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Space environment (natural and artificial) — Model of the Earth's magnetospheric magnetic field

Environnement spatial (naturel et artificiel) — Modèle du champ magnétique de la magnétosphère de la terre

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Foreword

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The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular, the different approval criteria needed for the different types of ISO documents should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2 (see www.iso.org/directives).

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This document was prepared by Technical Committee ISO/TC 20, *Aircraft and space vehicles*, Subcommittee SC 14, *Space systems and operations*.

This second edition cancels and replaces the first edition (ISO 22009:2009), which has been technically revised.

The main changes are as follows:

— upgraded list of the relevant models;

— added connection with the IGRF geomagnetic model;

— added field-aligned currents;

— added data availability information;

— added information about magnetospheric current systems modelling.

Any feedback or questions on this document should be directed to the user's national standards body. A complete listing of these bodies can be found at www.iso.org/members.html.

Introduction

This document describes the main requirements to the Earth's magnetospheric magnetic field model. A model satisfying the set of requirements is described in Annexes A and B as a working example. The model can be used in scientific and engineering applications and is intended to calculate the magnetic induction field generated from a variety of current systems located on the boundaries and within the boundaries of the Earth's magnetosphere under a wide range of environmental conditions, quiet and disturbed, affected by solar-terrestrial interactions simulated by solar activity such as solar flares and related phenomena which induce terrestrial magnetic disturbances such as magnetic storms.

The main goals of standardisation of the Earth's magnetospheric magnetic field are:

— providing the unambiguous presentation of the magnetic field in the Earth's magnetosphere;

— providing compatibility of results of interpretation and analysis of space experiments;

— providing less labour-consuming character of calculations of the magnetic field of magnetospheric currents in the space at geocentric distances of 1,0 to 6,6 Earth's radii (R_E);

— providing the most reliable calculations of all elements of the geomagnetic field in the space environment.

The magnetic field model presented in the Annex A (general description) and Annex B (submodels) can be used to forecast radiation situation in the space, including the periods of intense magnetic disturbances (magnetic storms) when developing systems of spacecraft magnetic orientation, when forecasting the influence of magnetic disturbances on transcontinental piping and power transmission lines.

Space environment (natural and artificial) — Model of the Earth's magnetospheric magnetic field

1 Scope

This document describes the main magnetospheric large-scale current systems and the magnetic field in the Earth's magnetosphere and provides the main requirements to the model of the magnetospheric magnetic field. Ionospheric currents are not considered in this document. The document also provides a working example of the model and establishes the parameters of magnetospheric large-scale current systems which are changing in accordance with conditions in the space environment. The document can be used to develop the new models of magnetospheric magnetic field. Such models are useful in investigating physical processes in the Earth's magnetosphere as well as in calculations, developing, testing and estimating the results of exploitation of spacecrafts and other equipment operating in the space environment.

2 Normative references

There are no normative references in this document.

3 Terms and definitions

For the purposes of this document, the following terms and definitions apply.

ISO and IEC maintain terminology databases for use in standardization at the following addresses:

— ISO Online browsing platform: available at https://www.iso.org/obp

— IEC Electropedia: available at https://www.electropedia.org/

3.1
magnetospheric magnetic field
external magnetic field
external magnetospheric magnetic field
magnetic field produced by *magnetospheric magnetic field sources* (3.4)

3.2
geomagnetic dipole tilt angle
angle of inclination of the geomagnetic dipole to the plane orthogonal to the Earth-Sun line

3.3
internal magnetic field
magnetic field produced by the sources inside the Earth's core

Note 1 to entry: It can be presented in the form of a series of spherical harmonic functions.

Note 2 to entry: The expansion coefficients (IGRF model) undergo very slight changes in time.

Note 3 to entry: The International Association of Geomagnetism and Aeronomy (IAGA) is responsible for IGRF model development and modifications and approves its coefficients every 5 years.

Note 4 to entry: The internal magnetic field is described in ISO 16695.

