

# INTERNATIONAL STANDARD

ISO  
8731-2

First edition  
1987-12-15



INTERNATIONAL ORGANIZATION FOR STANDARDIZATION  
ORGANISATION INTERNATIONALE DE NORMALISATION  
МЕЖДУНАРОДНАЯ ОРГАНИЗАЦИЯ ПО СТАНДАРТИЗАЦИИ

## Banking — Approved algorithm for message authentication —

### Part 2 : Message authenticator algorithms

*Banque — Algorithmes approuvés pour l'authentification des messages —*

*Partie 2 : Algorithme d'authentification des messages*

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Reference number  
ISO 8731-2:1987 (E)

## Foreword

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Draft International Standards adopted by the technical committees are circulated to the member bodies for approval before their acceptance as International Standards by the ISO Council. They are approved in accordance with ISO procedures requiring at least 75 % approval by the member bodies voting.

International Standard ISO 8731-2 was prepared by Technical Committee ISO/TC 68, *Banking and related financial services*.

Users should note that all International Standards undergo revision from time to time and that any reference made herein to any other International Standard implies its latest edition, unless otherwise stated.

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# Banking — Approved algorithm for message authentication —

## Part 2 : Message authenticator algorithms

### 1 Scope and field of application

ISO 8731 specifies, in individual parts, approved authentication algorithms i.e. approved as meeting the authentication requirements specified in ISO 8730. This part of ISO 8731 deals with the Message Authenticator Algorithm for use in the calculation of the Message Authentication Code (MAC).

The Message Authenticator Algorithm (MAA) is specifically designed for high speed authentication using a mainframe computer. This is a special purpose algorithm to be used where data volumes are high, and efficient implementation by software a desirable characteristic. MAA is also suitable for use with a programmable calculator.

Test examples are given in an annex, which does not form part of this International Standard.

### 2 Reference

ISO 8730, *Banking — Requirements for message authentication (wholesale)*.

### 3 Brief description

#### 3.1 General

The Message Authenticator Algorithm works on the principle of a Message Authentication Code (or MAC), a number sent with a message, so that a check can be made by the receiver of the message that it has not been altered since it left the sender.

#### 3.2 Technical

All numbers manipulated in this algorithm shall be regarded as 32-bit unsigned integers, unless otherwise stated. For such a number  $N$ ,  $0 < N < 2^{32}$ . This algorithm can be implemented conveniently and efficiently in a computer with a word length of 32 bits or more.

Messages to be authenticated may originate as a bit string of any length. They shall be input to the algorithm as a sequence of 32 bit numbers,  $M_1, M_2 - M_n$ , of which there are  $n$ , called message blocks. The detail of how to pad out the last block  $M_n$

to 32 bits is not part of the algorithm but shall be defined in any application. This algorithm shall not be used to authenticate messages with more than 1 000 000 blocks, i.e.  $n < 1\,000\,000$ .

The key shall comprise two 32 bit numbers J and K and thus has a size of 64 bits.

The result of the algorithm is a 32 bit authenticator value denoted Z. The calculation can be performed on messages as short as one block ( $n = 1$ ).

The calculation has three parts

- a) The prelude shall be a calculation made with the keys (J and K) alone and it shall generate six numbers  $X_0, Y_0, V_0, W, S$  and T which shall be used in the subsequent calculations. This part need not be repeated until a new key is installed.
- b) The main loop is a calculation which shall be repeated for each message block  $M_i$  and therefore, for long messages, dominates the calculation.
- c) The coda shall consist of two operations of the main loop, using as its message blocks the two numbers S and T in turn, followed by a simple calculation of Z, the authenticator.

The mode of operation (see clause 5) is an essential feature of the implementation of this algorithm.

The figure shows the data flow in schematic form.

