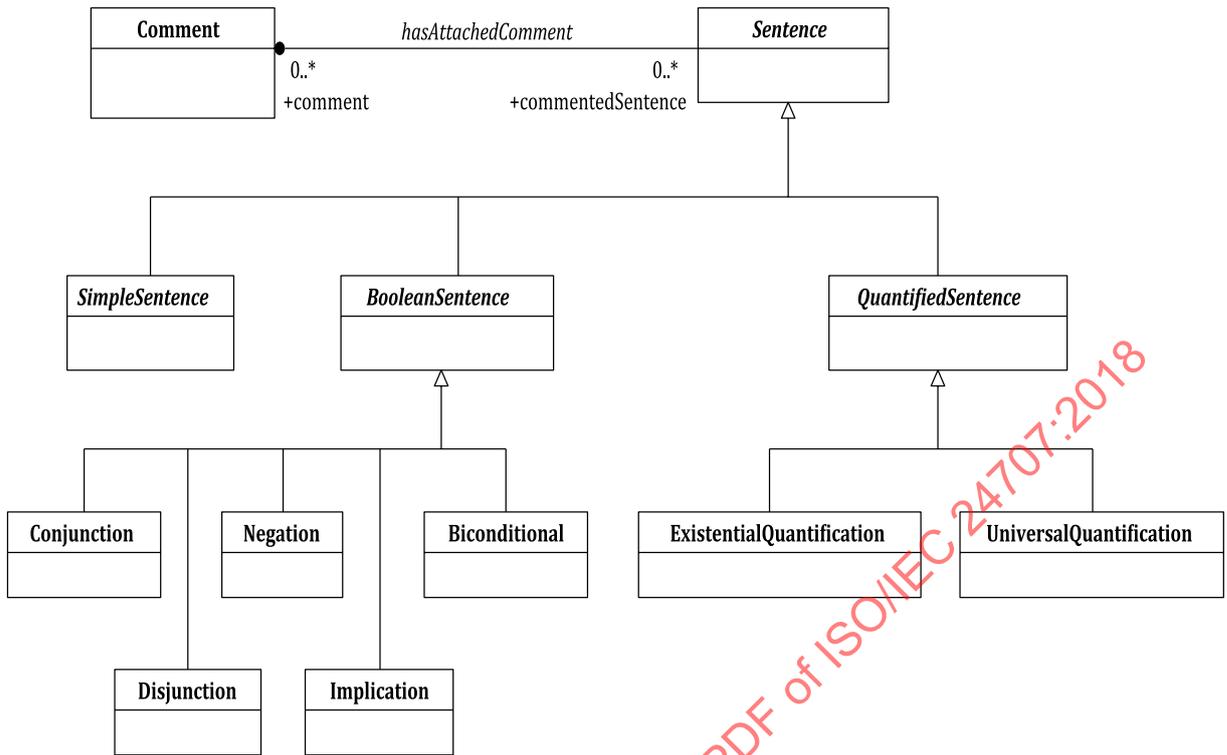
Figure 6 — Abstract syntax of sentences
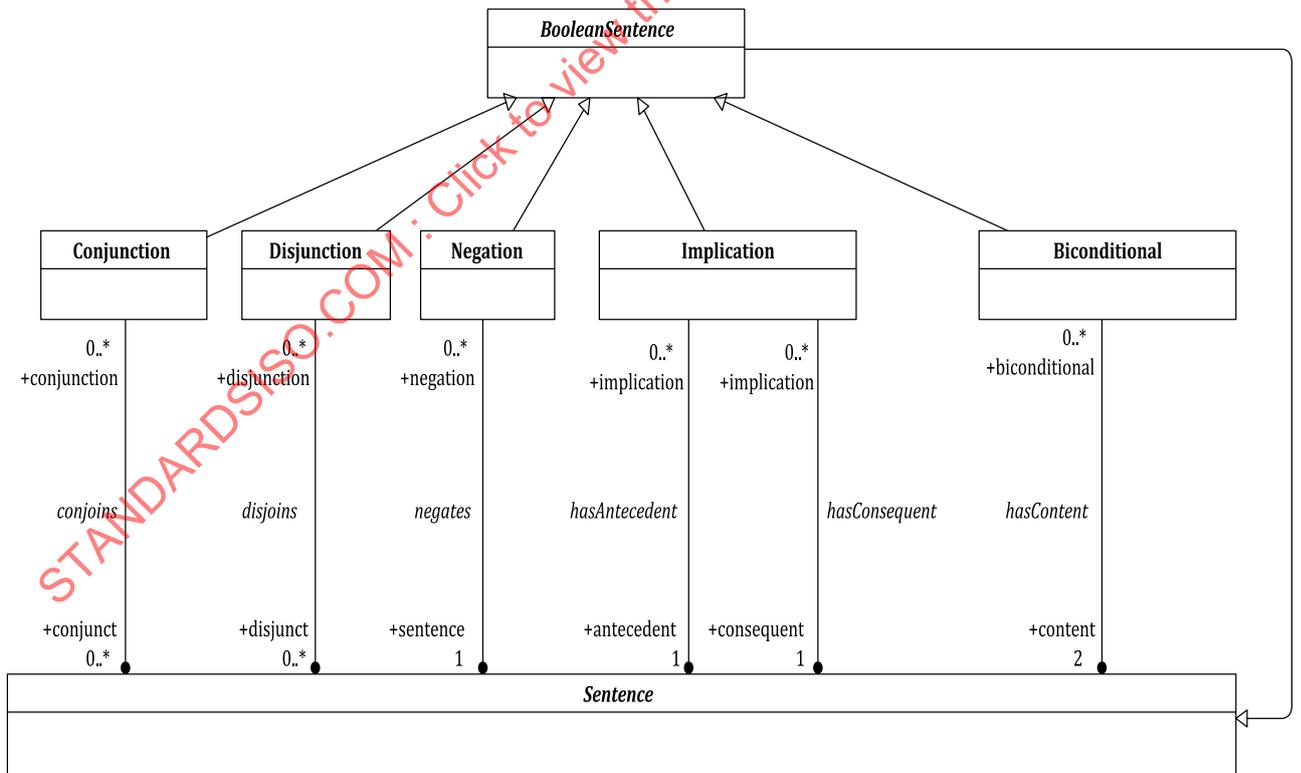
Figure 7 — Abstract syntax of Boolean sentences
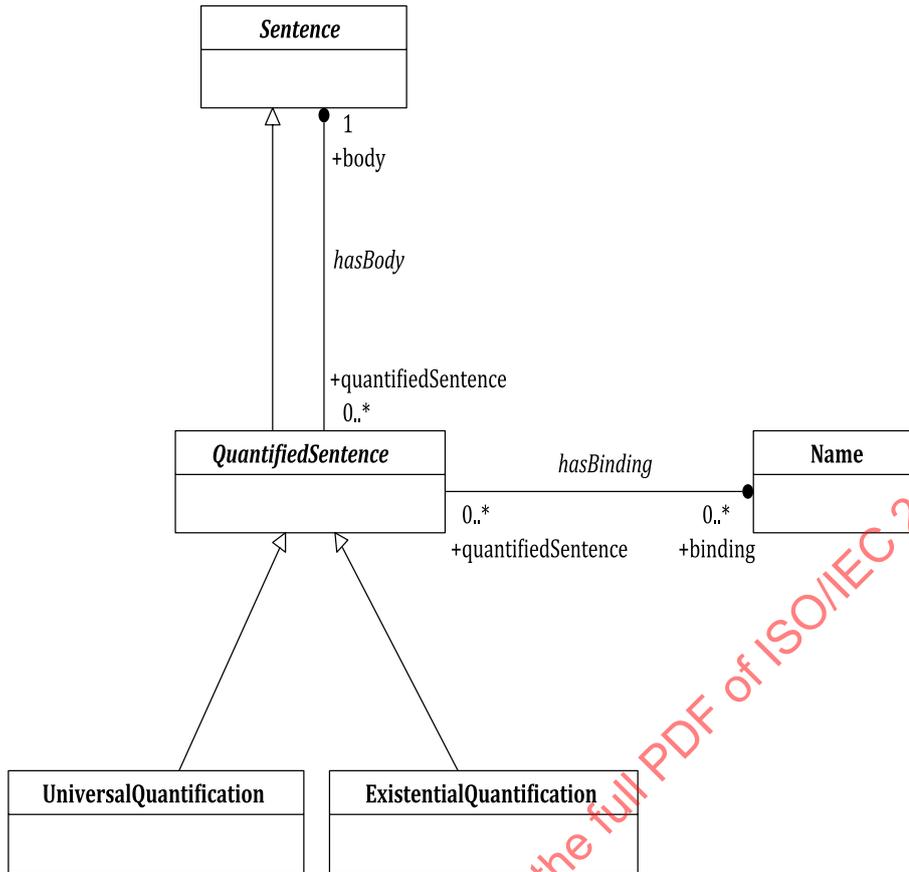
Figure 8 — Abstract syntax of a quantified sentence

6.1.2.4   Statements

The class of statements of a Common Logic language is the class Statement obtained from the recursive application of operations *outDiscourse*, *inDiscourse*, and *title* under the following conditions:

— *outDiscourse*:*TermSequence* → *DiscourseStatement*

— *inDiscourse*:*TermSequence* → *DiscourseStatement*

— *title*:Ttl × *Text* → *Titling*

Discourse statements and titlings are statements:

— *Statement = DiscourseStatement* ∪ *Titling*

6.1.2.5   Texts

The class of texts of a Common Logic language is the class Text that is obtained from the recursive application of the set of operations *txt*, *imports*, and *domain* under the following conditions:

— *txt*:(*Sentence* ∪ *Statement* ∪ *Text*) × … × (*Sentence* ∪ *Statement* ∪ *Text*) → *TextConstruction*

— *imports*:Ttl → *Importation*

— *domain*:*Term* × *Text* → *DomainRestriction*

Text Constructions, domain restrictions, and importations are texts:

— *Text = TextConstruction* ∪ *DomainRestriction* ∪ *Importation*
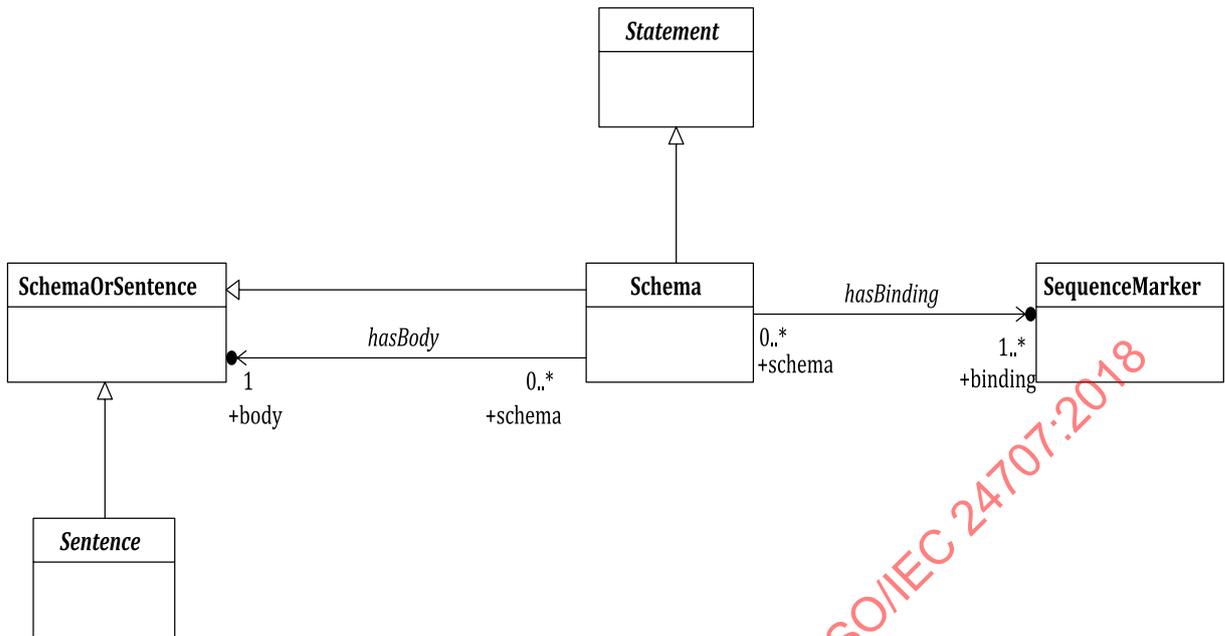
Figure 9 — Abstract syntax of text constructions
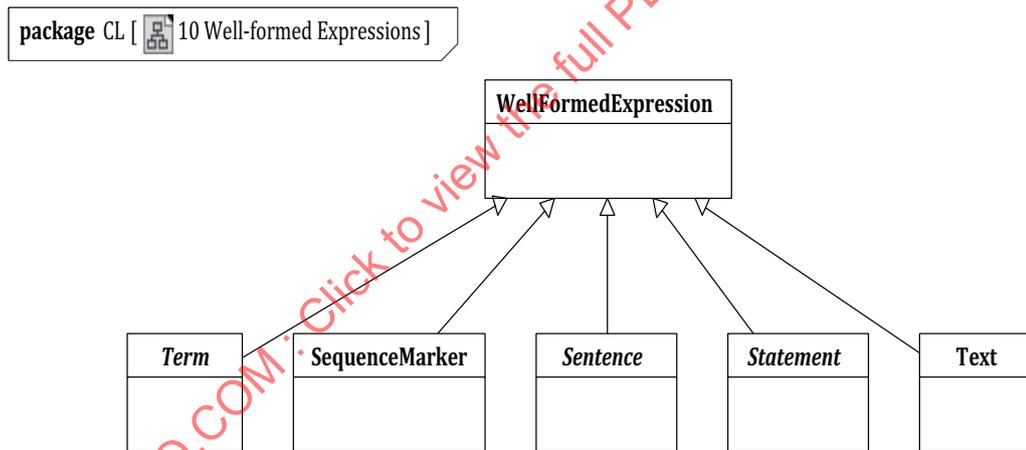
Figure 10 — Abstract syntax of well-formed expressions

6.1.2.6 Well-Formed Expressions

Terms, sequence markers, sentences, statements, and texts are well-formed expressions:

— *Wfe = Term ∪ SequenceMarker ∪ Sentence ∪ Statement ∪ Text*

6.1.2.7 Metamodel

Figures 1 to 9 provide a non-normative metamodel showing relationships among the syntactic categories.

6.1.3 Importation closure

An untitled importation in a text is an occurrence of an importation expression that is not a descendant of a titling in the abstract syntax tree as defined in 6.1.2.

A corpus is a set of texts in the Common Logic abstract syntax. A corpus may be empty, finite, or infinite. An importation fixed-point under a title mapping ttl is a corpus C such that if G is a text in C, then C contains every text G' derived from G by replacing one occurrence of an untitled importation with name N by the text which is the value ttl(N) of the title mapping. The importation closure of a corpus C under a title mapping ttl is the intersection of all importation fixed-points under ttl that contain C. The importation closure of every non-empty corpus in a Common Logic language is non-empty.

6.1.4   Abstract syntactic structure of dialects

Dialects **may**, in addition, provide for other forms of sentence construction not described by this syntax, but in order to be fully conformant, such constructions shall either be new categories defined in terms of these categories or be extensions of these categories (e.g. new kinds of Boolean sentence, or kinds of quantifier) which are equivalent in meaning to a construction using just this syntax, interpreted according to the Common Logic semantics; that is, they can be considered to be systematic abbreviations or macros, also known as "syntactic sugar". The CLIF dialect (described in Annex A) and XCL (described in Annex C) contain a number of syntactic sugared forms for quantified and atomic sentences. (Other types of compliance are also recognized: see Clause 7 for a full account of conformance.)

The only undefined terms in the abstract syntax clause are *name*, *sequence marker*, and *title*. The only required syntactic constraint on the basic lexical categories of *name* and *sequence marker* is that they **shall be** exclusive. Dialects intended for transmission of content on a network **should not** impose arbitrary or unnecessary restrictions on the form of names, and **shall** provide for certain names to be used as titles of Common Logic texts. Dialects intended for use on the Web **should** allow Internationalized Resource Identifiers to be used as names[2][4]. Common Logic dialects **should** define names in terms of Unicode (ISO/IEC 10646) conventions.