3.4
magnetospheric magnetic field sources
sources of magnetic fields including the following:

— currents flowing over the magnetopause and screening the geomagnetic dipole magnetic field;

— currents flowing inside the Earth's magnetosphere:

  — tail current, produced by currents across the geomagnetic tail and closure currents on the magnetopause;

  — ring current, including symmetrical ring current, circling around the Earth and carried by trapped particles and partial ring current, produced by currents flowing outside the region of symmetrical ring current, mostly in the pre-midnight sector of equatorial plane, closured by field-aligned and ionospheric currents;

  — field-aligned currents, produced by currents flowing along the auroral magnetic field lines, closured by currents on the magnetopause and in the ionosphere;

— currents flowing over the magnetopause and screening the ring current and partial ring current magnetic fields

Note 1 to entry: In different magnetospheric models, either predefined current systems or current systems dependent on parameters calculated from satellite data are used.

Note 2 to entry: Electric currents flowing entirely in the ionosphere (ionospheric currents) contribute to the magnetic field variation at altitudes below 1 000 km. In the region above 1,5 Re effect of ionospheric current is insignificant. Magnetic field of ionospheric currents is not the subject of this document.

3.5
magnetopause stand-off distance
geocentric distance to the subsolar point on the magnetopause

3.6
solar-magnetospheric coordinates
Cartesian geocentric coordinates, where X-axis is directed to the Sun, Z-axis lies in the one plane with OX axis and geomagnetic dipole axis and Y-axis supplements the X and Z axes to the right-hand system

4 General concepts and assumptions

4.1 Magnetic field induction in the Earth's magnetosphere

Vector of magnetic field induction $\vec{B}_M$ in the Earth's magnetosphere is calculated by Formula (1).

$$\vec{B}_M = \vec{B}_1 + \vec{B}_2 \tag{1}$$

where

$\vec{B}_1$ is the vector of induction of the internal magnetic field, in nT;

$\vec{B}_2$ is the vector of induction of the magnetospheric magnetic field, in nT.

The magnetic field of the magnetospheric currents (magnetospheric magnetic field), $\vec{B}_2$, is calculated in terms of the quantitative model of the magnetosphere.

4.2 Magnetospheric magnetic field standardization: process-based approach

The magnetospheric magnetic field standard does not specify a single magnetospheric model, theoretical or empirical. In order to encourage continual improvements in magnetospheric modelling, this document is process-based for determining the magnetospheric magnetic field. Magnetospheric magnetic field model, after its development, may satisfy the requirements in Clause 4 and the list of criteria presented in Clause 5. The working example of the model is presented in the Annex A and shall be reconsidered every 5 years on the basis of competitions of the candidate models. The current working example is presented in Annex A.

5 Model requirements

5.1 General

— The model of the magnetic field of magnetospheric currents (referred to below as "model") presents the vector of induction of magnetospheric currents in solar-magnetospheric coordinates.

— The model describes a regular part of the magnetic field in the region from 1,0 R_E to 6,6 R_E.

— The model reflects compression of the Earth's magnetosphere in the dayside due to interaction with the solar wind, day-night asymmetry (the field on the nightside is weakened), day and season variations.

— The model takes into account the geomagnetic dipole tilt angle, varying in the range from −35° to +35°.

5.2 The magnetospheric magnetic field sources

The standardised magnetospheric magnetic field is produced by currents described in 3.3. Ionospheric currents' effect is not considered in this document.

5.3 Parameterization

Each magnetospheric source of magnetic field depends on parameters which are calculated from empirical data.

5.4 Magnetospheric dynamics

The magnetospheric dynamics is determined to be a sequence of its instant states.

5.5 Model testing and comparison with measurements

The model testing is carrying out with the help of databases which include the spacecraft-based and on-ground measurements. The dataset used for the model testing is presented in the Annex C.

6 List of criteria

The conformity criteria for this document consist of the activities common for any candidate magnetospheric magnetic field model. These criteria specify the conformity process which includes the model documenting, publishing and testing.

— The candidate model shall include the statement of the modelling approach used (empirical or theoretical model). The empirical models are required to include a clear specification of the input data used to derive the model and where these data were measured. Theoretical models are required to include a description of the physical principles and approaches that are used as the basis of the model.

— The statement about the candidate model area of application and domain applicability should be included.

— The statement about the rms errors during the model calculations comparison with observational data obtained from measurements should be included. For empirical models, the comparisons should also be made with data, different from those from which the model was built.