## 4 The algorithm

### 4.1 Definition of the functions used in the algorithm

#### 4.1.1 General definitions

A number of functions are used in the description of the algorithm. In the following, X and Y are 32 bit numbers and the result is a 32 bit number except where stated otherwise.

- |          |  |
|----------|--|
| CYC(X)   | is the result of a one-bit cyclic left shift of X.                         |
| AND(X,Y) | is the result of the logical AND operation carried out on each of 32 bits. |

- OR(X,Y) is the result of the logical OR operation carried out on each of 32 bits.
- XOR(X,Y) is the result of the XOR operation (modulo 2 addition) carried out on each of 32 bits.
- ADD(X,Y) is the result of adding X and Y discarding any carry from the 32nd bit, that is to say, addition modulo  $2^{32}$ .
- CAR(X,Y) is the value of the carry from the 32nd bit when X is added to Y; it has the value 0 or 1.
- MUL1(X,Y), MUL2(X,Y) and MUL2A(X,Y) are three different forms of multiplication, each with a 32 bit result.

**4.1.2 Definition of multiplication functions**

To explain the multiplications, let the 64 bit product of X and Y be [U,L]. Here the square brackets mean that the values enclosed are concatenated, U on the left of L. Hence U is the upper (most significant) half of the product and L the lower (least significant) half.

**4.1.2.1 To calculate MUL1(X,Y)**

Multiply X and Y to produce [U,L]. With S and C as local variables,

- S := ADD(U,L); ... (1)
- C := CAR(U,L); ... (2)
- MUL1(X,Y) := ADD(S,C). ... (3)

That is to say, U shall be added to L with end around carry.

Numerically the result is congruent to  $X*Y$ , the product of X and Y, modulo  $(2^{32} - 1)$ . It is not necessarily the smallest residue because it may equal  $2^{32} - 1$ .

**4.1.2.2 To calculate MUL2(X,Y)**

This form of multiplication shall not be used in the main loop, only in the prelude. With D, E, F, S and C as local variables,

- D := ADD(U,U); ... (4)
- E := CAR(U,U); ... (5)
- F := ADD(D,2E); ... (6)
- S := ADD(F,L); ... (7)
- C := CAR(F,L); ... (8)
- MUL2(X,Y) := ADD(S,2C). ... (9)

Numerically the result is congruent to  $X*Y$ , the product of X and Y, modulo  $(2^{32} - 2)$ . It is not necessarily the smallest residue because it may equal  $2^{32} - 1$  or  $2^{32} - 2$ .

**4.1.2.3 To calculate MUL2A(X,Y)**

This is a simplified form of MUL2(X,Y) used in the main loop, which yields the correct result only when at least one of the numbers X and Y has a zero in its most significant bit.

This form of multiplication is employed for economy in processing. D, S, C are local variables.

- D := ADD(U,U); ... (10)
- S := ADD(D,L); ... (11)
- C := CAR(D,L); ... (12)
- MUL2A(X,Y) := ADD(S,2C). ... (13)

The result is congruent to  $X*Y$  modulo  $(2^{32} - 2)$  under the conditions stated because, in the notation of MUL2(X,Y) above, the carry E = 0.

**4.1.3 Definition of the functions BYT[X,Y] and PAT[X,Y]**

A procedure is used in the prelude to condition both the keys and the results in order to prevent long strings of ones or zeros. It produces two results which are the conditioned values of X and Y and a number PAT[X,Y] which records the changes that have been made. PAT[X,Y] < 255 so it is essentially an 8 bit number.

X and Y are regarded as strings of bytes. Using the notation [X,Y,...] for concatenating,

$[X,Y] = [B_0, B_1, B_2, B_3, B_4, B_5, B_6, B_7]$

Thus bytes  $B_0$  to  $B_3$  are derived from X and  $B_4$  to  $B_7$  from Y.