There is no notion of "bound variable" in the CL abstract syntax. Names that can occur bound are not required to be lexically distinguished from those that can (only) occur free, nor are names required to be partitioned into distinct classes such as relation, function or individual names. There are no sortal restrictions on names. Particular Common Logic dialects **may** make these or other distinctions between subclasses of names, and impose extra restrictions on the occurrence of types of names or terms in expressions — for example, by requiring that names that can occur bound (i.e. the variables of traditional first-order languages) be written with a special prefix, as in KIF, or with a particular style, as in Prolog; or by requiring that operators be in a distinguished category of relation names, as in traditional first-order syntax.

A dialect **may** impose particular semantic conditions on some categories of names, and apply syntactic constraints to limit where such names occur in expressions. For example, the CLIF and XCL syntaxes treat numerals as having a fixed denotation and prohibit their use as titles.

A dialect **may** require some names to be syntactic *non-discourse names*, which are understood to never denote entities in the universe of discourse. This requirement may be imposed, for example, by partitioning the vocabulary or by requiring names that occur in certain syntactic positions to be non-discourse. A dialect with syntactic non-discourse names is called *segregated*. In segregated dialects, names which are not non-discourse names are called *discourse names*.

A dialect **shall** provide sufficient syntactic constraints to guarantee that in any syntactically legal text of the dialect,

— every name shall be classified as either discourse or as non-discourse,

— no name shall be classified as both discourse and non-discourse,

— no non-discourse name shall be an argument of a simple sentence or functional term, and

— no non-discourse name shall be bound in a quantified sentence.

A dialect may have additional mechanisms for embedding information within CL texts that may be deleted without affecting the parsing of the text into the abstract syntax and may be omitted during the translation into other concrete dialects.

6.2 Common logic semantics

The semantics of Common Logic is defined in terms of a satisfaction relation between Common Logic text and mathematical structures called *interpretations*.

An *interpretation I* of a Common Logic language L with lexicon $\lambda = (V_\lambda, Smark_\lambda, Ttl_\lambda)$ (where $V_\lambda \subseteq V$, $Smark_\lambda \subseteq Smark$, $Ttl_\lambda \subseteq Ttl$) is a set UR_I, the *universe of reference*, with a distinguished subset UD_I, the *universe of discourse*, and five mappings:

— *int$_I$* from names in V_λ to UR_I;

— *rel$_I$* from UR_I to the power set of UD_I^*;

— *fun$_I$* from UR_I to total functions from UR_I^* into UR_I;

— *seq$_I$* from sequence markers in $Smark_\lambda$ to UR_I^*;

— *a title mapping ttl$_I$* from Ttl_λ to texts of L.

If UD_I is non-empty and the range of *fun$_I$* is total functions from UD_I^* into UD_I, then it can be said that *I* is a core interpretation of L.

Intuitively, UD_I is the universe or domain of discourse containing all the individual things the interpretation is "about" and over which the quantifiers range. UR_I is a potentially larger set of things that might also contain entities which are not in the universe of discourse. In particular, UR_I might contain relations not in UD_I to serve as the interpretations of the non-discourse names. All names are interpreted in the same way, whether or not they are understood to denote something in the universe of discourse; that is why there is only a single interpretation mapping that applies to all names regardless of their syntactic role. In particular, rel_I(x) is in UD_I^* even when x is not in UD_I. When considering only classical dialects, the elements of the universe of reference which are outside the universe of discourse may be identified with their corresponding values of the *rel$_I$* and *fun$_I$* mappings, which are then re-interpreted to be the identity mapping. The resulting construction maps predicates directly to relations and operators to functions, yielding a more traditional interpretation structure for the segregated syntax of traditional first-order logic.

Although sequence markers are mapped into finite sequences in an interpretation, these sequences are not denoted by names, and so are not required to be in the universe of reference.

The assignment of semantic values to complex expressions — notably, the assignment of truth values to sentences — requires some auxiliary definitions.

Let S be a subset of $V \cup Smark$. An interpretation *J* of V is an S-variant of *I* if it is exactly like *I* except that int_J and seq_J might differ with int_I and seq_I on what they assign to the members of S. More formally, *J* is an S-variant of *I* if $UR_J = UR_I$, $UD_J = UD_I$, $rel_J = rel_I$, $fun_J = fun_I$, $ttl_I = ttl_J$, $int_J(n) = int_I(n)$ for names $n \notin$ S, $int_I(n) \in UD_I$ for names $n \in$ S, $seq_J(s) = seq_I(s)$ for sequence markers $s \notin$ S, and $seq_J(s) \in UD_J^*$ for $s \in$ S.

If E is a subset of UD_I, then the *restriction* of *I* to E is an interpretation *K* of the same language L and over the same universe of reference and with $int_K = int_I$ and $seq_K = seq_I$, but where $UD_K = E$, rel_K(v) is the restriction of rel_I(v) to E^* and fun_K(v) = fun_I(v) for all v in the vocabulary of *I*.

If s = $<s_1, ..., s_n>$ and t = $<t_1, ..., t_m>$ are finite sequences, then s;t is the concatenated sequence $<s_1, ..., s_n, t_1, ..., t_m>$. In particular, s;<> = s for any sequence s.

Table 1 — Specification of auxiliary definitions to be used for the semantics

$E \in \lambda$	ArgC(E) = ∅
E = *Func* $(T,T_1,...,T_n)$	ArgC(E) = { $T_1,...,T_n$ } ∪ ArgC(T)
E = Atomic$(T,T_1,...,T_n)$	ArgC(E) = { $T_1,...,T_n$ } ∪ ArgC(T)
E = Neg(S)	ArgC(E) = ArgC(S)
NOTE For any well-formed expression E, this table specifies the set ArgC(E) of argument constants of E.	

Table 1 *(continued)*

E = Conj(S_1,...,S_n)	ArgC(E) = ArgC(S_1,...,S_n)
E = EQuant(N,S)	*ArgC(E) = ArgC(S) ∪ N*
E = outDiscourse(T_1,...,T_n)	ArgC(E) = $∪_i$ ArgC(T_i)
E = inDiscourse(T_1,...,T_n)	ArgC(E) = $∪_i$ ArgC(T_i)
E = txt(E_1,...,E_n)	*ArgC(E) = ArgC(E_i)*
E = domain(T,G)	*ArgC(E) = ArgC(G) ∪ ArgC(T)*
E = title(E_1,G)	ArgC(E) = ArgC(G)
E = imports(E_1)	ArgC(E) = ∅
NOTE For any well-formed expression E, this table specifies the set ArgC(E) of argument constants of E.	

The value of any expression E in the interpretation *I* is given by following the rules in Table 2.

Table 2 — Interpretations of Common Logic expressions

E1	Name **N**	$I(E) = int_I(N)$
E2	Sequence marker **S**	$I(E) = seq_I(S)$
E3	Title **N**	$I(E) = ttl_I(N)$
E4	Term sequence $T_1 ... T_n$ with T_1 a term	$I(E) = <I(T_1)>;I(<T_2 ... T_n >)$
E5	Term sequence $T_1 ... T_n$ with T_1 a sequence marker	$I(E) = I(T_1);I(<T_2 ... T_n >)$
E6	Term with operator **O** and argument sequence **S**	$I(E) = fun_I(I(O))(I(S))$
E7	Simple sentence which is an equation containing terms T_1, T_2	$I(E)$ = true if $I(T_1) = I(T_2)$; otherwise, $I(E)$ = false
E8	Atomic sentence with predicate **P** and argument sequence **S**	$I(E)$ = true if $I(S)$ is in $rel_I(I(P))$; otherwise, $I(E)$ = false
E9	Boolean sentence of type negation and component **C**	$I(E)$ = true if $I(C)$ = false; otherwise, $I(E)$ = false
E10	Boolean sentence of type conjunction and components $C_1 ... C_n$	$I(E)$ = true if $I(C_1) = ... = I(C_n)$ = true; otherwise, $I(E)$ = false
E11	Boolean sentence of type disjunction and components $C_1 ... C_n$	$I(E)$ = false if $I(C_1) = ... = I(C_n)$ = false; otherwise, $I(E)$ = true
E12	Boolean sentence of type implication and components C_1, C_2	$I(E)$ = false if $I(C_1)$ = true and $I(C_2)$ = false; otherwise, $I(E)$ = true
E13	Boolean sentence of type biconditional and components C_1, C_2	$I(E)$ = true if $I(C_1) = I(C_2)$; otherwise, $I(E)$ = false
E14	Quantified sentence of type universal with bindings **N** and body **B**	$I(E)$ = true if for every **N**-variant J of I, $J(B)$ is true; otherwise, $I(E)$ = false
E15	Quantified sentence of type existential with bindings **N** and body **B**	$I(E)$ = true if for some **N**-variant J of I, $J(B)$ is true; otherwise, $I(E)$ = false
E16	Irregular sentence **S**	$I(E) = int_I(S)$
E17	An out-discourse statement outDiscourse($T_1 ... T_n$)	$I(E)$ = true if $I(T_i) ∉ UD_I ∪ UD_I*$ for 0 < i < n; otherwise, $I(E)$ = false
E18	An in-discourse statement inDiscourse($T_1 ... T_n$)	$I(E)$ = true if $I(T_i) ∈ UD_I ∪ UD_I*$ for 0 < i < n; otherwise, $I(E)$ = false
E19	A text construction txt($E_1 ... E_n$)	$I(E)$ = true if $I(E_1) = ... = I(E_n)$ = true; otherwise, $I(E)$ = false

Table 2 *(continued)*

E20	A domain restriction domain(N,G)	$I(E)$ = true if there is some interpretation $J = \left[I < \left\{ x \middle\| x \middle\| \in rel_I \left(I(N) \right) \right\} \right]$ and J(G) = true; otherwise, $I(E)$ = false
E21	A text titling title(E_1 ,G), where G is a text in the sense of the abstract syntax	$I(E)$ = true if $ttl_I(E_1)$ = G; otherwise, $I(E)$ = false
E22	An import statement imports(E_1)	$I(E)$ = true

These are the basic logical semantic conditions which all conforming dialects shall satisfy. For texts with occurrences of interpreted names, the interpretations are further restricted (see 6.3). A dialect may impose further semantic conditions in addition to these.

A semantic extension which restricts Common Logic interpretations according to naming conventions, such as network identification conventions, is called external. External semantic constraints may refer to conventions or structures which are defined outside the model theory itself.

Table 2 specifies no interpretation for comments. The interpretation of an expression with an attached comment is the same as the interpretation of the corresponding expression without the comment. Thus, adding or deleting comments does not change the truth-conditions of any Common Logic text. Nevertheless, comments are part of the formal syntax and applications **should** preserve them when transmitting, editing or re-publishing Common Logic text. In particular, a name used to title a text in Common Logic is understood to be mapped to an expression of the abstract syntax, so that if the same name is used, within the same corpus, to title a text that parses to a different abstract syntax expression, that corpus will be unsatisfiable (see 6.4) even if the texts are identical except for comments.

Titlings are not required to be in 1:1 correspondence to documents, files or other units of data storage. Dialects or implementations may provide for texts to be distributed across storage units, or for multiple named texts to be stored in one unit. The titling conventions for text may be related to the addressing conventions in use for data units, but this is not required. Texts may also be identified by external naming conventions, for example, by encoding the text in documents or files which have network identifiers; the Common Logic semantics described in 6.2 **shall** be applicable to all network identifiers used as text titles on a network on which Common Logic texts are published or transmitted.

6.3 Datatypes

A datatype is a mapping from a lexical space (which can be represented explicitly in the syntax) to a value space (which is arbitrary). Within the abstract syntax, elements of a datatype's lexical space are interpreted names.

The semantics of datatypes in Common Logic is specified by the following conditions.

a) The denotation of interpreted names is the same in all interpretations.

b) The denotations of interpreted names of default datatypes are defined explicitly.

c) The denotations for datatyped interpreted names in cases where the datatype is standardized shall be specified by the corresponding standard (e.g. XSD).

d) For user-defined datatypes, the denotations shall be specified either by an explicit axiomatization or definition in mathematical language, or use the mechanisms for user-defined datatypes provided in other standards (e.g. XML Schema or Relax NG). If the name of the datatype is an IRI, then that IRI shall dereference to a document that provides this definition.

The occurrence of any interpreted name in a Common Logic text imposes a constraint on the interpretation of that text such that the value of int(I) for such a name is always the truth value assigned by the datatype associated with that interpreted name. A Common Logic dialect that includes

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interpreted names according to the above specifications is not classified as a semantic extension on that basis.

6.4   Satisfaction, validity and entailment

Since the semantics of Common Logic does not assume a fixed distinction between names which are out of discourse and names which are in discourse, texts may differ on these two sets. A discourse supposition may be full or partial. A full discourse presupposition D is a partition of the lexicon λ of names (V) and sequence markers (Smark) into the set of names and sequence markers λ_D which are in-discourse and the complementary set of names and sequence markers λ_N which are said to be out-of-discourse. While a full discourse presupposition provides a discourse assignment for every symbol in the lexicon, a partial discourse presupposition makes such an assignment for a proper subset of the lexicon; that is, $\lambda \cup D \cup \lambda_N$ is a subset of λ.

An interpretation I meets a discourse presupposition D iff

a)   for any name N $\in \lambda_D$, there is int$_I$ *(N)* $\in UD_I$,

b)   for any sequence marker S $\in \lambda_D$, there is seq$_I$ *(S)* $\in UD_I^*$,

c)   for any name N $\in \lambda_N$, there is int$_I$ *(N)* $\notin UD_I$, and

d)   for any sequence marker S $\in \lambda_N$, there is seq$_I$ *(S)* $\notin UD_I^*$.

A Common Logic corpus C is *satisfied* by an interpretation *I* under the discourse presupposition D iff

1)   *I*(G) = true and ArgC*(G)* $\in UD_I \cup UD_I^*$ for every G in the importation closure of C under ttl$_I$, and

2)   I meets D.

A corpus C is *satisfiable under a discourse presupposition D* if there is a core interpretation which satisfies it and meets D; otherwise, it is *unsatisfiable* or *contradictory*. If every core interpretation which satisfies S under a discourse presupposition D also satisfies C under the same discourse presupposition, then S *entails* C under the discourse presupposition D.

A corpus C is *satisfiable* if there is an interpretation which satisfies it; otherwise, it is *unsatisfiable* or *contradictory*. If every interpretation which satisfies S also satisfies C, then S *entails* C.

Common logic interpretations treat irregular sentences as opaque sentence variables by requiring that irregular sentences be parsed to propositions (nullary atomic sentences) in the abstract syntax. In a dialect which recognizes irregular sentences, the above definitions are used to refer to interpretations determined by the semantics of the dialect; however, when qualified by the prefixing adjective or adverb "common-logic", as in "common-logic entails", they shall be understood to refer to interpretations which conform exactly to the Common Logic semantic conditions. For example, a dialect might support modal sentences, and its semantics supports the entailment *(Necessary P) entails P*; but this would not be a common-logic entailment, even if the language was conformant as a Common Logic extension. However, the entailment *(Necessary P) entails (Necessary P)* is a common-logic entailment.

Several of the later discussions consider restricted classes of interpretations. All the above definitions may be qualified to apply only to interpretations in a certain restricted class. Thus, S *foo* entails T just when for any interpretation *I* in the class *foo*, if *I* satisfies S then *I* satisfies T. Entailment (or unsatisfiability) with respect to a class of interpretations implies entailment (or unsatisfiability) with respect to any subset of that class.

When describing entailment of T from S, S is referred to as the *set of premises*, and T the *conclusion*, of the entailment.

6.5   Sequence markers, recursion and argument lists: discussion

Sequence markers take Common Logic beyond first-order expressivity. A sequence marker occurring in an argument sequence stands for an arbitrary finite sequence of arguments. A universal sentence

binding a sequence marker has the same semantic import as the *infinite* conjunction of all the expressions obtained by replacing the sequence marker by a finite sequence of names, all bound by universal quantification.

This ability to represent infinite sets of sentences in a finite form means that Common Logic with sequence markers is not compact, and therefore not first-order; for clearly the infinite set of sentences corresponding in meaning to a single sentence quantifying a sequence marker is logically equivalent to that sentence and so entails it, but no finite subset of the infinite set does. However, the intended use of sentences containing sequence markers is to act as axiom schemata, and when they are restricted to this use, the resulting logic is compact. This amounts to allowing sequence markers to be bound only by universal quantifiers at the top statement level of a text and restricting these sentences to be used only as axioms. This restriction is often appropriate for texts which are considered to be "ontologies", i.e. authoritative information sources representing a conceptualization of some domain of application, intended to be applied to other data.