— The description and implementation of the magnetospheric magnetic field model should be published in internationally-accessible refereed journals.

Annex A
(normative)

Paraboloid model of the magnetospheric magnetic field: calculation of induction of the magnetic field of the magnetospheric currents

A.1 General

The magnetospheric magnetic field calculated by paraboloid model is the solution of the magnetostatic problem inside the paraboloid of revolution.

A.2 Paraboloid model of the magnetic field of magnetospheric currents

A.2.1 General

Vector of induction of the magnetic field of magnetospheric currents is calculated by Formula (A.1).

$$\vec{B}_2 = \vec{B}_{sd}(\psi, R_1) + \vec{B}_t(\psi, R_1, R_2, \Phi_\infty) + \vec{B}_r(\psi, b_t) + \vec{B}_{sr}(\psi, R_1, b_r) + \vec{B}_{fac}(I_0) \quad \text{(A.1)}$$

where

$\vec{B}_{sd}$ is the magnetic field of currents on the magnetopause screening the dipole field;

$\vec{B}_t$ is the magnetic field of the magnetospheric tail;

$\vec{B}_r$ is the magnetic field of the ring current;

$\vec{B}_{sr}$ is the magnetic field of currents on the magnetopause, screening the ring current field;

$\vec{B}_{fac}$ is the magnetic field of region 1 field-aligned currents.

The components of the magnetic field of magnetospheric currents, $\vec{B}_{sd}$, $\vec{B}_t$, $\vec{B}_r$, $\vec{B}_{sr}$, $\vec{B}_{fac}$ are calculated separately in terms of the paraboloid model of the magnetosphere in the form of series in the Bessel functions or Legendre polynomials.

A.2.2 Parameters

The components of the magnetic field of magnetospheric currents, $\vec{B}_{sd}$, $\vec{B}_t$, $\vec{B}_r$, $\vec{B}_{sr}$, $\vec{B}_{fac}$ are determined by the values of parameters of the magnetospheric current systems:

— ψ is the geomagnetic dipole tilt angle, in degrees;

— $\vec{R}_1$ is the distance to the subsolar point at the magnetopause, in R_E;

— $\vec{R}_2$ is the distance to the earthward edge of the magnetospheric tail current sheet, in R_E;

— Φ_∞ is the magnetic flux in the tail lobes, defining the current intensity in the magnetotail, in Wb;

— b_r is the intensity of the ring current magnetic field at the Earth's centre, in nT;

— I_0 being for total region 1 field-aligned currents intensity, in MA.

A.2.3 Submodels

The instant values of the parameters of the magnetospheric current systems, ψ, $\vec{R}_1$, $\vec{R}_2$, Φ_∞, b_r, I_0 are determined using a limited set of empirical data in terms of the so-called submodels (see Annex B).

A.3 Magnetic field of the magnetopause currents screening the geomagnetic dipole

$\vec{B}_{sd}$ is calculated by Formula (A.2).

$$\vec{B}_{sd} = -\nabla U_{sd} \quad \text{(A.2)}$$

where the scalar potential of the magnetic field of magnetopause currents is presented in spherical coordinates R, θ, φ (see C.1):

$$U_{sd} = -\frac{M_E}{R_1^2} \sum_{n=1}^{\infty} \left(\frac{R}{R_1} \right)^n \left[d_n^{||} \sin\ \psi \cdot P_n(\cos\theta) + d_n^{\perp} \cos\varphi\ \cos\varphi \cdot P_n^1(\cos\theta) \right] \quad \text{(A.3)}$$

where

$P_n = \left(2^n n!\right)^{-1} \cdot \left(d^n \left(x^2 - 1\right)^n / dx^n \right)$, $P_n^1(x) = \sqrt{1 - x^2} \cdot (dP_n / dx)$;

$M_E = B_0 \cdot R_E^3$ is the magnetic moment of the geomagnetic dipole;

B_0 is the magnetic field at the geomagnetic equator of the Earth;

$d_n^{||}$ and $d_n^{\perp}$ are dimensionless coefficients, the first six of which are listed in Table A.1.