The procedure is best described by a procedure where each byte  $B_i$  is regarded as an integer of length 8 bits.

```
begin
P := 0;
for i := 0 to 7 do
begin
P := 2*P;
if B[i] = 0 then
begin
P := P + 1;
B'[i] := P
end
else if B[i] = 255 then
begin
P := P + 1;
B'[i] := 255 - P
end
end
else
B'[i] := B[i];
end
end;
```

NOTE — The procedure is written in the programming language PASCAL (see ISO 7185), except that the non-standard identifier B' has been used to maintain continuity with the text. The symbols B[i] and B'[i] correspond to B<sub>i</sub> and B'<sub>i</sub> in the text.

The results are

$$\text{BYT}[X,Y] = [B'_0, B'_1, B'_2, B'_3, B'_4, B'_5, B'_6, B'_7]$$

and

$$\text{PAT}[X,Y] = P$$

## 4.2 Specification of the algorithm

### 4.2.1 The prelude

$$\begin{aligned} [J_1, K_1] &:= \text{BYT}[J, K]; \\ P &:= \text{PAT}[J, K]; \\ Q &:= (1 + P) * (1 + P). \end{aligned} \quad \dots (14)$$

First, by means of a calculation using J<sub>1</sub>, produce H<sub>4</sub>, H<sub>6</sub>, and H<sub>8</sub> from which X<sub>0</sub>, V<sub>0</sub> and S are derived.

$$\begin{aligned} J_{1_2} &:= \text{MUL1}(J_1, J_1); & J_{2_2} &:= \text{MUL2}(J_1, J_1); \\ J_{1_4} &:= \text{MUL1}(J_{1_2}, J_{1_2}); & J_{2_4} &:= \text{MUL2}(J_{2_2}, J_{2_2}); \\ J_{1_6} &:= \text{MUL1}(J_{1_2}, J_{1_4}); & J_{2_6} &:= \text{MUL2}(J_{2_2}, J_{2_4}); \\ J_{1_8} &:= \text{MUL1}(J_{1_2}, J_{1_6}); & J_{2_8} &:= \text{MUL2}(J_{2_2}, J_{2_6}). \end{aligned} \quad \dots (15)$$

$$\begin{aligned} H_4 &:= \text{XOR}(J_{1_4}, J_{2_4}); \\ H_6 &:= \text{XOR}(J_{1_6}, J_{2_6}); \\ H_8 &:= \text{XOR}(J_{1_8}, J_{2_8}). \end{aligned} \quad \dots (16)$$

From a similar calculation using K<sub>1</sub>, produce H<sub>5</sub>, H<sub>7</sub> and H<sub>9</sub>, from which Y<sub>0</sub>, W and T are derived.

$$\begin{aligned} K_{1_2} &:= \text{MUL1}(K_1, K_1); & K_{2_2} &:= \text{MUL2}(K_1, K_1); \\ K_{1_4} &:= \text{MUL1}(K_{1_2}, K_{1_2}); & K_{2_4} &:= \text{MUL2}(K_{2_2}, K_{2_2}); \\ K_{1_5} &:= \text{MUL1}(K_1, K_{1_4}); & K_{2_5} &:= \text{MUL2}(K_1, K_{2_4}); \\ K_{1_7} &:= \text{MUL1}(K_{1_2}, K_{1_5}); & K_{2_7} &:= \text{MUL2}(K_{2_2}, K_{2_5}); \\ K_{1_9} &:= \text{MUL1}(K_{1_2}, K_{1_7}); & K_{2_9} &:= \text{MUL2}(K_{2_2}, K_{2_7}). \end{aligned} \quad \dots (17)$$

$$\begin{aligned} H' &:= \text{XOR}(K_{1_5}, K_{2_5}); \\ H_5 &:= \text{MUL2}(H', Q); \\ H_7 &:= \text{XOR}(K_{1_7}, K_{2_7}); \\ H_9 &:= \text{XOR}(K_{1_9}, K_{2_9}). \end{aligned} \quad \dots (19)$$