A compact dialect which does not support sequence markers can imitate much of the functionality provided by sequence markers, by the use of explicit argument lists, represented in Common Logic by terms built up from a list-constructing function. A sequence marker translates into the name of a list, and quantification over list names replaces quantification over sequence markers. The finiteness condition on sequences then corresponds to an implicit fixed-point assumption made on all "standard" models of the list axioms. Such conventions are widely used in logic programming applications and in RDF and OWL. The costs of this technique are a considerable reduction in syntactic clarity and readability, the need to allow lists as entities in the domain of discourse, and possibly the reliance on external software to manipulate the lists. The advantage is the ability of rendering arbitrary argument sequences using only a small number of primitives and the use of a compact base logic. Implementations based on argument-list constructions are often limited to conventional first-order expressivity and fail to support all inferences involving quantification over lists. This may be considered either as an advantage or as a disadvantage.

6.6 Special cases and translations between dialects

A dialect in which all operators and predicates are non-discourse names and all non-discourse names are operators or predicates is called a *classical* dialect.

An interpretation I is *single-universe* when $UD_I = UR_I$. An interpretation I is *extensional* when rel_I and fun_I are the identity function on $(UR_I - UD_I)$, so that the entities in the universe of reference outside the domain are the extensions of the non-discourse names. For classical dialects, only extensional interpretations need be considered: for any given interpretation I, there is an extensional interpretation J which satisfies the same expressions of any text of the dialect as I does. J may be obtained by replacing $I(x)$ by $fun_I(I(x))$ for every operator x and by $rel_I(I(x))$ for every predicate x in the vocabulary, and removing them from the domain if they are present. Since all operator and predicates in a classical dialect influence the truth-conditions only through their associated extensions, this does not affect any truth-values. Formally, $UD_J = UD_I - \{I(v): v \text{ an operator or predicate in V}\}$, $int_J(x) = int_I(x)$ for discourse names, $int_J(x) = rel_I(int_I(x))$ for predicates x and $int_J(x) = fun_I(int_I(x))$ for operators x.

Guidelines for specifying translations between dialects are given in Annex D.

7 Conformance

7.1 Dialect conformance

7.1.1 Syntax

A dialect is defined over some set of inscriptions, which **shall** be specified. Commonly, this should be Unicode character strings (as specified in ISO/IEC 10646), but other inscriptions, e.g. diagrammatical representations such as directed graphs or structured images, are possible. A method **shall** be specified for the dialect which will unambiguously parse any inscription of text in the set, or reject it as syntactically illegal. For Unicode character string inscriptions, a grammar in EBNF is a sufficiently

precise specification. A *parsing* is an assignment of each part of a legal inscription into its corresponding CL abstract syntax category in 6.1.1, and the parsed inscription is an *expression*.

A dialect which provides only some types of the Common Logic expressions is said to be a *syntactically partial* Common Logic dialect or *syntactically partially conformant*. In particular, a dialect that does not include sequence markers, but is otherwise fully conformant, is known as a *syntactically compact* dialect. See 7.1 for a description of some relationships between syntactic and semantic conformance.

A dialect is **syntactically fully conformant** if its parsings recognize expressions for every category of the abstract syntax in 6.1.1. For Common Logic conformity, dialects or sub-dialects whose parsings include other categories of sentences **shall** either (a) categorize them as irregular sentences or (b) specify how these categories are mapped into the abstract syntax categories defined in 6.1.1. If a dialect conforms as in (a), such a dialect or sub-dialect shall be referred to as *semantic extensions* (see 7.1.2). It is conformant as a **syntactic sub-dialect** if it recognizes at least one of the CL categories, but any dialect **shall** recognize some form of sentence category. Three particular cases of syntactic sub-dialect are identified. A **compact sub-dialect** is a dialect that does not recognize sequence markers. An **unstructured sub-dialect** is a dialect that does not recognize titlings and importation statements. A **single domain sub-dialect** is a dialect that does not recognize domain restrictions.

A dialect is **syntactically segregated** if the parsing requires a distinction to be made between lexical categories of CL names in order to check legality of an expression in that dialect. Segregated dialects **shall** specify criteria which are sufficient to enable an application to detect the category of a name in the dialect without performing operations on any structure other than the name itself.

7.1.2   Semantics

Any CL dialect **shall** have a model-theoretic semantics, defined on a set of interpretations, called *dialect interpretations*, which assigns one of the two truth-values *true* or *false* to every statement, sentence or text in that dialect.

A dialect is **weakly semantically conformant** when, for any syntactically legal sentence (except comment) or text T in that dialect, there exists a mapping *tr* from expressions in the dialect to expressions in Common Logic abstract syntax and there exists a mapping *mod* from Common Logic interpretations to dialect interpretations such that the following conformance condition is true:

— *mod*(I) entails T iff I entails *tr*(T) for each Common Logic interpretation I of *tr*(T).

A dialect is **faithfully semantically conformant** when, for any syntactically legal sentence, statement (except comment) or text T in that dialect, there exists a mapping *tr* from expressions in the dialect to expressions in Common Logic abstract syntax such that the following conformance condition is true:

— a text T' is entailed by T iff *tr*(T') is entailed by *tr*(T).

A dialect is **expansively conformant** iff it is weakly semantically conformant and *mod* is a surjective mapping.

A dialect is **sublanguage semantically conformant** when, for any syntactically legal sentence, statement (except comment) or text T in that dialect, there exists a mapping *tr* from expressions in the dialect to expressions in Common Logic abstract syntax and there exists a mapping *mod* from Common Logic interpretations to dialect interpretations such that the following conformance conditions are true:

— the dialect is weakly semantically conformant;

— *tr* is an injective mapping;

— *mod* is a bijective mapping.

A dialect is **exactly semantically conformant** when, for any syntactically legal sentence, statement (except comment) or text T in that dialect, there exists a mapping *tr* from expressions in the dialect

to expressions in Common Logic abstract syntax and there exists a mapping *mod* from Common Logic interpretations to dialect interpretations such that the following conformance conditions are true:

— the dialect is weakly semantically conformant;

— *tr* is a bijective mapping;

— *mod* is a bijective mapping.

It follows that the notions of satisfiability, contradiction and entailment corresponding to the dialect interpretations, and to Common Logic interpretations, are identical for an exactly conforming dialect.

The simplest way to achieve exact semantic conformance is to adopt the CL model theory as the model-theoretic semantics for the dialect, but the definition is phrased so as to allow other ways of formulating the semantic meta-theory to be used if they are preferred for mathematical or other reasons, provided only that satisfiability, contradiction and entailment are preserved.

A *semantic sub-dialect* is a syntactic sub-dialect (see 7.1.1) and meets the semantic conditions in Table 1 and Table 2; that is, it recognizes only some parts of the full Common Logic and its interpretations are equivalent to the restrictions of a Common Logic interpretation to those parts.

A *semantic extension* is a dialect which satisfies the first condition, but does not satisfy the second condition. In other words, a semantic extension dialect has some part(s) whose interpretation is more constrained than they would be by a CL interpretation. Any dialect which imposes non-trivial semantic conditions on irregular sentences is a semantic extension in this sense.

This allows a semantic extension to apply "external" semantic conditions to irregular sentences, in addition to the CL semantic conditions. CLIF is an example of a semantic extension, by virtue of the semantic conditions it imposes on numbers and quoted strings.

Semantic extensions **shall** be referred to as "conforming semantic extension" or "conforming extension", rather than as exactly conformant or simply as "conformant". For sentences, statements and texts of a conforming extension, contradiction and entailment with respect to the Common Logic semantics implies, respectively, contradiction and entailment with respect to the dialect semantics, but not vice versa; and satisfaction with respect to the dialect semantics implies satisfaction with respect to Common Logic semantics, but not vice versa. This means that inference engines which perform Common Logic inferences will be correct, but may be less complete, for the dialect.

No dialect may restrict the range of quantification of a different dialect. Other dialects may treat all names as discourse names.

7.1.3   Presupposing dialects

CL dialects **may** mandate a partial or full discourse presupposition as the entailment regime for its texts. The specification of the discourse presupposition shall be unambiguously specified for each text in the dialect, but otherwise is arbitrary, e.g. it may be based on a naming convention or may be derived from the usage of names in the text.

Traditional first-order logic as a CL dialect is presupposing, with a discourse presupposition of "non-discourse" for all names used as function operators or predicates, and "discourse" for all names used as the arguments of functional terms or simple sentences or as bindings.

Single-universe CL dialects are also presupposing, with a discourse presupposition of "discourse" for all names.

Any CL dialect may include a syntactic construct for referring to an external discourse presupposition as the intended entailment regime for a text.

7.2 Application conformance

"Application" means any piece of computational machinery (software or hardware, or a network) which performs any operations on CL text (even very trivial operations like storing it for later re-transmission).

Conformance of applications is defined relative to a collection of dialects called the *conformance set*. Applications which are conformant for the XCL dialect may be referred to as "conformant" without qualification.

All conformant applications **shall** be capable of processing all legal inscriptions of the dialects in the conformance set. Applications which input, output or transmit CL text, even if embedded inside text processed using other textual conventions, **shall** be capable of round-tripping any CL text; that is, they shall output or transmit the exact inscription that was input to them, without textual alteration.

Applications which detect entailment relationships between CL texts in the conformance set are **correct** when, for any texts T and S in dialects in the conformance set, if the application detects the entailment of T from S, then S common-logic entails T [that is, for any Common Logic interpretation *I*, if *I*(S) = true, then *I*(T) = true]. The application is **complete** when, for any texts T and S in dialects in the conformance set, if S common-logic entails T, then the application can detect the entailment of T from S. (Note that this requires completeness "across" dialects in the conformance set).

Completeness does not require that the application can detect entailment in a semantic extension which is not common-logic entailment. If a dialect is a semantic extension, then an application is **dialect complete** for that dialect if, for any dialect interpretation *I* of that dialect, *I*(T) = true whenever *I*(S) = true, then the application detects the entailment of T by S.

7.3 Network conformance

Conformance of communication networks is defined relative to a collection of dialects called the conformance set. A network is conformant when it transmits all expressions of all dialects in the conformance set without distortion from any node in the network to any other node, and provides for network identifiers which satisfy the semantic conditions E17, E20 and as described in 6.2. Network transmission errors or failures which are indicated as error conditions do not count as distortion for purposes of conformance of a network.

Annex A
(normative)

Common Logic Interchange Format (CLIF)

A.1 General

Historically, the Common Logic project arose from an effort to update and rationalize the design of KIF[3] which was first proposed as a "knowledge interchange format" over a decade ago and, in a simplified form, has become a *de facto* standard notation in many applications of logic. Several features of Common Logic, most notably its use of sequence markers, are explicitly borrowed from KIF. However, the design philosophy of Common Logic differs from that of KIF in various ways, which is briefly reviewed here.

First, the goals of the languages are different. KIF was intended to be a common notation into which a variety of other languages could be translated without loss of meaning. Common Logic is intended to be used for information interchange over a network, as far as possible without requiring any translation to be done, and when it shall be done, Common Logic provides a single common *semantic* framework, rather than a syntactically defined interlingua.

Second, largely as a consequence of this, KIF was seen as a "full" language, containing representative syntax for a wide variety of forms of expressions, including, for example, quantifier sorting, various definition formats and with a fully expressive meta-language. The goal was to provide a single language into which a wide variety of other languages could be directly mapped. Common Logic, in contrast, has been deliberately kept "small". This makes it easier to state a precise semantics and to place exact bounds on the expressiveness of subsets of the language, and allows extended languages to be defined as encodings of axiomatic theories expressed in Common Logic.

Third, KIF was based explicitly on LISP. KIF syntax was defined to be LISP S-expressions, and LISP-based ideas were incorporated into the semantics of KIF, for example, in the way that the semantics of sequence variables was defined. Although the CLIF surface syntax retains a superficially LISP-like appearance in its use of nested unlabelled parentheses and could be readily parsed as LISP S-expressions, Common Logic is not LISP-based and makes no basic assumptions of any LISP structures. The recommended Common Logic interchange notation is based on XML, a standard which was not available when KIF was originally designed.

Finally, many of the "new" features of Common Logic have been motivated directly by the ideas arising from new work on languages for the semantic web[9].

The name chosen for Common Logic's KIF-like syntax is the Common Logic Interchange Format (CLIF). This is primarily to identify it as the version being prescribed in this document and to distinguish it from various other dialects of KIF that may or may not be exactly compatible.

KIF and CLIF are similar in several ways. Both languages contain as sub-dialects a syntax for classical first-order (FO) logic. Both languages have notation for sequence variables (called sequence markers in this document). Both languages use exclusively a prefix notational convention and S-expression style syntax conventions. Both use parentheses as lexical delimiters. Both indicate quantifier restrictions similarly.

Some known differences between KIF and CLIF are as follows.

a) KIF requires ASCII encoding; CLIF uses Unicode encoding.

b) KIF has explicit notations for defining functions and relations, which CLIF does not.

c) KIF does not use the enclosed-name notation which CLIF has.

d) KIF uses the "@" symbol as a sequence variable prefix; CLIF uses the three-dot sequence for sequence markers.

e) KIF handles comments differently than CLIF and does not have the "enclosing" construction.

f) KIF does not have the role-pair construction which CLIF has.

g) KIF does not have the irregular sentence type which CLIF has to allow for extensions of the language.

h) KIF does not have the notions of importation, texts, statements, and domain restrictions which CLIF has.

i) KIF distinguishes variables from names and requires quantifiers to bind only variables; CLIF does not make the distinction.

j) Free variables in KIF are treated as universally quantified. Free names in CLIF are simply names, and no quantification is implied.

k) KIF restricts operators and predicates to be names; CLIF allows general terms and also allows these names to be bound by quantifiers.

l) KIF does not support the guarded quantifier construction.

A.2   CLIF syntax

A.2.1   Characters

Any CLIF expression is encoded as a sequence of Unicode characters in accordance with ISO/IEC 10646. Any character encoding which supports the repertoire of ISO/IEC 10646 may be used, but UTF-8 (ISO/IEC 10646:2014, Annex D) is preferred. Only characters in the US-ASCII subset are reserved for special use in CLIF itself, so that the language can be encoded as an ASCII text string if required. This document uses ASCII characters. Unicode characters outside the ASCII range are represented in CLIF ASCII text by a character coding sequence of the form \u*nnnn* or \U*nnnnnn* where *n* is a hexadecimal digit character. When transforming an ASCII text string to a full-repertoire character encoding, or when printing or otherwise rendering the text for maximum accessibility for human readers, such a sequence **may** be replaced by the corresponding direct encoding of the character or an appropriate glyph. Moreover, these coding sequences are understood as denoting the corresponding Unicode character when they occur in quoted strings (see below).

The syntax is defined in terms of disjoint blocks of characters called *lexical tokens* (in accordance with ISO/IEC 2382:2015, 15.01.01 on lexical tokens). A character stream can be converted into a stream of lexical tokens by a simple process of lexicalization which checks for a small number of *delimiter* characters, which indicate the termination of one lexical token and possibly the beginning of the next lexical token. Any consecutive sequence of whitespace characters acts as a *separator* between lexical tokens (except within quoted strings and names; see below). Certain characters are reserved for special use as the first character in a lexical item. The double-quote (U+0022) character is used to start and end names which contain delimiter characters, the single-quote (apostrophe U+002C) character is used to start and end quoted strings, which are also lexical items which may contain delimiter characters, and the equality sign shall be a single lexical item when it is the first character of an item.

The backslash \ (reverse solidus U+005C) character is reserved for special use. Followed by the letter u or U and a four- or six-digit hexadecimal code, respectively, it is used to transcribe non-ASCII Unicode characters in an ASCII character stream, as explained above. Any string of this form in an ASCII string rendering plays the same Common Logic syntactic role as a single ordinary character. The combination \' (U+005C, U+002C) is used to encode a single quote inside a Common Logic quoted string, and similarly, the combination \" (U+005C, U+0022) indicates a double quote inside a double-quoted enclosed name string. In both cases, a backslash is indicated by two backslashes \\ (U+005C, U+005C). Any other occurrence of the backslash character is an error. These inner-quote conventions apply in both ASCII and full Unicode renderings.

A.2.2   Lexical syntax

A.2.2.1   General

A distinction is made between lexical and syntactic constructs for convenience in dividing up the presentation into two parts. This subclause may help implementers in identifying logical tokens that make up syntactic expressions, as shown in the next subclause, A.2.3. Implementations are not required to adhere to this distinction.