Table A.1 — Expansion coefficients for the scalar potential of the magnetic field of magnetopause currents

n	$d_n^{\perp}$	$d_n^{\|\|}$
1	0,649 7	0,940 3
2	0,216 5	0,465 0
3	0,043 4	0,129 3
4	−0,000 8	−0,014 8
5	−0,004 9	−0,016 0
6	−0,002 2	−0,022 5

A.4 Magnetic field of the tail current system

The magnetic field of the tail current system, $\vec{B}_{\mathrm{t}}$, is calculated from Formula (A.4).

$$\vec{B}_{\mathrm{t}} = -\nabla U_{\mathrm{t}} + \vec{B}_{\mathrm{t_{in}}} \tag{A.4}$$

where U_{t} is determined by the series

$$U_{\mathrm{t}} = b_{\mathrm{t}} R_1 = \begin{cases} \sum\limits_{k,n=1}^{\infty} \left(b_{nk} + c_{nk} K_n^{'}(\lambda_{nk}\alpha_0)\lambda_{nk} \right) \cos n\varphi \cdot J_n(\lambda_{nk}\beta) I_n(\lambda_{nk}\alpha) & \text{for } \alpha < \alpha_0 \\ \beta_{\mathrm{t}} \alpha_0 \ln\alpha \cdot \mathrm{sign}\left(\frac{\pi}{2} - |\varphi| \right) + \\ \sum c_{nk} \cos n\varphi \cdot I_n^{'}(\lambda_{nk}\alpha_0)\lambda_{nk} J_n(\lambda_{nk}\beta) K_n(\lambda_{nk}\alpha) & \text{for } \alpha \geq \alpha_0 \end{cases} \tag{A.5}$$

here

$$c_{nk} = b_{nk} \lambda_{nk} I_n(\lambda_{nk}\alpha_0) \tag{A.6}$$

$$b_{nk} = \frac{2\lambda_{nk} \int_0^1 \int_{-\pi}^{\pi} J_n(\lambda_{nk}\beta) f(\beta,\varphi) \cos n\varphi \, d\varphi d\beta}{\pi \left(\lambda_{nk}^2 - n^2 \right) J_n^2(\lambda_{nk}) I_n^{'}(\lambda_{nk}\alpha_0)} \tag{A.7}$$

$$f(\beta,\varphi) = \begin{cases} \frac{\alpha_0}{\beta_t} \beta \cos\varphi, & \text{for } \alpha_0 \beta \cos\varphi < \beta_t \\ \mathrm{sign}\left(\frac{\pi}{2} - |\varphi| \right), & \text{for } \alpha_0 \beta \cos\varphi \geq \beta_t \end{cases} \tag{A.8}$$

where

λ_{nk} are zeros of the $J' = 0$ equation;

$\alpha_0 = \sqrt{1 - 2R_2 / R_1}$ is the parabolic $\alpha-$ coordinate of the inner edge of the tail current sheet;

$\beta_t = \frac{d}{R_1}$;

d is the half thickness of the current sheet;

$b_{\mathrm{t}} = \frac{2\Phi_\infty}{\pi R_1^2} \sqrt{R_1 / (2R_2 + R_1)}$ is a magnetic field in the tail lobe at the inner edge of the tail current sheet.

The magnetic field inside the current sheet, $B_{\mathrm{t_{in}}}$, is calculated from Formula (A.9).

$$B_{\mathrm{t_{in}}\alpha} = b_{\mathrm{t}} \frac{\alpha_0}{\alpha} \frac{\beta}{\beta_{\mathrm{t}}} \frac{\cos\varphi}{\sqrt{\alpha^2 + \beta^2}}, \; B_{\mathrm{t_{in}}\beta}, \; B_{\mathrm{t_{in}}\varphi} = 0 \tag{A.9}$$

Description of the paraboloid coordinates is presented in C.3.