Finally, condition the results using the BYT function

$$\begin{aligned} [X_0, Y_0] &:= \text{BYT}[H_4, H_5]; \\ [V_0, W] &:= \text{BYT}[H_6, H_7]; \\ [S, T] &:= \text{BYT}[H_8, H_9]. \end{aligned} \quad \dots (20)$$

### 4.2.2 The main loop

This loop shall be performed in turn for each of the message blocks M<sub>i</sub>. In addition to M<sub>i</sub>, the principal values employed shall be X and Y and the main results shall be the new values of X and Y. It shall also use V and W and modify V at each performance. X, Y and V shall be initialized with the values provided by the prelude. In order to use the same keys again, the initial values of X, Y and V shall be preserved, therefore they shall be denoted X<sub>0</sub>, Y<sub>0</sub> and V<sub>0</sub> and there shall be an initializing step X := X<sub>0</sub>, Y := Y<sub>0</sub>, V := V<sub>0</sub>, after which the main loop shall be entered for the first time. The coda, which shall be used after all message blocks have been processed by n cycles of the loop, is described in 4.2.3.

NOTE — The program is shown in columns to clarify its parallel operation but it should be read in normal reading order, left to right on each line.

$$\begin{aligned} V &:= \text{CYC}(V); \\ E &:= \text{XOR}(V, W); \end{aligned} \quad \dots (21)$$

$$X := \text{XOR}(X, M_i); \quad Y := \text{XOR}(Y, M_i); \quad \dots (22)$$

$$\begin{aligned} F &:= \text{ADD}(E, Y); & G &:= \text{ADD}(E, X); \\ F &:= \text{OR}(F, A); & G &:= \text{OR}(G, B); \end{aligned} \quad \dots (23)$$

$$\begin{aligned} F &:= \text{AND}(F, C); & G &:= \text{AND}(G, D); \\ X &:= \text{MUL1}(X, F); & Y &:= \text{MUL2A}(Y, G). \end{aligned} \quad \dots (24)$$

The numbers A, B, C, D are constants which are, in hexadecimal notation :

$$\begin{aligned} \text{Constant A} &: 0204 \quad 0801 \\ \text{Constant B} &: 0080 \quad 4021 \\ \text{Constant C} &: BFEF \quad 7FDF \\ \text{Constant D} &: 7DFE \quad FBFF \end{aligned}$$

NOTE — Lines (21) are common to both paths. Line (22) introduces the message block M<sub>i</sub>. Lines (23) prepare the multipliers and line (24) generates new X and Y values. Only X, Y and V are modified for use in the next cycle. F and G are local variables. Since the constant D has its most significant digit zero, G < 2<sup>31</sup> and this ensures that MUL2A in line (24) will give the correct result.

### 4.2.3 The coda

After the last message block M<sub>n</sub> has been processed, the main loop shall be performed with message block S, then again with block T, i.e. M<sub>n+1</sub> = S, M<sub>n+2</sub> = T.

After this, the Message Authentication Code (MAC) shall be calculated as Z = XOR(X, Y) and the algorithm shall then be complete.

NOTE — In order to calculate further MAC values without repeating the prelude (key calculation) until the keys are changed the values X<sub>0</sub>, Y<sub>0</sub>, V<sub>0</sub>, W, S and T should be retained.

## 5 Specification of the mode of operation

Messages longer than 1 024 bytes shall be divided into blocks of 1 024 bytes and chained as follows.

For the first block of 1 024 bytes the MAC (4 bytes) shall be formed. The MAC value shall be prefixed to (but not transmitted in) the second block and the resultant 1 028 bytes authenticated. This procedure shall continue, with the MAC of each block prefixed to the next, until the last block, which need not be of size 1 024 bytes, and the final MAC shall be used as the transmitted MAC for the whole message.