A.2.2.2   White space

```
white = space U+0032 | tab U+0009 | line U+0010 | page U+0012 | return U+0013 ;
```

A.2.2.3   Delimiters

Single quote (apostrophe) is used to delimit quoted strings, and double quote to delimit enclosed names, which obey special lexicalization rules. Quoted strings and enclosed names are the only CLIF lexical items which can contain whitespace and parentheses. Parentheses elsewhere are self-delimiting; they are considered to be lexical tokens in their own right. Parentheses are the primary grouping device in CLIF syntax.

```
open = '(' ;

close = ')' ;

stringquote = ''' ;

namequote= '"' ;

backslash= '\' ;
```

A.2.2.4   Characters

char is all the remaining ASCII non-control characters, which can all be used to form lexical tokens (with some restrictions based on the first character of the lexical token). This includes all the alphanumeric characters.

```
char = digit | '~' | '!' | '#' | '$' | '%' | '^' | '&' | '*' | '_' | '+' | '{' | '}' | '|' |
     ':' | '<' | '>' | '?' | '`' | '-' | '=' | '[' | ']' |   ';'| ',' | '.' | '/' | 'A' |
     'B' | 'C' | 'D' | 'E' | 'F' | 'G' | 'H' | 'I' | 'J' | 'K' | 'L' | 'M' | 'N' | 'O' |
     'P' | 'Q' | 'R' | 'S' | 'T' | 'U' | 'V' | 'W' | 'X' | 'Y' | 'Z' | 'a' | 'b' | 'c' |
     'd' | 'e' | 'f' | 'g' | 'h' | 'i' | 'j' | 'k' | 'l' | 'm' | 'n' | 'o' | 'p' | 'q' |
     'r' | 's' | 't' | 'u' | 'v' | 'w' | 'x' | 'y' | 'z' ;

digit = '0' | '1' | '2' | '3' | '4' | '5' | '6' | '7' | '8' | '9' ;

hexa = digit | 'A' | 'B' | 'C' | 'D' | 'E' | 'F' | 'a' | 'b' | 'c' | 'd' | 'e' | 'f' ;
```

A.2.2.5   Quoting within strings

Certain character sequences are used to indicate the presence of a single character. *nonascii* is the set of characters or character sequences which indicates a Unicode character outside the ASCII range.

For input using a full Unicode character encoding, this production should be ignored and nonascii should be understood instead to be the set of all non-control characters of Unicode outside the ASCII range which are supported by the character encoding. The use of the \uxxxx and \Uxxxxxx sequences in text encoded using a full Unicode character repertoire is deprecated.

innerstringquote is used to indicate the presence of a single-quote character inside a quoted string. A quoted string can contain any character, including whitespace; however, a single-quote character can occur inside a quoted string only as part of an *innerstringquote*, i.e. when immediately preceded by a backslash character. The occurrence of a single-quote character in the character stream of a quoted string marks the end of the quoted string lexical token unless it is immediately preceded by a backslash character. Inside enclosed name strings, double quotes are treated exactly similarly. *Innernamequote* is used to indicate the presence of a double-quote character inside an enclosed name.

```
nonascii = '\u' , hexa, hexa, hexa, hexa | '\U' , hexa, hexa, hexa, hexa, hexa, hexa ;


innerstringquote = '\'' ;


innernamequote = '\"' ;


innerbackslash= '\\'


numeral = digit , { digit } ;
```

Sequence markers are a distinctive syntactic form with a special meaning in Common Logic. Note that a bare ellipsis without any text (i.e. '. . .') is itself a sequence marker.

```
seqmark = '...' , { char } ;
```

Single quotes are delimiters for quoted strings; double quotes for enclosed names.

An enclosed name is simply a name which may contain characters which would break the lexicalization, such as "Mrs Norah Jones" or "Girl(interrupted)"; like any other name, it may denote anything. The surrounding double-quote marks are not considered part of the name, which is defined to be the character string obtained by removing the enclosing double-quote marks and replacing any internal occurrences of an innernamequote by a single double-quote character. In the case of double-quoted numerals, a new symbol is assigned to this interpretable name during parsing into the abstract syntax. It is recommended to use the enclosed-name syntax when writing URIs, URI references and IRIs as names, since these Web identifiers may contain characters which would otherwise break CLIF lexicalization: in particular, Xpath-compliant URI references will often end in a closing parenthesis.

A quoted string, in contrast, is an expression with a fixed semantic meaning: it *denotes* a text string similarly related to the string inside the quotes.

A.2.2.6   Quoted strings

Quoted strings and enclosed names require a different lexicalization algorithm than other parts of CLIF text, since parentheses and whitespace do not break a quoted text stream into lexical tokens.

When CLIF text is enclosed inside a text or document which uses character escaping conventions, the Common Logic quoted string conventions here described are understood to apply to the text described or indicated by the conventions in use, which should be applied first. Thus, for example, the content of the XML element **<cl- text>'a\'b<c'</cl-text>** is the CLIF syntax

quoted string 'a\'b<c' which denotes the five-character text string a'b<c. Considered as bare CLIF text, however, `'a\'b<c&apos` would simply be a rather long name.

```
quotedstring = stringquote, { white | open | close | char | nonascii | namequote |
     innerstringquote | innerbackslash }, stringquote ;


enclosedname = namequote, { white | open | close | char | nonascii | stringquote |
     innernamequote }, namequote
```

A.2.2.7   Reserved tokens

reservedelement consists of the lexical tokens which are used to indicate the syntactic structure of Common Logic expressions. These may not be used as names in CLIF text.

```
reservedelement = '=' | 'and' | 'or' | 'iff' | 'if' | 'forall' | 'exists' |
     'not' | 'cl:text' | 'cl:ttl' | 'cl:imports' | 'cl:restrict' | 'cl:indiscourse' |
     'cl:outdiscourse' | 'cl:comment' | 'cl:prefix' ;
```

A.2.2.8   Name character sequence

A *namecharsequence* is a lexical token which does not start with any of the special characters. Note that namecharsequences may not contain whitespace or parentheses, and may not start with a quote mark although they may contain them. Numerals and sequence markers are not namecharsequences.

```
namecharsequence = ( char , { char | stringquote | namequote | backslash } ) - (
     reservedelement | numeral | seqmark ) ;
```

A.2.2.9   Lexical categories

The task of a lexical analyser is to parse the character stream into consecutive, non-overlapping lexbreak and nonlexbreak strings, and to deliver the lexical tokens it finds as a stream of tokens to the next stage of syntactic processing. Lexical tokens are divided into eight mutually disjoint categories: the open and closing parentheses, numerals, quoted strings (which begin and end with ''), sequence markers (which begin with '..'), enclosed names (which begin and end with '"'), and namesequences and reserved elements.

```
lexbreak  = open | close | white , { white } ;


nonlexbreak = numeral | quotedstring | seqmark | reservedelement | namecharsequence |
     enclosedname ;


lexicaltoken  = open | close | nonlexbreak ;


charstream = { white } , { lexicaltoken, lexbreak }  ;
```

A.2.3 Expression syntax

A.2.3.1 Term sequence

Both terms and atomic sentences use the notion of a sequence of terms representing a vector of arguments to a function or relation. Sequence markers are used to indicate a subsequence of a term sequence; terms indicate single elements.

```
termseq = { term | seqmark } ;
```

```
cseqmark = seqmark | ( open, 'cl:comment', quotedstring , seqmark , close ) ;
```

A.2.3.2 Name

A name is any lexical token which is understood to denote an element. The names which have a fixed meaning from those which are given a meaning by an interpretation are distinguished.

```
interpretedname =  numeral | quotedstring | ( open, 'cl:comment', quotedstring , (numeral |
    quotedstring) , close ) ;
```

```
interpretablename =  namecharsequence | enclosedname |( open, 'cl:comment', quotedstring ,
    interpretablename , close );
```

```
name = interpretedname | interpretablename ;
```

A.2.3.3 Term

Names count as terms, and a functional term consists of an operator, which is itself a term, together with a vector of arguments. Terms may also have an associated comment, represented as a quoted string (in order to allow text which would otherwise break the lexicalization). Comment wrappers syntactically enclose the term they comment upon.

```
term = name | ( open, operator, termseq, close ) | ( open, 'cl:comment', quotedstring ,
    term, close ) ;
```

```
operator = term  ;
```

A.2.3.4 Equation

Equations are distinguished as a special category because of their special semantic role and special handling by many applications. The equality sign is not a name.

```
equation = open, '=', term, term, close ;
```

A.2.3.5 Sentence

Like terms, sentences may have enclosing comments. Note that comments may be applied to sentences which are subexpressions of larger sentences.

```
sentence = atomsent | boolsent | quantsent | commentsent ;
```

A.2.3.6 Atomic sentence

Atomic sentences are similar in structure to terms, but in addition, the arguments to an atomic sentence may be represented using role-pairs consisting of a role-name and a term. Equations are considered to

be atomic sentences, and an atomic sentence may be represented using role-pairs consisting of a role-name and a term.

```
atomsent = equation | atom ;


simple_sentence = ( open, predicate , termseq, close ) ;


predicate =  term ;
```

A.2.3.7   Boolean sentence

Boolean sentences require implication and biconditional to be binary, but allow conjunction and disjunction to have any number of arguments, including zero; the sentences (and) and (or) can be used as the truth-values true and false, respectively.

```
boolsent = ( open, ('and' | 'or') , { sentence }, close ) | ( open, ('if' | 'iff') ,
     sentence , sentence, close ) | ( open, 'not' , sentence, close ;
```

A.2.3.8   Quantified sentence

Quantifiers may bind any number of variables, and bound variables may be restricted to a category indicated by a term.

```
quantsent  = open, ('forall' | 'exists') ,  boundlist, sentence, close ;


boundlist = open, bvar, { bvar } , close ;


bvar = interpretablename |  cseqmark |


        ( open, (interpretablename | cseqmark), term, close ) ;
```

A.2.3.9   Commented sentence

A comment may be applied to any sentence, so comments may be attached to sentences which are subexpressions of larger sentences.

```
commentsent = open, 'cl:comment', quotedstring , sentence , close ;
```

A.2.3.10 Titling

CLIF titling gives a text a name.

```
titling = open, 'cl:ttl', interpretable  name , text , close ;
```

A.2.3.11 Discourse statement

A CLIF discourse statement is either an in-discourse statement (that specifies the set of terms which denote elements in universe of discourse) or an out-of-discourse statement (that specifies the set of terms which do not denote elements in the universe of discourse).

```
indiscourse = open, 'cl:indiscourse', term, {term} , close ;
```

```
outdiscourse = open, 'cl:outdiscourse', term, {term} , close ;
```

```
discoursestatement = indiscourse | outdiscourse ;
```

A.2.3.12 Statement

A CLIF statement is either a titling or a discourse statement, optionally with a comment.

```
statement = titling | discoursestatement | ( open, 'cl:comment', quotedstring , statement ,
      close ) ;
```

A.2.3.13 Importation

A CLIF importation contains a title that provides an identifier to an external Common Logic text.

```
importation = open, 'cl:imports', interpretablename , close ;
```

A.2.3.14 Domain restriction

Domain restrictions are named text segments which represent a text intended to be understood in a "local" context, where the name indicates the domain of the quantifiers in the text. The text name shall not be a numeral or a quoted string. Note that text and domain restriction are mutually recursive categories, so that domain restrictions may be nested.

```
domainrestriction =  open, 'cl:restrict , term , text, close;
```

A.2.3.15 Text

CLIF text is a text construction, importation, or domain restriction.

```
textconstruction = open, 'cl:text', { sentence | statement | text },  close ;
```

```
prefixdeclaration = open, 'cl:prefix', (quotedstring - 'cl'), interpretablename, close ;
```

```
commenttext = open, 'cl-comment', quotedstring, {prefixdeclaration}, cltext, close ;
```

```
text  = textconstruction | domainrestriction | importation |  commenttext ;
```

```
cltext = {text} ;
```

A.3 CLIF semantics

The semantics of CLIF is equivalent to the semantics of the abstract CL syntax in 6.2.

NOTE   The interpretation of any expression of CLIF is then determined by the entries in Table A.1. The notation <T_1 … T_n> indicates a term sequence when referring to the syntax, and a sequence, i.e. an element of U_I*, when referring to the semantics. The first column indicates links to rows in Table 2.

Table A.1 — CLIF semantics

	If E is an expression of the form	Then $I(E)$ =
E1	A decimal numeral	The natural number denoted by the decimal numeral
E1	A quoted string 's'	The Unicode character string formed by removing the outer single quotes and replacing escaped inner substrings by their Unicode equivalents
E1, E2	An interpretable name	$I(E) = int_I(E)$
E3	A term sequence <T_1 … T_n> starting with a term T_1	$I(E) = <I(T_1)>;I(<T_2 … T_n>)$
E4	A term sequence T_1 … T_n starting with a sequence marker T_1	$I(E) = I(T_1); I(<T_2 … T_n>)$
E5	A term (O T_1 … T_n)	$I(E) = fun_I(I(O))(I(<T_1 … T_n>)$
	A name, term or sequence marker (cl-comment 'string' T)	$I(E) = I(T)$
E6	An equation (= T_1 T_2)	$I(E)$ = true if $I(T_1) = I(T_2)$; otherwise, $I(E)$ = false
E7	An atomic sentence (P T_1 … T_n)	$I(E)$ = true if $I(<T_1 … T_n>)$ is in $rel_I(I(P))$; otherwise, $I(E)$ = false
E8	A Boolean sentence (not P)	$I(E)$ = true if $I(P)$ = false; otherwise, $I(E)$ = false
E9	A Boolean sentence (and P_1 … P_n)	$I(E)$ = true if $I(P_1) = …I(P_n)$ = true; otherwise, $I(E)$= false
E10	A Boolean sentence (or P_1 … P_n)	$I(E)$ = false if $I(P_1) = …I(P_n)$ = false; otherwise, $I(E)$ = true
E11	A Boolean sentence (if P Q)	$I(E)$ = false if $I(P)$ = true and $I(Q)$ = false; otherwise, $I(E)$ = true
E12	A Boolean sentence (iff P Q)	$I(E)$ = true if $I(P) = I(Q)$; otherwise, $I(E)$ = false
	A sentence or statement (cl:comment "string" P)	$I(E) = I(P)$
E13	A quantified sentence (forall (N_1 … N_n) B) where N = {N_1, …, N_n} is the set of bindings for the sentence	$I(E)$ = true if for every N-variant J of I, $J(B)$ = true; otherwise, $I(E)$ = false
E14	A quantified sentence (exists (N_1 … N_n) B) where N = {N_1, …, N_n} is the set of bindings for the sentence	$I(E)$ = true if for some N-variant J of I, $J(B)$ = true; otherwise, $I(E)$ = false
	A well-formed expression (cl:comment "string")	$I(E)$ = true
E17	An importation (cl:imports N)	$I(E)$ = true
E19	A text construction (cl:text T_1 … T_n)	$I(E)$ = true if $I(T_1)$= … = $I(T_n)$ = true; otherwise, $I(E)$ = false
E20	A titling (cl:ttl N T)	$I(E)$ = true if $ttl_I(N)$ = T; otherwise, $I(E)$ = false

Table A.1 *(continued)*

	If E is an expression of the form	Then $I(E) =$
E21	An in-discourse statement (cl:indiscourse $\mathbf{T}_1 \dots \mathbf{T}_n$)	$I(E)$ = true if $I(\mathbf{T}_i) \in UD_I \cup UD_I*$ for $1 \le i \le n$; otherwise, $I(E)$ = false
E22	An out-of-discourse statement (cl:outdiscourse $\mathbf{T}_1 \dots \mathbf{T}_n$)	$I(E)$ = true if $I(\mathbf{T}_i) \notin UD_I \cup UD_I*$ for $1 \le i \le n$; otherwise, $I(E)$ = false
E23	A domain restriction (cl:restricts $\mathbf{N}$ $\mathbf{T}$)	The text $\mathbf{T}$ [$\mathbf{T}'$]) where $\mathbf{T}'$ is the text $\mathbf{T}$ in which every name or sequence marker $\mathbf{X}$ in the boundlist of a quantifier is replaced with ($\mathbf{X}$ $\mathbf{N}$)

Not every CLIF syntactic form is covered by Table A.1. The interpretation of the remaining syntactic cases is defined by mapping them to other CLIF expressions whose interpretation is defined by Table A.1. The translation is defined by Table A.2, which defines the translation **T [E]** of the expression **E**.

Table A.2 — Mapping from additional CLIF forms to core CLIF forms

If E is	Then E translates to T [E] =
A quantified sentence (forall (($\mathbf{N}_1$ $\mathbf{T}_1$) ...) $\mathbf{B}$)	The quantified sentence (forall ($\mathbf{N}_1$) **T [** (forall (...) (if ($\mathbf{T}_1$ $\mathbf{N}_1$) $\mathbf{B}$) **]**
A quantified sentence (exists (($\mathbf{N}_1$ $\mathbf{T}_1$) ...) $\mathbf{B}$)	The quantified sentence (exists ($\mathbf{N}_1$) **T [** (exists (...) (and ($\mathbf{T}_1$ $\mathbf{N}_1$) $\mathbf{B}$) **]**

The forms on the left side of Table A.2 can be considered to be "syntactic sugar" for their translations on the right, which are correspondingly referred to as their *sour* syntactic equivalents, and the subdialect of CLIF without these expressions forms as *sour CLIF*.

A.4 CLIF conformance

A.4.1 Syntactic conformity

The correspondence of CLIF syntax to the CL abstract syntax is indicated by the entries in the left column of Table A.1, which refer to the entries in Table 2, and from which the full syntactic conformance of sour CLIF can be determined by inspection. Note that both interpretednames and interpretablenames are considered to be CL names. The syntactic conformity of CLIF then follows by virtue of the mapping defined by Table A.2. Note that the CLIF comments syntax treats a commented expression as identical in meaning to the expression without the comment, so the comment can be considered to be "attached" to the uncommented expression.

A.4.2 Semantic conformity

CLIF is a CL semantic extension. To show that CLIF is a CL semantic extension, it is necessary to show that if I is a CLIF interpretation, then a CL interpretation shall exist which gives the same truth value to every sentence. This will be demonstrated by constructing J from I using the notation and conventions from above when describing I and from 6.2 when describing J.

J has the same vocabulary as I: $UD_J = UR_J = U_I$, $rel_J = rel_I$ and $fun_J = fun_I$. The interpretation of interpretablenames is defined in the obvious way: $int_J(x) = int_I(x)$ for any interpretablename x. Since the interpretednames of a CLIF vocabulary are classified as CL names, $int_J(x)$ shall also be defined when x is an interpretedname, and clearly, this is done to follow the first two entries in the CLIF semantic table, i.e. $int_J(x)$ = the integer denoted by x when x is a decimal numeral, and $int_J(x)$ = the Unicode character string denoted by x when x is a CLIF quoted string. It is then easy to see by a comparison of cases that J(s) = I(s) for any CLIF sentence s. If s is a text named N with an exclusion list L and a body B, then it shall be shown that J(s) = true just when [J<L](B) = true and rel(J(N)) = $UR_{[J<L]}*$ (since $UD_J = UR_J$). It is easy to see that this is exactly equivalent to the truth in I of sentences in the sour translation of the body text

defined by the second table above, as described in [6.2](#). (A formal proof would proceed by a structural induction on the sentences of the body text.) Hence, for any CLIF text t, J(t) = I(t).

It is not the case that if I is any CL interpretation of a CLIF text t, that there shall be a CLIF interpretation J which gives t the same value; for since CLIF interpretednames are treated simply as names in CL, J may assign them a value which does not conform to their fixed interpretation in CLIF, e.g. J('a string') = 3 is not ruled out by the common logic semantics rules. This is a general phenomenon with any dialect which imposes predetermined, externally defined, meanings on some category of names, such as numerals or datatyped expressions. Such dialects may support inferences which cannot be expressed as CL axioms, and shall be classified as external CL semantic extensions. The subdialect of CLIF which does not use numerals or quoted strings is exactly semantically conformant, as can be shown by inverting the above construction of J from I.

Annex B
(normative)

Conceptual Graph Interchange Format (CGIF)

B.1 General

B.1.1 General

This clause summarizes conceptual graphs and then describes a set of transformation (rewrite) rules that will be used with the rest of this annex to specify the description of the syntactic rules for CGIF.

The CG abstract syntax is a notation-independent specification of the expressions and components of the *conceptual graph core*, which is the minimal CG subset capable of expressing the full CL semantics. The semantics of any expression *x* in the CG core syntax is specified by the function *cg2cl*(*x*), which maps *x* to a logically equivalent expression in the CL abstract syntax. The function *cg2cl* is recursive, since a CG or its components may be nested inside other components.

B.2.1 to B.2.11 define the abstract CG syntax, the mapping of the abstract CG syntax to the abstract CL syntax, and the corresponding concrete syntax for CGIF core. Each subclause includes a formal definition, a mapping to CL, a syntax rule for CGIF concrete syntax, and a comment with explanation and examples. The syntax rules are written in Extended Backus-Naur Form (EBNF) rules, as specified by ISO/IEC 14977, and summarized in B.1.3. For each CGIF syntax rule, the lexical categories of A.2.2 shall be assumed. In A.2.3.2, the category *name* includes a category *enclosedname* of strings enclosed in quotes and a category *namesequence* of strings that are not enclosed. To avoid possible ambiguities, the category *CGname* requires that all CLIF name sequences except those in the CGIF category *identifier* shall be enclosed in quotes:

```
CGname  =  identifier | '"', (namesequence - identifier), '"'
          | numeral | enclosedname | quotedstring;
identifier  =  letter, {letter | digit | "_"};
```

When CGIF is translated to CL, any CGname shall be translated to a CLIF name by removing any quotes around a name sequence. CLIF does not make a syntactic distinction between constants and variables, but in CGIF, any CGname that is not used as a defining label or a bound label shall be called a *constant*.

The start symbol for CGIF syntax shall be the category `text`, if the input is a complete text, or the category `CG`, if the input is a string that represents a conceptual graph.

B.1.2 Conceptual graphs

A conceptual graph (CG) is a representation for logic as a bipartite graph with two kinds of nodes, called *concepts* and *conceptual relations*. The *Conceptual Graph Interchange Format* (CGIF) is a fully conformant dialect of Common Logic (CL) that serves as a serialized representation for conceptual graphs. This annex specifies the CGIF syntax and its mapping to the CL semantics. A nonnormative graphical notation, called the *CG display form*, is used in this document only in examples that illustrate the CG structures. The first example, Figure B.1, shows the display form that represents the sentence *John is going to Boston by bus*.
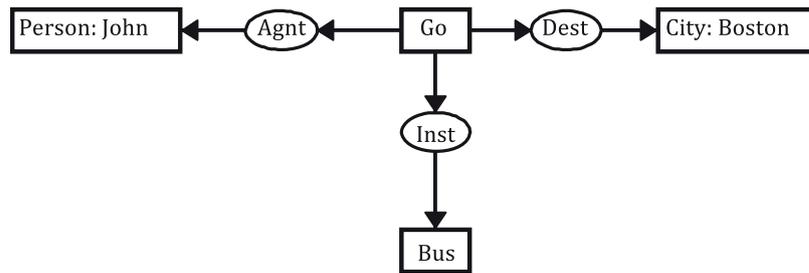
Figure B.1 — CG display form for "John is going to Boston by bus"

In the display form, rectangles or boxes represent concepts, and circles or ovals represent conceptual relations. An arc with an arrowhead pointing toward a circle marks the first *argument* of the relation, and an arc pointing away from a circle marks the last argument. If a relation has only one argument, the arrowhead is omitted. If a relation has more than two arguments, the arrowheads are replaced by integers 1,...,*n*.

The CG in Figure B.1 has four concepts, each with a *type label* that represents the type of entity to which the concept refers: Person, Go, Boston, and Bus. Two of the concepts have *constants* that identify individuals: John and Boston. Each of the three conceptual relations has a type label that represents the type of relation: Agnt for the agent of going, Inst for the instrument, and Dest for the destination. The CG as a whole indicates that the person John is the agent of an instance of going with Boston as the destination and a bus as the instrument. The following is the CGIF representation of Figure B.1:

```
[Go: *x] [Person: John] [City: Boston] [Bus: *y]
(Agnt ?x John) (Dest ?x Boston) (Inst ?x ?y)
```

In CGIF, the concepts are represented by square brackets and the conceptual relations are represented by parentheses. A character string prefixed with an asterisk, such as *x, is a *defining label*, which may be referenced by the *bound label* ?x, which is prefixed with a question mark. These strings, which are called *coreference labels* in CGIF, correspond to variables in Common Logic Interchange Format (CLIF). Unless prefixed with the symbol @every, a defining label is translated to an existential quantifier. The following is the equivalent CLIF representation of Figure B.1:

```
(exists ((x Go) (y Bus))
    (and (Person John) (city Boston)
         (Agnt x John) (Dest x Boston) (Inst x y)))
```

As this example illustrates, the differences between CGIF and CLIF result from the graph structure: the nodes of the graph have no implicit ordering, and the coreference labels such as *x or ?x represent connections of nodes rather than variables. Note that CGIF uses the prefixes * and ? to distinguish coreference labels from constants, but CLIF does not use any syntactic convention for distinguishing variables and constants.

Figure B.1 and its representation in CGIF illustrate the *extended syntax* of CGIF, which adds type labels on concepts and several other syntactic extensions to the *core syntax*. To convert the extensions of the extended syntax to the core CGIF, the type labels in the concept nodes are replaced by relations linked to the nodes. The concept [Go:*x], for example, becomes an untyped concept [*x] and a conceptual relation (Go ?x). The concept [Person: John] becomes [:John] (Person John), which may be simplified to just the relation (Person John). The following is the core CGIF and the corresponding CLIF:

```
[*x] [*y]
(Go ?x) (Person John) (City Boston) (Bus ?y)
(Agnt ?x John) (Dest ?x Boston) (Inst ?x ?y)

(exists (x y)
    (and (Go x) (Person John) (City Boston) (Bus y)
         (Agnt x John) (Dest x Boston) (Inst x y)))
```

To illustrate *contexts* and logical operators, Figure B.2 shows the display form for the sentence *If a cat is on a mat, then it is a happy pet.* As in Figure B.1, the rectangles represent concept nodes, but the two large rectangles contain nested conceptual graphs. Any concept that contains a nested CG is called a *context*; in this example, the type labels If and Then indicate that the proposition stated by the CG in the if-context implies the proposition stated by the CG in the then-context. The Attr relation indicates that the cat, also called a pet, has an attribute, which is an instance of happiness.
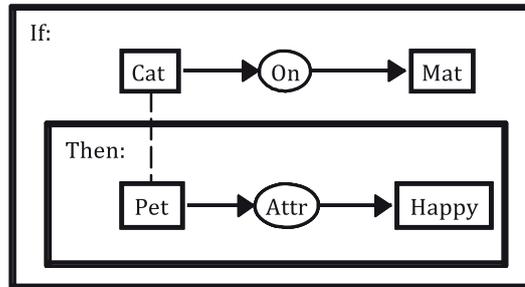
Figure B.2 — CG display form for "If a cat is on a mat, then it is a happy pet"

The dotted line connecting the concepts [Cat] and [Pet] is a *coreference link*, which indicates that they both refer to the same entity. In CGIF, the connection is shown by the defining label *x in the concept [Cat: *x] and the bound label ?x in the concept [Pet: ?x]:

```
[If: [Cat: *x] [Mat: *y] (On ?x ?y)
   [Then: [Pet: ?x] [Happy: *z] (Attr ?x ?z) ]]
```

In core CGIF, the type labels If and Then are replaced by a negation symbol ~ in front of the opening bracket, and the type labels are replaced by monadic relations:

```
~[ [*x] [*y] (Cat ?x) (Mat ?y) (On ?x ?y)
   ~[ [*z] (Pet ?x) (Happy ?z) (Attr ?x ?z) ]]
```

CLIF:

```
(not (exists (x y) (and (Cat x) (Mat y) (On x y)
   (not (exists (z) (and (Pet x) (Happy z) (Attr x z)))))))
```

In core CGIF, the only quantifier is the existential. In extended CGIF, universal quantifiers may be used to represent the logically equivalent sentence *For every cat and every mat, if the cat is on the mat, then it is a happy pet.* In extended CGIF, the universal quantifier is represented as @every:

```
[Cat: @every *x] [Mat: @every *y]
[If: (On ?x ?y) [Then: [Pet: ?x] [Happy: *z] (Attr ?x ?z) ]]
```

CLIF:

```
(forall ((x Cat) (y Mat))
   (if (On x y) (and (Pet x) (exists ((z Happy)) (Attr x z)))))
```

In CGs, functions are represented by conceptual relations called *actors*. Figure B.3 is the CG display form for the following equation written in ordinary algebraic notation:

```
y = (x + 7)/sqrt(7)
```

The three functions in this equation would be represented by three actors, which are drawn in Figure B.3, as diamond-shaped nodes with the type labels Add, Sqrt, and Divide. The boxes represent concept nodes, which contain the input and output values of the actors. The two empty concepts contain the output values of Add and Sqrt.
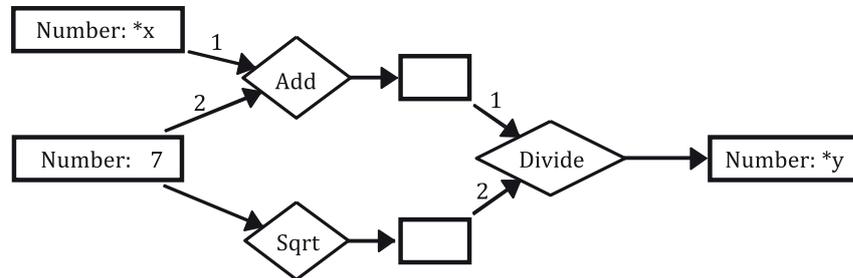
Figure B.3 — CL functions represented by actor nodes

In CGIF, actors are represented as relations with two kinds of arcs: a sequence of *input arcs* and a sequence of *output arcs*, which are separated by a vertical bar:

```
[Number: *x] [Number: *y] [Number: 7]
(Add ?x 7 | [*u]) (Sqrt 7 | [*v]) (Divide ?u ?v | ?y)
```

In the display form, the input arcs of Add and Divide are numbered 1 and 2 to indicate the order in which the arcs are written in CGIF. The following is the corresponding CLIF:

```
(exists ((x Number) (y Number))
   (and (Number 7) (= y (Divide (Add x 7) (Sqrt 7)))))
```

No CLIF variables are needed to represent the coreference labels *u and *v since the functional notation used in CLIF shows the connections directly.

All semantic features of CL, including the ability to quantify over relations and functions, are supported by CGIF. As an example, someone might say "Bob and Sue are related," but not say exactly how they are related. The following sentences in CGIF and CLIF state that there exists some familial relation *r* that relates Bob and Sue:

```
[Relation: *r] (Familial ?r) (#?r Bob Sue)

(exists ((r Relation)) (and (Familial r) (r Bob Sue)))
```

The concept [Relation: *r] states that there exists a relation *r*. The next two relations state that *r* is familial and *r* relates Bob and Sue. In CGIF, the prefix # indicates a bound coreference label used as a type label.

B.1.3 EBNF Syntax Rules for CGIF

In order to describe the syntax of CGIF, the EBNF notation is used, in accordance with ISO/IEC 14977. The specifications in this annex use only the following subset of the features specified by ISO/IEC 14977. B.1.3 is intended as informative only, as ISO/IEC 14977 shall be considered the normative reference.

Terminal symbol. Any string enclosed in either single quotes or double quotes.

EXAMPLE

```
"This is a quoted string." 'and so is this'
```

Nonterminal symbol. A name of a category in a syntax rule. For example, the following syntax rule contains two nonterminal symbols: one terminal symbol `'";"'`, a defining symbol `"="`, a concatenation symbol `","`, and a terminator symbol `";"`.

```
syntaxRule  =  expression, ";";
```

Option. An expression enclosed in square brackets. It specifies zero or one occurrence of any string specified by the enclosed expression.

EXAMPLE

```
[ "This string may or may not occur." ]
```

Iteration. An expression enclosed in curly braces. It specifies zero or more occurrences of any string specified by the enclosed expression.

EXAMPLE

```
{ "This string may occur many times." }
```

Concatenation. Two or more terms separated by commas.

```
"Two kinds of quotes: ", "'", " and ", '"', "."
```

Exception. Two terms separated by a minus sign −, which specifies any string specified by the first term, but not the second. The following example specifies a sequence of zero or more digits that does not contain "6":

```
{digit} - 6
```

Group. An expression enclosed in parentheses and treated as a single term. The following group encloses an exception that specifies a sequence of one or more digits by excluding the empty term:

```
({digit} - )
```

Alternatives. Two or more concatenations separated by vertical bars.