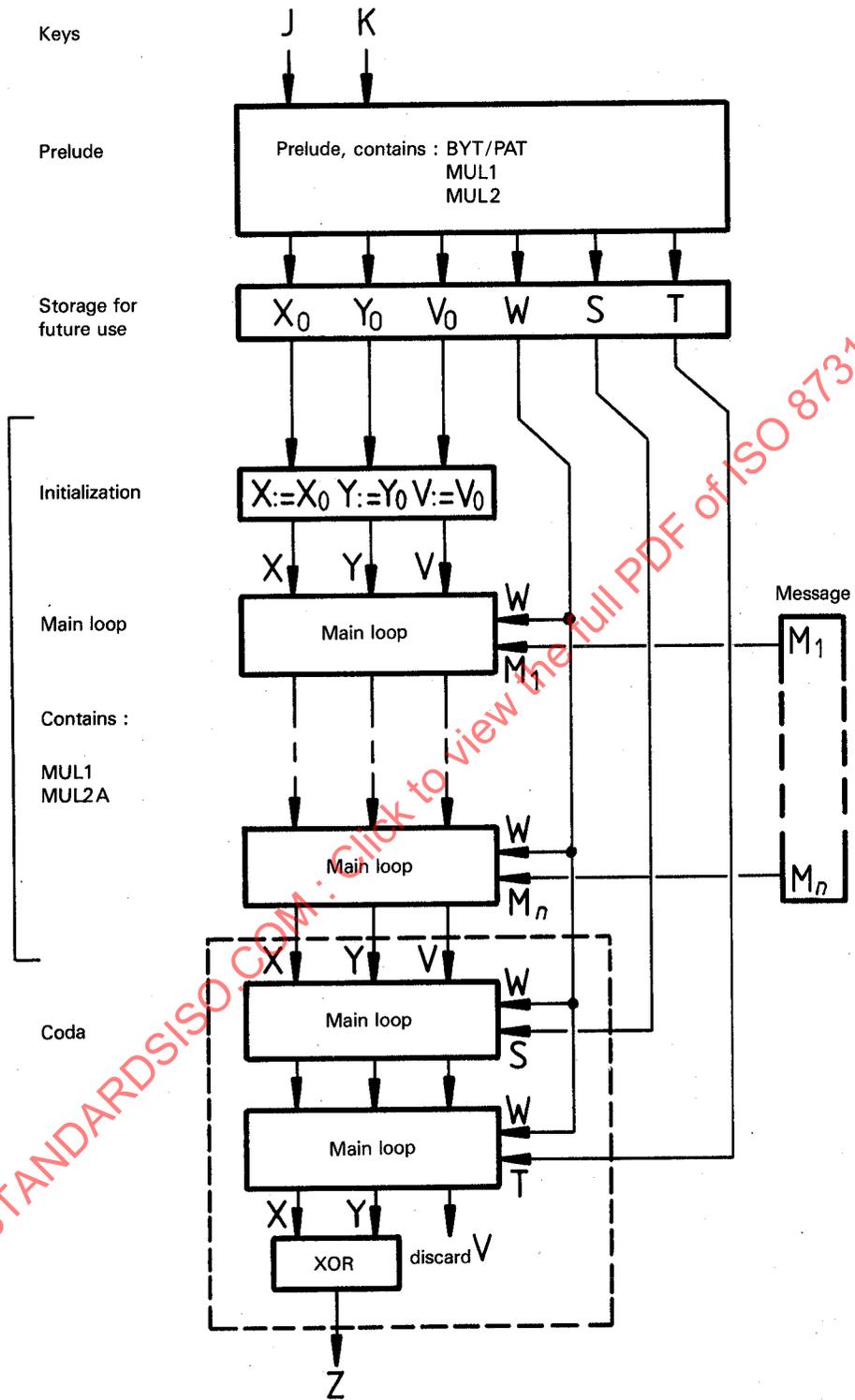


Figure — Schematic showing data flow

## Annex

### Test examples for implementation of the algorithm

(This annex does not form part of this Standard.)