EXAMPLE

```
"cat", "dog" | "cow", "horse", "sheep" | wildAnimal
```

Special sequence. Any string enclosed by question marks. These sequences shall not affect the syntax specified by the syntax rules, but they may be used to copy strings analysed by a syntax rule for later use by the rewrite rules specified in B.1.3.

EXAMPLE

```
?sqn?
```

Syntax rule. A nonterminal symbol followed by "=" followed by an expression and ending with ";". The following syntax rules define the syntax of the syntax rules used in Annex B.

```
syntaxRule  =  expression, ";";
expression  =  alternative, {"|" alternative} | term, "-", term;
alternative =  term [variable], {"," term [variable]};
term        =  terminal | nonterminal | "[", expression, "]"
            |  "{", expression, "}" | "(", expression, ")" | empty;
terminal    =  "'", ({character - '"'} - empty), "'"
```

```
              | '"', ({character - "'"} - empty), '"';
nonterminal =  identifier;
variable    =  "?", identifier, "?";
identifier  =  letter, {letter | digit | "_"};
empty       =  ;
```

These rules specify a subset of the syntax rules specified in ISO/IEC 14977:1996, 8.1. The rules imply that ",", has higher precedence than "|", which has higher precedence than "=". Parentheses may be used to override the precedence or to make the grouping more obvious.

B.1.4   Notation for rewrite rules

B.1.4.1   General

The syntax of both core (see B.2) and extended CGIF (see B.3) is defined by rules in Extended Backus-Naur Form (EBNF) rules as specified by ISO/IEC 14977. To specify the translation from core CGIF to Common Logic, B.2 uses a combination of EBNF rules and mathematical notation supplemented with English. To specify the translation from extended CGIF to core CGIF, B.3 uses a combination of EBNF rules in B.1.4 and the rewrite rules defined in B.1.4.2. The syntax rules in Annex B presuppose a lexical analysis stage that has subdivided the text into *tokens* as in ISO/IEC 2382:2015, 15.01.01 (on lexical tokens); therefore, at any point where a comma occurs in an EBNF rule, zero or more characters of white space may occur in the input text.

B.1.4.2   Transformation rules

Each transformation rule shall define a function that analyses an input string and returns a sequence of one or more output strings. A transformation rule shall have three parts: a *header*, a syntax rule as defined in B.1.3, and zero or more *rewrite rules*. The first string in a header shall specify the name of the function, which shall also be the name of the nonterminal symbol defined by the syntax rule. The header shall also specify a variable whose value shall be the *input string* to be analysed by the syntax rule, and it shall specify a sequence of one or more *output variables*. If the syntax rule successfully analyses the input string from beginning to end, the rewrite rules, if any, are executed. The following are the syntax rules that define the syntax of the transformation rules; transRule is the start symbol.

```
transRule   =    header, syntaxRule, {rewriteRule}, "end", ";";
header      =    nonterminal, "(", variable, ")", "->",
                 variable, {"," variable};
rewriteRule =    assignment | conditional;
assignment  =    variable, "=", rewriteExpr, ";";
conditional =    "if", condition, ({rewrite rule} - empty),
                 {"elif", condition, ({rewrite rule} - empty)},
                 ["else", ({rewrite rule} - empty)], "end;"
condition   =    "(", test, {"&", test}, ")";
test        =    rewriteTerm, ["~"], "=", rewriteTerm;
test        =    rewriteTerm, ["~"], "=", rewriteTerm;
rewriteExpr =    rewriteTerm {"," rewriteTerm};
rewriteTerm =    terminal | variable | funTerm;
funTerm     =    identifier, "(", [funTerm, {"," funTerm}, ")";
```

The following nonterminal symbols from ISO/IEC 14977 shall be defined as in B.1.3: syntaxRule, terminal, nonterminal, variable, identifier, empty.

The function defined by a transformation rule shall translate the input string to the sequence of values of the output variables by copying substrings from the input and executing rewrite rules to transform those strings. The execution shall be determined by the following procedure.

Any parsing algorithm may be used to the analyse the input string according to the specifications of the syntax rule. At the beginning of the analysis, all variables that occur in the transformation rule shall be initialized to the empty string. Although some parsing algorithms may assign values to variables during the parsing phase, the semantics shall not require those values to be accessible for executing any rewrite rules until after all parsing has finished.

Any variable *x* in the syntax rule shall occur immediately after some term *t* in that rule; there shall be no comma or other symbol separating *t* and *x*. The value assigned to *x* shall be the substring *s* of the input string that was matched to the pattern specified by *t*. If the alternative in which *t* occurs was not taken or if *t* matched the empty string, the value of *x* shall be empty.

After parsing has finished, the rewrite rules following the syntax rule are executed sequentially, unless one or more rewrite rules in the options of a conditional are skipped.

When an assignment is executed, the values of the terminals, variables, and functional terms on the right side of the rule shall be concatenated in the order in which they are written. The resulting string shall be assigned as the value of the variable on the left side of the rule.

A condition that occurs in a conditional is a conjunction of one or more tests for the equality or inequality of the values of two terms. An empty term, which is written as a blank, has the empty string as value. Therefore, the condition (?x?= & ?y?~=) shall be true if and only if ?x? is empty and ?y? is not empty.

When a conditional is executed, the conditions for the if, elif, and else options shall be evaluated sequentially. (The condition for else shall always be true.) When the first true condition is found, the rewrite rules following that condition shall be executed sequentially until the next occurrence of elif, else, or end for that rule is found. Then execution shall continue with the rewrite rule, if any, which occurs after the end marker for that conditional.

When the end marker for the transformation rule is reached, execution shall stop. Then the value of the function named in the header shall be a sequence of the values of all the output variables. Any output variable that had not been assigned a value shall have the value of the empty string. Any output variable that has the same identifier as some variable in the syntax rule shall have the value assigned to it from the input string. No assignment shall change the value of any variable after a value has been assigned to it.

According to this specification, some transformation rules may have no rewrite rules. The following rule, for example, defines an identity function, whose output is identical to its input:

```
identity(?s?) -> ?t?;
identity = {character} ?t?;
end;
```

The input string *s* is parsed by the syntax rule as a string of zero or more characters. That string is assigned to *t*, which becomes the output of the function.

The value assigned to a variable as a result of the parse is always some substring from the input. Except for the identity function, the output values generated by the rewrite rules for any syntactic category are often very different from any substring of the input. As an example, the transformation rule named negation translates a negation from extended CGIF to core CGIF:

```
negation(?b?) -> ?ng?;
negation  =  "~[", [comment] ?cm?, CG ?x?, [endComment] ?ecm?, "]";
?ng?  = "~[", ?cm?, CG(?x?), ?ecm?, "]";
end;
```

The strings for the opening comment *cm* and the ending comment *ecm* are copied unchanged from input to output. But the nested CG, whose input string *x* is in extended CGIF, is very different from the core CGIF output of CG(*x*). The transformation rules for the syntactic categories of extended CGIF behave like compilers that translate input strings for extended CGIF categories to output strings in core CGIF.

B.1.4.3   Functions used in rewrite rules

Any function defined by a transformation rule may be used in a rewrite rule. It may even be used recursively in the same transformation rule that defines it. In addition to the functions defined by transformation rules, the following seven functions shall be available for use in processing strings or sequences in any rewrite rule.

— **first**(s) shall return the first or only element of a sequence s. If length(s)="0", first(s) shall be empty.

— **gensym**() shall return a string that represents a CGname that shall be different from any other CGname in the current text. Each time gensym() is invoked, the string it returns shall also be different from any string it had previously returned.

— **length**(s) shall return the length of the sequence s as a string of one or more characters that represent the decimal digits of the length. If s is empty, length(s) shall be "0". If s is a single element, length(s) shall be "1".

— **map**(f,s) shall apply a function f to each element of a sequence s in order to return the sequence of values of $f(x)$ for each x in s.

— **second**(s) shall return the second element of a sequence s. If length(s)<"2", second(s) shall be empty.

— **substitute**(s,t,x) shall return the result of substituting the string s for every occurrence of the string t in the string x. If t does not occur in x, substitute(s,t,x) shall be x.

— **third**(s) shall return the third element of a sequence s. If length(s)<"3", third(s) shall be empty. The English phrase "CG name" shall refer to any syntactic token of the category "CGname".

B.2   CG core syntax and semantics

B.2.1   actor

Definition: A conceptual relation $ac=(r,s)$, in which r shall be a reference called the *type label* of ac and the arc sequence $s=s_1,s_2$ shall consist of an arc sequence s_1, called the *input arcs*, and a single arc s_2, called the *output arc*.

CL: $cg2cl(ac)$ shall be an equation eq: the first term of eq shall be the name $cg2cl(s_2)$, and the second term of eq shall be the functional term with operator $cg2cl(r)$ and term sequence $cg2cl(s_1)$ with an optional sequence marker sqn.

CGIF:

```
actor  =  "(", [comment], [ "#", "?"], CGname, arcSequence, "|", arc,
          [endComment], ")";
```

Like other conceptual relations, an actor node is enclosed in parentheses. The symbol # shall mark a bound coreference label that is used as a type label.

Comment: Although an actor is defined as a special case of a conceptual relation, the CG core syntax restricts an actor to exactly one output arc so that it may be mapped to a CL function. The input arcs may include a sequence marker at the end, but no sequence marker shall be used for the output arc. The extended CGIF syntax allows actors to have any number of output arcs.

B.2.2   arc

Definition: A reference ar that occurs in an arc sequence of some conceptual relation.

CL: $cg2cl(ar)$ shall be the name n without the marker of the reference ar.

CGIF:

```
arc = [comment], reference;
```

Comment: The function *cg2cl* maps an arc to the name of the reference and omits any marker that distinguishes a bound label.

B.2.3   arcSequence

Definition: A pair *as*=(*s,sqn*) consisting of a sequence *s* of zero or more arcs followed by an optional sequence marker *sqn*.

CL: *cg2cl*(*as*) shall be a term sequence *ts*=*cg2cl*(*s*) and the sequence marker *sqn* if present in *as*. The term sequence *ts* shall be map(*cg2cl*,*s*), where *map* is a function that applies *cg2cl* to each arc of the sequence *s* to extract the name that becomes the corresponding element of the sequence *ts*.

CGIF:

```
arcSequence = {arc}, [[comment], "?", seqmark];
```

Any sequence marker in an arc sequence *as* shall be identical to the sequence marker in some existential concept that is directly contained in a context that contains the actor or conceptual relation that has the arc sequence *as*.

Comment: The option of having a sequence marker in an arc sequence implies that a conceptual relation may have a variable number of arcs.

B.2.4   comment

Definition: A string *cm*, which shall have no effect on the semantics of any CGIF expression *x* in which *s* occurs.

CL: *cg2cl*(*cm*) shall be the substring *s* of *cm* that does not include the delimiters "/*" and "*/" of a comment or the opening ";" of an end comment. The string *s* shall be included in a CL representation for a comment and shall be associated with the CL syntactic expression to which the CGIF expression *x* is translated. The syntax rules for comment and end comment are identical for core CGIF and extended CGIF.

CGIF:

```
comment = "/*", {(character-"*") | [ "*", (character-"/")]}, [ "*"], "*/";

endComment = ";", {character - ("]" | ")")};
```

The string enclosed by the delimiters "/*" and "*/" shall not contain a substring "*/". The string of an end comment may contain any number of ";", but it shall not contain "]" or ")".

Comment: A comment may occur immediately after the opening bracket of any concept, immediately after the opening parenthesis of any actor or conceptual relation, immediately before any arc, or intermixed with the concepts and conceptual relations of any conceptual graph. An end comment may occur immediately before the closing bracket of any concept or immediately before the closing parenthesis of any conceptual relation or actor. Since the syntax of comments is identical in core and extended CGIF, no additional syntax rules for comments shall be included in B.3.

B.2.5   concept

Definition: A pair *c*=(*R,g*) where *R* shall be either a defining label or a set of zero or more references, and *g* shall be a conceptual graph that is said to be *directly contained* in *c*.

CL: *cg2cl*(*c*) shall be the sentence *s* determined by one of the first three options below.

Context. If *R* is empty, then *s*=*cg2cl*(*g*). In this case, *c* shall be called a *context*.

Existential. If *g* is blank and *R* is a defining label, then the sentence *s* shall be a quantified sentence of type existential with a set of names {*cg2cl*(*R*)} and with a body consisting of a Boolean sentence of type conjunction and zero components. In this case, *c* shall be called an *existential concept*.

Coreference. If *g* is blank and *R* is a set of one or more references, then let *r* be any reference in *R*. The sentence *s* shall be a Boolean sentence of type conjunction whose components are the set of equations with first term *cg2cl*(*r*) and second term *cg2cl*(*t*) for every reference *t* in *R*–{*r*}. In this case, *c* shall be called a *coreference concept*.

Syntactically invalid. The case in which *g* is nonblank and *R* is not empty is not permitted in core CGIF, and no translation to CL is defined.

CGIF:

```
concept   =  context | existentialConcept | coreferenceConcept;

context   =  "[", [comment], CG, [endComment], "]";

existentialConcept  =  "[", [comment], "*", (CGname | seqmark),
                           [endComment], "]";

coreferenceConcept  =  "[", [comment], ":", {reference}-,
                           [endComment], "]";
```

A context shall be a concept that contains a CG; if the CG is blank, the context is said to be *empty*, even if it contains one or more comments. Any comment that occurs immediately after the opening bracket shall be part of the concept; any other comments shall be part of the nested CG. A coreference concept shall contain one or more constants or bound coreference labels; in EBNF, an iteration followed by a minus sign with nothing after it indicates at least one iteration.

Comment: A context is represented by a pair of brackets, which serve to limit the scope of quantifiers of the nested CG; an empty context [ ] is translated to CLIF as (and), which is true by definition. An existential concept is represented by a concept such as [*x], which is translated to CLIF as (exists (x) (and)); this sentence asserts that there exists some *x*. A coreference concept is represented by a concept that contains a set of constants or bound coreference labels, such as [: ?x Cicero Tully ?abcd], which is translated to a conjunction of equations in CLIF:

```
(and (= x Cicero) (= x Tully) (= x abcd))
```

A coreference concept with just one reference, such as [:?x], would become an empty conjunction (and). Since it has no semantic effect, such a concept may be deleted.

B.2.6 conceptual graph (CG)

Definition: A triple *g*=(*C*,*R*,*A*), where *C* is a set of concepts, *R* is a set of conceptual relations, and *A* is the set of arcs that shall consist of all and only those arcs that occur in the arc sequence of some conceptual relation in *R*. If *C* and *R* are both empty, then *A* is also empty, and *g* is called a *blank* conceptual graph.

CL: Let *E* be the subset of *C* of existential concepts; and let *X* be the set of all concepts, conceptual relations, and negations of *g* except for those in *E*.

Let *B* be a Boolean sentence of type conjunction with components consisting of all the sentences *cg2cl*(*x*) for every *x* in *X*.

If *E* is empty, then *cg2cl*(*g*) is *B*.

If *E* is non-empty, then *cg2cl*(*g*) is a quantified sentence of type existential with the set of names consisting of the CGname of the defining coreference label of every *e* in *E* and with the body *B*.

CGIF:

```
CG  =  {concept | conceptualRelation | negation | comment};
```

A conceptual graph consists of an unordered set of concepts, conceptual relations, negations, and comments. Formally, a negation is a pair consisting of a concept and a conceptual relation that are never separated in CGIF.

Comment: According to this specification, every CG maps to either a quantified sentence of type existential or to a Boolean sentence of type conjunction. If the conjunction has only one component, then the sentence could be simplified to an equality, an atomic sentence, or a Boolean sentence of type negation. If *g* is blank, the corresponding CLIF is (and), which is true by definition. Although there is no required ordering of the nodes of a CG, some software that processes CGIF may run more efficiently if the defining coreference labels occur before the corresponding bound labels; the simplest way to ensure that condition is to move the existential concepts to the front of any context.

B.2.7 conceptual relation

Definition: A pair *cr*=(*r,s*), in which *r* shall be a reference called the *type label* of *cr* and *s* shall be an arc sequence.

CL: *cg2cl*(*ac*) shall be an atomic sentence whose predicate is *cg2cl*(*r*) and whose term sequence is *cg2cl*(*s*).

CGIF:

```
conceptualRelation  =  ordinaryRelation | actor;

ordinaryRelation  =  "(", [comment], [ "#", "?"], CGname, arcSequence,
                        [endComment], ")";
```

An ordinary conceptual relation has just one sequence of arcs. An actor partitions the sequence of arcs in two subsequences. A bound coreference label that is used as a type label shall begin with the string "#?" or "#?".