#### A.0 Introduction

For most parts of the algorithm, simple test examples are given. The data used are not always realistic, i.e. they are not values which could be produced by earlier parts of the algorithm, and artificial values of constants are used. This is done to keep the test cases so simple that they can be verified by a pencil and paper calculation and thus the verification of the algorithm's implementations does not consist of comparing one machine implementation with another. The parts thus tested are

- MUL1, MUL2, MUL2A;
- BYT[X,Y] and PAT[X,Y];
- Prelude, except the initial BYT[J,K] operation;
- Main loop.

The coda is not tested separately because it uses only the main loop and one XOR function. For testing the whole algorithm, some results from a trial implementation are given.

#### A.1 Test examples for MUL1, MUL2, MUL2A

It is suggested that the multiplication operations should be tested with very small numbers and very large numbers. To represent a large number these examples use the ones complement. Thus if  $a$  is a small number (say less than 4 096) the notation  $\bar{a}$  is used to mean its complement, i.e.  $2^{32} - 1 - a$ .

For small numbers  $a$  and  $b$ , all three multiplication functions produce their true product  $a*b$ . When large numbers are used the functions can give different results. They should be tested both ways round, with MUL(x,y) and MUL(y,x) to verify that these are equal.

##### A.1.1 Test cases for MUL1

In modulo  $(2^{32} - 1)$  arithmetic  $\bar{a}$  is effectively  $-a$ , therefore the results are very simple

$$\text{MUL1}(\bar{a}, b) = \text{MUL1}(a, \bar{b}) = \overline{a*b}$$

$$\text{MUL1}(\bar{a}, \bar{b}) = a*b$$

Examples for testing are given in table 1.

##### A.1.2 Test cases for MUL2

$$\text{MUL2}(\bar{a}, b) = \overline{a*b - b + 1}$$

$$\text{MUL2}(a, \bar{b}) = \overline{a*b - a + 1}$$

$$\text{MUL2}(\bar{a}, \bar{b}) = a*b - a - b + 1$$

Examples for testing are given in table 1.

##### A.1.3 Test cases for MUL2A

This will give the same result as MUL2 when tested with numbers within its range. For testing with large numbers,  $\bar{a}$  and  $\bar{b} - 2^{31}$  shall be used

$$\text{MUL2A}(\bar{a}, b) = \overline{a*b - b + 1}$$

$$\text{MUL2A}(a, \bar{b}) = \overline{a*b - a + 1}$$

$$\text{MUL2A}(\bar{a}, \bar{b} - 2^{31}) = 2^{31} * (1 - p) + a*b + p - b - 1$$

where  $p$  is the parity of  $a$ ; the value of its least significant bit.

That is, for even values of  $a$  the result is  $2^{31} + a*b - b - 1$  and for odd values of  $a$  the result is  $a*b - b$ .

Examples for testing are given in table 1.

Table 1 — Test cases for multiplication functions (hexadecimal)

Function	a	b	Result
MUL1	0000 000F	0000 000E	0000 00D2
	FFFF FFF0	0000 000E	FFFF FF2D
	FFFF FFF0	FFFF FFF1	0000 00D2
MUL2	0000 000F	0000 000E	0000 00D2
	FFFF FFF0	0000 000E	FFFF FF3A
	FFFF FFF0	FFFF FFF1	0000 00B6
MUL2A	0000 000F	0000 000E	0000 00D2
	FFFF FFF0	0000 000E	FFFF FF3A
	7FFF FFF0	FFFF FFF1	8000 00C2
	FFFF FFF0	7FFF FFF1	0000 00C4

## A.2 Test examples for BYT and PAT

Three cases for testing these functions are listed in table 2.