Comment: By allowing the type label of a conceptual relation to be a bound label, CGIF supports the CL ability to quantify over relations and functions. As an example, see the CGIF at the end of B.1.2 that represents the sentence "Bob and Sue are related."

B.2.8 negation

Definition: A pair *ng*=(*c,cr*), in which *c* shall be a concept and *cr* shall be a conceptual relation whose type label *r* shall be a constant with CGname Neg. The pair (*c,cr*) shall be treated as a single unit.

CL: *cg2cl*(*ng*) shall be a Boolean sentence of type negation with the component *cg2cl*(*g*).

CGIF:

```
negation  =  "~", context;
```

A negation shall begin with the symbol ~. Although a negation is formally defined as a pair consisting of a context and a conceptual relation, the two elements of the pair shall not be expressed as separate nodes in CGIF.

Comment: A negation negates the proposition stated by the nested conceptual graph *g*. For examples, see the CGIF for Figure B.2. The negation of the blank CG, written ~ [ ], is always false; the corresponding CLIF is (not (and)).

B.2.9 reference

Definition: A pair *r*=(*m,n*) where *n* is a CG name and *m* is a *marker* that shall designate a *constant* or a *bound label*.

CL: *cg2cl*(*r*) shall be the name *n*. The marker *m* shall be ? for a bound label and the empty string "" for a constant.

CGIF:

```
reference  =  ["?"], CGname;
```

This syntax of references is identical in core CGIF and extended CGIF. Any CG name that consists of a quoted namesequence shall be translated to a CL name by erasing the enclosing quotes; all other CG names are identical to the corresponding CL names. Sequence markers are identical in CLIF and CGIF.

Comment: Since references are identical in core and extended CGIF, no additional syntax rules for references are included in B.3.

B.2.10 scope

Definition: A set of contexts *S* associated with a concept *x* that has a defining label with CG name *n*.

The following terms are used in defining the constraints on defining labels in both core and extended CGIF:

— *constant*, a CG name without any prefix.

— *bound coreference label*, a CG name with the prefix "?".

— *bound sequence label*, a sequence marker with the prefix "?".

— *bound label*, a bound coreference label or a bound sequence label.

— *defining coreference label*, a CG name with the prefix "*".

— *defining sequence label*, a sequence marker with the prefix "*".

— *defining label*, either a defining coreference label or a defining sequence label.

According to this definition, a defining sequence label shall begin with the string "*…" and a bound sequence label shall begin with the string "?…".

Constraints: The verb *contains* shall be defined as the transitive closure of the relation *directly contains*, and it shall satisfy the following constraints in both core and extended CGIF.

If a context *c* directly contains a conceptual graph *g*, then *c* directly contains every node of *g* and every component of those nodes, except for those that are contained in some context of *g*.

If a context *c* directly contains a context *d*, then *c* indirectly contains everything that *d* contains.

The phrase "*c* contains *x*" is synonymous with "*c* directly or indirectly contains *x*".

If a concept *x* with a defining label with name *n* is directly contained in some context *c*, then *c* shall not contain any concept other than *x* with a defining label with the same CG name *n*, and *c* shall be in the scope S associated with the concept *x*.

If a context *c* is in the scope S associated with a concept *x*, then any context *d* directly contained in *c* shall also be in the scope S, unless *d* directly contains a concept *y* with a defining label with the same CG name as the defining label of *x*.

Every bound label with CG name *n* shall be in the scope associated with some concept with a defining label with CG name *n*.

No constant with CG name *n* shall be in the scope associated with some concept with a defining label with CG name *n*.

These constraints ensure that for every CGIF sentence s, the translation *cg2cl*(s) shall obey the CL constraints on scope of quantifiers. Since the constraints on scope are identical in core and extended CGIF, no additional constraints shall be included in B.3.

B.2.11 text

Definition: A context *c* that is not contained directly or indirectly in any context.

CL: *cg2cl*(*c*) shall be text consisting of the sentence *cg2cl*(*g*), where *g* is the conceptual graph directly contained in *c*. If a CG name *n* occurs immediately before *g* in the CGIF specification of the context *c*, then *n* shall be the name of the CL text.

CGIF:

```
text  =  "[", [comment], "Proposition", ":", [CGname], CG,
            [endComment], "]";
```

Since a text is not contained in any context, it shall also be called the *outermost context*.

Comment: This syntax rule uses the syntax of extended CGIF, which allows a context to have a type label and a CG name. Since core CGIF syntax is a subset of extended CGIF syntax, text in core CGIF can be used by any processor that accepts extended CGIF. Context brackets may be used to group the concepts and relations of a text into units that correspond to CLIF sentences. That grouping is a convenience that has no effect on the semantics.

B.3   Extended CGIF syntax

B.3.1   General

Extended CGIF is a superset of core CGIF, and every syntactically correct sentence of core CGIF is also syntactically correct extended CGIF. Its most prominent feature is the option of a *type label* or a *type expression* on the left side of any concept. In addition to types, extended CGIF adds the following features to core CGIF:

— more options in concepts, including universal quantifiers;

— Boolean contexts for representing the operators or, if, and iff;

— the option of allowing concept nodes to be placed in the arc sequence of conceptual relations;

— the ability to import text into a text.

These extensions are designed to make sentences more concise, more readable, and more suitable as a target language for translations from natural languages and from other CL dialects, including CLIF. None of them, however, extend the expressive power of CGIF beyond the CG core, since the semantics of every extended feature is defined by its translation to core CGIF, whose semantics is defined by its translation to CL.

B.3 defines the concrete syntax of extended CGIF and the translation of each extended feature to core CGIF. This translation has the effect of specifying a function *CG*, which translates any sentence *s* of extended CGIF to a semantically equivalent sentence CG(*s*) of core CGIF. The combined functions *cg2cl*(CG(*s*)) translate *s* to a logically equivalent sentence in the CL abstract syntax.

The function CG and other functions for the other CGIF categories are defined by *transformation rules* whose notation is specified in B.1.4.1. Two categories, comment and reference, have identical syntax in core and extended CGIF; for any comment *cm* in extended CGIF, comment(*cm*)=*cm*; and for any reference *r* in extended CGIF, reference(*r*)=*r*. For any other category X of core CGIF, the strings of category X are a proper subset of the extended CGIF strings of the same category.

Since the definitions in B.2 specified the conceptual graph abstract syntax and its mapping to the abstract syntax of Common Logic, they used notation-independent constructs, such as sets. The definitions below specify the mapping from the concrete syntax of extended CGIF to the concrete syntax of core CGIF. Therefore, they are defined in terms of strings and functions that transform strings.

B.3.2   actor

Definition: A string *ac* that shall contain a comment *cm*, a reference *r* called the *type label*, an arc sequence s_1 called the *input arcs*, an arc sequence s_2 called the *output arcs*, and an optional end comment *ecm*. The output arcs s_2 shall not contain a sequence marker.

Translation: A conceptual graph *g*.

```
actor(?ac?) -> ?g?;
    actor  = "(", [comment] ?cm?, (["#", "?"], CGname) ?r?,
             arcSequence ?s1?, "|", {arc} ?s2?, [endComment] ?ecm?, ")";
    ?z1?   = first(arcSequence(?s1?));
    ?z2?   = first(arcSequence(?s2?));
    ?sqn?  = third(arcsequence(?s1?));
    if (length(?s2?)="0")
       ?cr? = "(", ?cm?, ?r?, ?z1?, ?sqn?, ?ecm?, ";0-output actor", ")";
    elif (length(?s2?)="1")
       ?cr? = "(", ?cm?, ?r?, ?z1?, ?sqn?, "|", ?z2?, ?ecm?, ")";
    else ?cr? = "(", ?cm?, ?r?, ?z1?, ?sqn?, "/*|*/", ?z2?, ?ecm?, ")";
    end;
    ?g?    = second(arcSequence(?s1?)), second(arcSequence(?s2?)), ?cr?;
    end;
```

If *s2* has no output arcs, *cr* shall be an ordinary conceptual relation, as defined in B.3.7; but to show that *cr* was derived from an actor, an end comment "0-output actor" is inserted. If *s2* has one output arc, *cr* shall be an actor, but *cr* differs from *ac* because the arcs are translated to core CGIF. If *s2* has two or more output arcs, *cr* shall be an ordinary conceptual relation, but the comment "/*|*/" is inserted to distinguish the input arcs from the output arcs. The final rewrite rule puts *cr* after any conceptual graphs derived from the arc sequences.

Comment: As an example, the combined effect of the transformation rules for actors, arcs, arc sequences, and concepts would translate the following actor node:

```
(IntegerDivide [Integer: *x] [Integer: 7] | *u *v)
```

to a six-node conceptual graph consisting of three concepts and three conceptual relations:

```
[*x] (Integer ?x) (Integer 7) [*u] [*v]
(IntegerDivide ?x 7 /*|*/ ?u ?v)
```

The comment /*|*/ has no semantic effect in core CGIF or CL, but if preserved, it would enable a mapping back to extended CGIF to distinguish the input arcs from the output arcs. If the distinction is important for some application, axioms may be used to state the functional dependencies of the outputs on the inputs. For example, the CL relation that results from the translation of an actor of type IntegerDivide would satisfy the following constraint stated in CLIF:

```
(exists (Quotient Remainder) (forall (x1 x2 x3 x4)
   (iff (IntegerDivide x1 x2 x3 x4)
        (and (= x3 (Quotient x1 x2)) (= x4 (Remainder x1 x2))))))
```

This sentence asserts that there exist functions Quotient and Remainder that determine the values of the third and fourth arguments of the relation IntegerDivide. The translation rules would not generate that axiom automatically, but it could be stated by a CGIF sentence that would be translated to the CLIF sentence:

```
[*Quotient] [*Remainder]
[[@every*x1] [@every*x2] [@every*x3] [@every*x4]
[Equiv: [Iff: (IntegerDivide ?x1 ?x2 | ?x3 ?x4)]
        [Iff: (#?Quotient ?x1 ?x2 | ?x3) (#?Remainder ?x1 ?x2 | ?x4)]]]
```

To show that the existential quantifiers for [*Quotient] and [*Remainder] take precedence over the universal quantifiers for the four arguments, a pair of context brackets is used to enclose the concept nodes with universal quantifiers.

B.3.3 arc

Definition: A string *ar* that shall contain an optional comment *cm* and either a reference *r*, a defining label with CG name *n*, or a concept *c*.

Translation: A pair (*x*,*g*) consisting of an arc *x* and a conceptual graph *g*.

```
arc(?ar?) -> ?x?, ?g?;
arc = [comment] ?cm?, (reference ?r? | "*", CGname ?n? | concept ?c?);
if   (?r?~= )  ?x?  = ?ar; ?g? = ;
elif (?n?~= )  ?x?  = ?cm?, "?", ?n?;  ?g? = "[*", ?n?, "]";
else           ?x?  = ?cm?, first(concept(?c?));
               ?g?  = third(concept(?c?));
end; end;
```

If *ar* is a reference, *x* shall be *ar* unchanged, and *g* shall be blank. If *ar* contains a defining label, *x* shall be the result of replacing the marker * in *ar* with ?, and *g* shall be the concept [*n]. If *ar* contains a concept *c*, *x* shall be the result of replacing the concept *c* in *ar* with a reference *r*, and *g* shall be third(concept(*c*)).

Comment: As an example, if the arc *ar* is [Integer], the value of concept([Integer]) would be a CG name, such as g00023, and arc([Integer]) would be the pair consisting of the reference ?g00023 and the conceptual graph [*g00023] (Integer ?g00023).

B.3.4 arcSequence

Definition: A string *as* that shall contain a sequence *s* of zero or more arcs followed by an optional sequence marker *sqn*.

Translation: A triple (*rs*,*g*,*sqn*) consisting of a sequence of references *rs*, a conceptual graph *g*, and the sequence marker *sqn*.

```
arcSequence(?as?) -> ?rs?, ?g?, ?sqn?;
arcSequence  =  {arc} ?s?, [[comment], "?", seqmark] ?sqn?;
?rs? = map(first,map(arc,?s?));
?g? = map(second,map(arc,?s?));
end;
```

Comment: The function map(arc,?s?) applies arc to each arc of *s* to generate a sequence of pairs consisting of a reference and a concept. Then map(first,map(arc,?s?)) extracts the sequence of references from the first element of each pair. Finally, map(second,map(arc,?s?)) extracts the sequence of concepts from the second element of each pair. The option of having a sequence marker in an arc sequence implies that a conceptual relation may have a variable number of arcs. An actor may have a variable number of input arcs, but the number of output arcs shall be fixed; therefore, the output arcs shall not have a sequence marker.

B.3.5 boolean

Definition: A string *b* that shall contain a context *bc*, which shall not directly contain a reference or a defining label. The context *bc* shall have either a prefix "~" and no type label or no prefix and one of the following constants as type label: Either, Equiv, Equivalence, If, Iff, Then.

Translation: A negation *ng* that shall be negation(*b*), eitherOr(*b*), ifThen(*b*), or equiv(*b*).

```
boolean  =  negation | eitherOr | ifThen | equiv;

negation(?b?) -> ?ng?;
negation  =  "~[", [comment] ?cm?, CG ?x?, [endComment] ?ecm?, "]";
?ng?  =  "~[", ?cm?, CG(?x?), ?ecm?, "]";
end;

ifThen(?b?) -> ?ng?;
ifThen  =  "[", [comment] ?cm1?, "If", [":"], CG ?ante?,
               "[", [comment] ?cm2?, "Then", [":"], CG ?conse?,
                   [endComment] ?ecm1?, "]", [endComment] ?ecm2?, "]";
?ng?    =  "~[", ?cm1?, CG(?ante?),
               "~[", ?cm2?, CG(?conse?), ?ecm1?, "]", ?ecm2?, "]";
end;

equiv(?b?) -> ?ng?;
equiv = "[", [comment] ?cm1?, ("Equiv" | "Equivalence"), [":"],
        "[", [comment] ?cm2?, "Iff", [":"], CG ?g1?,
            [endComment] ?ecm2? "]",
        "[", [comment] ?cm3?, "Iff", [":"], CG ?g2?,
            [endComment] ?ecm3? "]", [endComment] ?ecm1? "]";
?ng? = "[", ?cm1?, "~[", ?cm2?, CG(?g1?),
               "~[", CG(?g2?), "]", ?ecm2?, "]",
            ?cm2?, "~[", ?cm3?, CG(?g2?),
               "~[", CG(?g1?), "]", ?ecm3?, "]", ?ecm1?, "]";
end;

eitherOr(?b?) -> ?ng?;
eitherOr = "[", [comment] ?cm?, "Either", [":"],
               {[comment], nestedOrs} ?ors?, [endComment] ?ecm?, "]";
?ng?  =  "~[", ?cm?, nestedOrs(?ors?), ?ecm?, "]";
end;

nestedOrs(?ors?) -> ?g?;
nestedOrs  = ( "[", [comment] ?cm?, "Or" ?first?, [":"], CG ?ng?,
                   [endComment] ?ecm?, "]", nestedOrs ?more?
             | );
if (?first?= )  ?g? = ;
else ?g? = "~[", ?cm?, CG(?ng?), ?ecm?, "]", nestedOrs(?more?);
end; end;
```

The rule for nestedOrs recursively processes a sequence of zero or more Boolean contexts of type `Or`. If *b* contains zero nested Ors, `eitherOr(b)` shall be `~[  ]`, which is false; the corresponding CLIF sentence (or) is defined to be false.

Comment: The scope of quantifiers in any of the Boolean contexts shall be determined by the nesting of their translations to core CGIF. Any defining label in a context of type `If` shall have the nested context of type `Then` within its scope. For any two contexts directly contained in a context of type `Either`, `Equivalence`, or `Equiv`, neither one shall have the other within its scope.

B.3.6   concept

Definition: A string *c* consisting of four substrings, any or all of which may be omitted: an opening comment *cm*, a type field, a referent field, and an end comment *ecm*.

The referent field of *c* may contain a defining sequence label with sequence marker *sqn*. If so, the type field of *c* shall be empty, the defining sequence label may be preceded by "@every", and there shall not be any references or any conceptual graph in the referent field of *c*.

If no *sqn*, the type field of *c* shall contain either a type expression *tx* and a colon ":" or an optional reference *ty* called a *type label* and an optional colon ":". If no *sqn*, the referent field of *c* shall contain an optional defining label with CG name *df* (which may be preceded by "@every"), a sequence of zero or more references *rf*, and a conceptual graph *g*, which may be blank. If all the options are omitted, the concept *c* shall be the string "`[]`".