Table 2 — Test cases for the BYT and PAT functions

Function	X	Y
[X,Y]	00 00 00 00	00 00 00 00
BYT[X,Y]	01 03 07 0F	1F 3F 7F FF
PAT[X,Y]	FF	
[X,Y]	FF FF 00 FF	FF FF FF FF
BYT[X,Y]	FE FC 07 F0	E0 C0 80 00
PAT[X,Y]	FF	
[X,Y]	AB 00 FF CD	FF EF 00 01
BYT[X,Y]	AB 01 FC CD	F2 EF 35 01
PAT[X,Y]	6A	

**A.3 Test examples for the prelude**

An example is given in table 3. The initial BYT[J,K] operation is not tested. It is assumed that the results from lines (14) are

$$J_1 = 0000\ 0100, \quad K_1 = 0000\ 0080, \quad P = 1.$$

**Table 3 — Test cases for lines (15) to (20) of the prelude**

J1 <sub>2</sub>	0001 0000	J2 <sub>2</sub>	0001 0000
J1 <sub>4</sub>	0000 0001	J2 <sub>4</sub>	0000 0002
J1 <sub>6</sub>	0001 0000	J2 <sub>6</sub>	0002 0000
J1 <sub>8</sub>	0000 0001	J2 <sub>8</sub>	0000 0004
H <sub>4</sub>		0000 0003	
H <sub>6</sub>		0003 0000	
H <sub>8</sub>		0000 0005	
K1 <sub>2</sub>	0000 4000	K2 <sub>2</sub>	0000 4000
K1 <sub>4</sub>	1000 0000	K2 <sub>4</sub>	1000 0000
K1 <sub>5</sub>	0000 0008	K2 <sub>5</sub>	0000 0010
K1 <sub>7</sub>	0002 0000	K2 <sub>7</sub>	0004 0000
K1 <sub>9</sub>	8000 0000	K2 <sub>9</sub>	0000 0002
H'		0000 0018	
H <sub>5</sub>		0000 0060 (Q = 4)	
H <sub>7</sub>		0006 0000	
H <sub>9</sub>		8000 0002	
[X <sub>0</sub> , Y <sub>0</sub> ]	0103 0703 1D3B 7760	PAT[X <sub>0</sub> , Y <sub>0</sub> ]	EE (1110 1110)
[V <sub>0</sub> , W]	0103 050B 1706 5DBB	PAT[V <sub>0</sub> , W]	BB (1011 1011)
[S, T]	0103 0705 8039 7302	PAT[S, T]	E6 (1110 0110)

The PAT values obtained from conditioning the results of the prelude are quoted for checking purposes but are not used in the algorithm.

**A.4 Test examples for the main loop**

In table 4, three examples of single block messages are given, using small and large numbers with the convention that  $\bar{a}$  is  $2^{32} - 1 - a$ . In the third example there are two cases of large numbers which must have zero in the 32nd bit, shown as  $\bar{2} - 2^{31}$  and  $\bar{3} - 2^{31}$  respectively. They could have been written  $2^{31} - 2$  and  $2^{31} - 3$  respectively. In order to keep the numbers small, artificial values of the constants A, B, C and D are used. Three single block examples are followed by a message of three blocks, in order to check that the implementation correctly retains the value of X, Y and W. The final S and T cycles of the coda are not included in this table.

**Table 4 — Test cases for the main loop (decimal)**

Single block messages					Three-block message									
A	B	4	1	1	4	1	2	2	1					
C	D	8	4	6	3	1	2*	4	4	4	4			
V	W	3	3	3	3	7	7	1	1	2	1			
X <sub>0</sub>	Y <sub>0</sub>	2	3	2	3	2	3	1	2	3	2	20	9	
M		5		1		8		0		1		2		
V		6		6		14		2		4		8		CYC
E		5		5		9		3		5		9		XOR
X	Y	7	6	3	2	10	11	1	2	2	3	22	11	XOR
F	G	11	12	2	1	2	1	5	4	8	7	20	31	ADD
F	G	15	13	3	5	2	1	7	5	10	7	22	31	OR
F	G	7	9	1	4	3	3*	3	1	10	3	18	27	AND
X	Y	49	54	3	5	30	30	3	2	20	9	396	297	MUL
Z		7		6		0		1		29		165		XOR