Translation: A triple (*r,q,g*) consisting of a reference or a bound sequence label *r*, a quantifier *q*, which shall be "@every" or the empty string, and a conceptual graph *g*, which shall contain at least one concept.

```
concept = "[", [comment] ?cm?,
            ( (typeExpression ?tx?, ":"
             | [["#" , "?"], CGname] ?ty?, [":"]),
              [["@every"] ?q?, "*", CGname ?df?], {reference} ?rf?, CG ?x?
             | ["@every"] ?q?, "*", seqmark ?sqn?
            ), [endComment] ?ecm?, "]";
  if (?sqn?~= )  ?r? = "?", ?sqn?; ?g1? = "[", ?cm?, "*", ?sqn?, ?ecm?];
  elif (?df?~= ) ?r? = "?", ?df?; ?g1? = "[", ?cm?, "*", ?df?, ?ecm?];
                if (?rf?~= ) ?g2? = "[", ":", ?r?, ?rf?, "]"; end;
  elif (?rf?~= ) ?r? = first(?rf?);
                ?g2? = "[", ?cm?, ":", ?rf?, ?ecm?, "]";
  else          ?df? = gensym(); ?r? = "?", ?df?;
                ?g1? = "[", ?cm?, "*", ?df?, ?ecm?, "]";
  end;
  if (?tx?~= )   ?b?  = first(typeExpression(?tx?));
                ?gx? = second(typeExpression(?tx?));
                ?g3? = substitute(?r?,?b?,?gx?);
  elif (?ty?~= ) ?g3? = "(", ?ty?, ?r?, ")"; end;
  if (?x?~= )   ?g4? = "[", CG(?x?), "]";
  end;
  ?g? = ?g1?, ?g2?, ?g3?, ?g4?;
  end;
```

Four options are permitted in the type field: a type expression *tx*, a bound coreference label prefixed with "#", a constant, or the empty string; a colon is required after *tx*, but optional after the other three. The rewrite rules move features from the concept *c* to four strings, which are concatenated to form the conceptual graph *g*: *g1* is an existential concept with the defining label from *c* or with a label generated by gensym() if no defining label or reference occurs in *c*; *g2* is a coreference concept if any references occur in *c*; *g3* is either a conceptual relation with a type label *ty* or a conceptual graph generated from a type expression *tx*; and *g4* is a context containing any nonblank CG *x*. Any comments *cm* and *ecm* are placed in the first nonblank concept, which shall be either *g1* or *g2*.

Comment: To illustrate the translation, the sentence *A pet cat Yojo is on a mat* could be represented in extended CGIF with two concept nodes in the arc sequence of a conceptual relation:

```
(On [@*x (Pet ?x) (Cat ?x): Yojo] [Mat])
```

To generate the equivalent core CGIF, the concepts are removed from the arc sequence. In their place, references are left to link them to the concepts, which are expanded by the above rewrite rules. The following is the resulting core CGIF:

```
[: Yojo] (Pet Yojo) (Cat Yojo)
[*g00238] (Mat ?g00238) (On Yojo ?g00238)
```

The CG name Yojo is the reference for the first concept, and the CG name g00238 for the mat is generated by gensym(). See B.3.9 for a discussion of the type expression and its translation. The translation by *cg2cl* would translate the core CGIF to the abstract syntax, which would be expressed by the following CLIF:

```
(exists (g00238) (and (= Yojo Yojo) (Pet Yojo) (Cat Yojo)
        (Mat ?g00238) (On Yojo ?g00238)))
```

A coreference concept with only one reference, such as [: Yojo], has no effect on the truth or falsity of the sentence. It could be deleted by an optimizing compiler, unless it is needed as a container for comments.

B.3.7 conceptual graph (CG)

Definition: A string *cg* consisting of an unordered sequence of substrings that represent concepts, conceptual relations, booleans, and comments.

Translation: A conceptual graph *g*.

```
CG(?cg?) -> ?g?;
CG  = {concept | conceptualRelation | boolean | comment};
if (first(sortCG(?cg?)~= )
     ?g?  =  "~", "[", first(sortCG(?cg?)),
             "~", "[", second(sortCG(?cg?), "]", "]";
else  ?g?  =  second(sortCG(?cg?));
end; end;
```

sortCG(*cg*) shall be the pair (*g1,g2*), where *g1* is the conceptual graph derived from all the universally quantified concepts in *cg* and *g2* is the conceptual graph derived from all other concepts, conceptual relations, and comments in *cg*.

```
sortCG(?cg?) -> ?g1?,?g2?;
sortCG = ( (concept ?c? | conceptualRelation ?x?
           | boolean ?x? | comment ?x?), sortCG ?rem?
          | );
if (?c?= ) ?cg2? = CG(?x?));
elif (second(concept(?c?)) = "@every")
           ?cg1? = third(concept(?c?));
else       ?cg2? = third(concept(?c?));
end;
?g1? = ?cg1?, first(sortCG(?rem?)); ?g2? = ?cg2?, second(sortCG(?rem?));
end;
```

Comment: If there are no concepts containing universal quantifiers in the input string, the result shall be a single string in core CGIF that concatenates the results of translating each node independently of any other node. But if the input string contains any universal concepts, the output string shall be a nest of two negations. The outer context shall contain the translations of all the universal concepts, and the inner context shall contain the translations of all other nodes in the input.

B.3.8 conceptual relation

Definition: A string *cr* that represents an ordinary conceptual relation or an actor.

Translation: A conceptual graph *g*, which shall be either ordinaryRelation(*cr*) or actor (*cr*).

```
conceptualRelation = ordinaryRelation | actor;

ordinaryRelation(?cr?) -> ?g?;
   ordinaryRelation  =  "(", [comment] ?cm?, (["#", "?"], CGname) ?r?,
                    arcSequence ?s?, [endComment] ?ecm?, ")";
   ?g?  =  second(arcSequence(?s?)),
        "(", ?cm?, ?r?, first(arcSequence(?s?)),
        third(arcSequence(?s?)), ?ecm?, ")";
   end;
```

The first line of the rewrite rule extracts a conceptual graph from the arc sequence *s*. The second line adds the opening comment, type label, and arc sequence of a conceptual relation. The third line adds the sequence marker, if any, the end comment, and the closing parenthesis of the conceptual relation.

Comment: As an example, the conceptual relation (On [Cat: Yojo] [Mat]) would be translated by the rules for conceptual relations, arcs, arc sequences, and concepts to generate a conceptual graph expressed in core CGIF, such as the following:

```
[: Yojo] (Cat Yojo) [*g00719] (Mat ?g00719) (On Yojo ?g00719)
```

B.3.9   text

Definition: A context *c* that is not contained directly or indirectly in any context.

Translation: A context *cx*.

```
text(?c?) -> ?cx?;
text = "[", [comment] ?cm?, "Proposition", ":", [CGname] ?n?,
       CG ?g?, [endComment] ?ecm?, "]";
?cx? = "[", ?cm?, "Proposition", ":", ?n?, CG(?g?), ?ecm?, "]";
end;
```

Comment: CGIF does not provide an explicit syntax for modules. Instead, any CL module shall first be translated to a text in core CLIF according to the specification in A.3. Then the result of that translation shall be translated to a text in extended CGIF according to the function *cl2cg*, which is defined in B.4.

B.3.10 type expression

Definition: A string *tx* containing a CG name *n* and a conceptual graph *g*.

Translation: A pair (*b*,*g*), consisting of a bound label *b* and a conceptual graph *g*.

```
typeExpression(?tx?) -> ?b?,?g?;
typeExpression  =  "@", "*", CGname ?n?, CG ?g?;
?b?  =  "?", ?n?;
end;
```

If a concept *c* contains a type expression, the rewrite rules that specify concept(*c*) use the function `substitute(?r?,?b?,?g?)` to substitute some reference *r* for every occurrence of *b* in *g*.

Comment: A type expression corresponds to a lambda expression in which the CG name *n* specifies the formal parameter, and the conceptual graph *g* is the body of the expression. If a concept *c* contains a type expression, the transformation rules that process *c* shall substitute a reference derived from *c* for every occurrence of the bound label ?*n* that occurs in *g*.

B.4   CGIF conformance

This annex has specified the syntax of three CL dialects: an abstract syntax for conceptual graphs, a concrete syntax for core CGIF, and a concrete syntax for extended CGIF. All three of these languages are fully conformant CL dialects in the sense that every CL sentence can be translated to a semantically equivalent sentence in each of them, and every sentence in any of these three dialects can be translated to a semantically equivalent sentence in CL. The semantic equivalence is established by definition: the semantics of every sentence in extended CGIF is defined by a translation to a sentence in core CGIF, the semantics of every sentence in core CGIF is defined by a translation to a sentence in the abstract CG syntax, and the semantics of every abstract CG sentence is defined by its translation to the abstract syntax of CL.

To demonstrate full conformance, B.4 specifies the function *cl2cg*, which shall translate any sentence s in CL to a sentence *cl2cg*(*s*) in extended CGIF, which shall have the same truth value as *s* under every interpretation for CL. For most CL expressions, the mapping to some expression in extended CGIF is straightforward. The translation of functional terms from CL to CGIF, however, requires more than one step. Any CL function application can be translated to an actor that represents the function plus a reference to some concept whose referent is the value of that function. In order to translate a sequence of CL terms to an arc sequence in extended CGIF, the actor node shall be enclosed inside the concept node.

As an example, let (F X1 X2) be a CLIF term with an operator F applied to arguments X1 and X2, where the names X1 and X2 are bound by quantifiers, but F is not. When that term is translated by *cl2cg*, the gensym() function shall be used to generate a CG name, such as g00592. When prefixed with "?", that name becomes a bound coreference label, which shall be used as the output arc of an actor that

represents the function F. The result of translating the original CLIF term by *cl2cg* shall be (F ?X1 ?X2 | ?g00592). The defining label *g00592 shall be placed in a concept, such as [*g00592], and the actor shall be placed inside that concept as a nested conceptual graph: [*g00592 (F X1 X2 | ?g00592)]. This concept shall be the result of *cl2cg* when applied to the functional term. It may appear as an arc in an arc sequence of some actor or conceptual relation.

Since the predicate of a CL relation or the operator of a CL function may be a functional term, the same transformation shall be used to translate the predicate or the operator to a concept. As an example, let ((F X1 X2) Y1 Y2) be a CLIF atomic sentence whose predicate is the same functional term that appeared in the previous example. Therefore, the bound label "?g00592", which represents the value of the function, shall be the type label of the corresponding conceptual relation. If both Y1 and Y2 are bound by quantifiers in CL, the conceptual relation shall be (#?g00592 ?Y1 ?Y2). In order to generate a single syntactic unit as the value of *cl2cg*, this conceptual relation shall be placed inside the concept that represents the functional term, immediately before "]": [*g00592 (F X1 X2 | ?g00592) (#?g00592 ?Y1 ?Y2)]. This concept shall be the result of *cl2cg* when applied to the original atomic sentence. It may appear as a node of a conceptual graph that results from the translation of a larger CL sentence that contains the original atomic sentence.

For every CL expression **E**, Table B.1 specifies the extended CGIF expression that defines *cl2cg*(**E**). In order to ensure that the CL constraints on quantifier scope are preserved in the translations by *cl2cg*, context brackets, "[" and "]", are used to enclose the translations for expressions of type E13 and E14. In some cases, these brackets are unnecessary, and they may be ignored.

The first column of Table B.1 indicates links to rows in Table 2. The second column uses the metalanguage and conventions used to define the CL abstract syntax. The third column mixes that metalanguage with the notation used for rewrite rules in B.1.4.2. That combination defines a function *cg2cl*, which translates any sentence *s* of core CGIF to a logically equivalent sentence *cg2cl*(*x*) of Common Logic.

Table B.1 — Mapping from CL abstract syntax to extended CGIF syntax

	If E is a CL expression of the form	Then *cl2cg*(E) =
E1	A numeral 'n'	The numeral 'n'
E1	A quoted string 's'	The quoted string 's'
E1	A interpretable name 'n'	The name 'n' shall be enclosed in quotes if it is not a CG identifier. If it occurs in the quantifier of some CL sentence, it shall be prefixed with "*". If it is bound by a quantifier, it shall be prefixed with "?".
E2	Sequence marker *S*	*S*
E3	A term sequence <T1 ... Tn> starting with a term T1	An arc sequence: *cl2cg*(T1) ... *cl2cg*(Tn)
E4	A term sequence T1 ... Tn starting with a sequence marker T1	An arc sequence: *cl2cg*(T2), ..., *cl2cg*(Tn), *cl2cg*(T1)
E5	A term (O T1 ... Tn)	A concept with a generated name 'n' that contains a nested actor: "[", "*", 'n', "(", *cl2cg*(O), *cl2cg*(T1, ... Tn), ")", "|", "?", 'n', ")", "]"
	A term (cl:comment 'string' T)	An arc with a comment: "/*", 'string', "*/", *cg2cl*(T)

Table B.1 *(continued)*

	If E is a CL expression of the form	Then *cl2cg*(E) =
E6	An equation (= T1 T2)	A CG consisting of one, two, or three concepts
		If both T1 and T2 are names, one concept: "[:", *cl2cg*(T1), *cl2cg*(T2), "]"
		If both T1 and T2 are functional terms, three concepts: *cg2cl*(T1), *cg2cl*(T2), "[", "?", 'n1', "?", 'n2', "]" where 'n1' is the name generated for T1 and 'n2' is the name generated for T2
		If Ti is a functional term (where i=1 or i=2) and the other term Tj is a name, two concepts: *cl2cg*(Ti), "[", "?", 'ni', *cl2cg*(Tj), "]" where 'ni' is the name generated for Ti
E7	An atomic sentence (P T1 … Tn)	A CG consisting of either a conceptual relation or a concept
		If P is a name, a conceptual relation: "(", *cl2cg*(P), *cl2cg*(T1 …Tn), ")"
		If P is a functional term, a concept: *cl2cg*(P) as modified by inserting the following conceptual relation immediately before the closing "]": "(", 'n', *cl2cg*(T1 … Tn), ")" where 'n' is the name generated for *cl2cg*(P)
E8	A Boolean sentence (not P)	A negation: "~", "[", *cl2cg*(P), "]"
E9	A Boolean sentence (and P1 … Pn)	A CG: *cl2cg*(P1), …, *cl2cg*(Pn)
E10	A Boolean sentence (or P1 … Pn)	A CG: "[", "Either", "[", "Or", *cl2cg*(P1), "]", …, "[", *cl2cg*(Pn), "]", "]"
E11	A Boolean sentence (if P Q)	A CG: "[", "If", *cl2cg*(P), "[", "Then", *cl2cg*(Q), "]", "]"
E12	A Boolean sentence (iff P Q)	A CG: "[", "Equiv", ":", "[", "Iff", *cl2cg*(P), "]", "[", "Iff", *cl2cg*(Q), "]", "]"
	A sentence (cl:comment 'string' P)	A comment and a CG: "/*", 'string', "*/", *cl2cg*(P)
E13	A quantified sentence (forall (N1 … Nn) B) where N1 to Nn are names or sequence markers	A CG: "[", "[", "@every", "*", *cl2cg*(N1), "]", …, "[", "@every", "*", *cl2cg*(Nn), "]", *cl2cg*(B), "]"
E14	A quantified sentence (exists (N1 … Nn) B) where N1 to Nn are names or sequence markers	A CG: "[", "[", "*", *cl2cg*(N1), "]", …, "[", "*", *cl2cg*(Nn), "]", *cl2cg*(B), "]"
	A statement (cl:comment "string")	A comment: "/*", 'string', "*/"
E17	A statement (cl:imports N)	A concept: "[", "cg_Imports", *cl2cg*(N), "]"
E18	A module with name N, exclusion list N1 … Nn, and text T	If M is the translation to core CL specified in A.3, then a text: "[", "Proposition", ":", *cl2cg*(M), "]"
E19	A statement (cl:text T1 … Tn)	A text: "[", "Proposition", *cl2cg*(T1 … Tn), "]"
E20	(cl:text N T1 …Tn)	A text: "[", "Proposition", ":", *cl2cg*(N), *cg2cl*(T1 … Tn), "]"

To specify the translation from extended CGIF to core CGIF, B.3 uses a combination of EBNF syntax rules plus the rewrite rules specified in B.1.4.2 to define a function ex2cor, which translates any sentence *s* of extended CGIF to a logically equivalent sentence CG(*s*) of core CGIF.