\* - 2<sup>31</sup>

**A.5 Test examples for the whole algorithm**

Using the original implementation of the algorithm, the four test examples with two block messages given in table 5 were calculated. For ease of checking, intermediate results are tabulated : the results of the prelude and the X and Y values after each operation of the main loop, that is for  $M_1$ ,  $M_2$ , S and T.

**Table 5 – Test cases for the whole algorithm**

J	00FF	00FF	00FF	00FF	5555	5555	5555	5555
K	0000	0000	0000	0000	5A35	D667	5A35	D667
P		FF		FF		00		00
$X_0$	4A64	5A01	4A64	5A01	34AC	F886	34AC	F886
$Y_0$	50DE	C930	50DE	C930	7397	C9AE	7397	C9AE
$V_0$	5CCA	3239	5CCA	3239	7201	F4DC	7201	F4DC
W	FECC	AA6E	FECC	AA6E	2829	040B	2829	040B
$M_1$	5555	5555	AAAA	AAAA	0000	0000	FFFF	FFFF
X	48B2	04D6	6AEB	ACF8	2FD7	6FFB	8DC8	BBDE
Y	5834	A585	9DB1	5CF6	550D	91CE	FE4E	5BDD
$M_2$	AAAA	AAAA	5555	5555	FFFF	FFFF	0000	0000
X	4F99	8E01	270E	EDAF	A70F	C148	CBC8	65BA
Y	BE9F	0917	B814	2629	1D10	D8D3	0297	AF6F
S	51ED	E967	51ED	E967	9E2E	7B36	9E2E	7B36
X	3449	25FC	2990	7CD8	B1CC	1CC5	3CF3	A7D2
Y	DB91	02B0	BA92	DB12	29C1	485F	160E	E9B5
T	24B6	6FB5	24B6	6FB5	1364	7149	1364	7149
X	277B	4B25	28EA	D8B3	288F	C786	D048	2465
Y	D636	250D	81D1	0CA3	9115	A558	7050	EC5E
Z	F14D	6E28	A93B	D410	B99A	62DE	A018	C83B

A further set of test cases for the whole algorithm is given in table 6. The J and K values were chosen to give long strings of zeros after conditioning. The message consists of 20 blocks of zeros. Intermediate values of X and Y are listed as well as the final authenticator value Z.

$$J = 8001\ 8001, K = 8001\ 8000 \text{ (all message blocks are zeros)}$$

**Table 6 – Test case for a 20 block message**

Block	X	Y	Z
1	303F F4AA	1277 A6D4	
2	55DD 063F	4C49 AAEO	
3	51AF 3C1D	5BC0 2502	
4	A44A AAC0	63C7 0DBA	
5	4D53 901A	2E80 AC30	
6	5F38 EEF1	2A60 91AE	
7	F023 9DD5	3DD8 1AC6	
8	EB35 B97F	9372 CDC6	
9	4DA1 24A1	C6B1 317E	
10	7F83 9576	74B3 9176	
11	11A9 D254	D786 34BC	
12	D880 4CA5	FDC1 A8BA	
13	3F6F 7248	11AC 46B8	
14	ACBC13DD	33D5 A466	
15	4CE9 33E1	C21A 1846	
16	C1ED 90DD	CD95 9B46	
17	3CD5 4DEB	613F 8E2A	
18	BBA57835	07C7 2EAA	
19	D784 3FDC	6AD6 E8A4	
20	5EBA 06C2	9189 6CFA	
S	1D9C 9655	98D1 CC75	
T	7BC1 80AB	A0B8 7B77	DB79 FBDC