A.5 Ring current magnetic field

The ring current magnetic field, $\vec{B}_r$, is determined by Formula (A.10).

$$\vec{B}_r = \frac{M_R}{M_E} \cdot \begin{cases} \left(\frac{R}{R_{rc}}\right)^5 \cdot \vec{B}_d + 2B_0 \frac{R_E^3}{R_2^3}\left(\frac{R_2^5}{R_{rc}^5} - 1\right)\vec{e}_z, & \text{for } 0 \le R \le R_2 \\ \vec{B}_d, & \text{for } R \ge R_2 \end{cases} \quad \text{(A.10)}$$

where

$R_{rc} = \sqrt{0,5\left(R^2 + R_2^2\right)}$;

$M_R = 0,5 b_r \cdot R_2^3 / \left(4\sqrt{2} - 1\right)$ is the magnetic moment of the ring current;

$\vec{B}_d$ is the magnetic field of the geomagnetic dipole;

$\vec{e}_z$ is a unite vector directed oppositely to the geomagnetic dipole.

Expressions for $\vec{B}_d$ and $\vec{e}_z$ in the solar-magnetospheric coordinates are presented in C.4.

A.6 Magnetic field of the magnetopause currents screening the ring current

The magnetic field of the magnetopause currents screening the ring current, $\vec{B}_{sr}$, is calculated from the Formula (A.11).

$$\vec{B}_{sr} = -\nabla U_{sr} \quad \text{(A.11)}$$

where the scalar potential, U_{sr}, of the magnetic field of magnetospheric currents presented in spherical coordinates R, θ, φ (see C.2) reads

$$U_{sr} = -\frac{M_R}{M_1^2} \sum_{n=1}^{\infty} \left(\frac{R}{R_1}\right)^n \left[d_n^{\parallel} \sin\psi \cdot P_n(\cos\theta) + d_n^{\perp} \cos\psi \cos\varphi \cdot P_n^1(\cos\theta)\right] \quad \text{(A.12)}$$

Coefficients $d_n^{\parallel}$ and $d_n^{\perp}$ are listed in Table A.1.

A.7 Magnetic field of field-aligned currents

The magnetic field of field-aligned currents, $\vec{B}_{\mathrm{fac}}$, is calculated from Formula (A.13).

$$\vec{B}_{\mathrm{fac}} = \mathrm{curl}\vec{A}_{\mathrm{fac}} \tag{A.13}$$

where the vector potential $\vec{A}_{\mathrm{fac}}$ of the magnetic field of field-aligned currents is presented in spherical coordinates R, θ, φ with polar axis directed opposite the Earth's dipole (see C.2 and C.4):

$$\vec{A}_{\mathrm{fac}} = \frac{\mu_0 I_0 \sin\varphi}{2(1+\cos\theta_{\mathrm{m}})} \begin{cases} \dfrac{\tan(\theta/2)}{\tan(\theta_{\mathrm{m}}/2)}, \text{ for } 0 \le \theta \le \theta_{\mathrm{m}} \\ \dfrac{\sin\theta_{\mathrm{m}}}{\sin\theta}, \text{ for } \theta_{\mathrm{m}} \le \theta \le \pi - \theta_{\mathrm{m}} \\ \dfrac{\cot(\theta/2)}{\tan(\theta_{\mathrm{m}}/2)}, \ \pi - \theta_{\mathrm{m}} \le \theta \le \pi \end{cases} \tag{A.14}$$

where θ_m is the polar cap radius in radians: $\sin^2\theta_{\mathrm{m}} = 3{,}9 \cdot \Phi_\infty / |B_0|$, with Φ_∞ in WMb and B_0 in nT.

A.8 Accuracy of the model

a) Comparison with the large magnetosphere magnetic field database[7].

Analysis of distribution of relative discrepancies integral over the whole experimental material have the discrepancy mean value about +3 %; σ of the distribution is about 80 %.

b) Comparisons with Dst and satellite measurements

RMS errors are about 10 % to 15 % of peak Dst for different magnetic storms.

The comparison of the model calculations with the empirical data is presented in detail in the Explanatory Report and published in References [3], [4], [8] and [9].

A.9 The other relevant models

a) Semi-empirical T96 model by Reference [16];

b) Semi-empirical T01 model by References [17] and [18];

c) Semi-empirical T04 model by Reference [21].

d) Semi-empirical T15B model by Reference [19].

e) Semi-empirical T15N model by Reference [20].

The model's parameterization is performed using large magnetospheric databases, different for different models. Several model revisions reflect the different mathematical description of the major sources of the magnetospheric field and their different parameterization. The most popular T01 model parameters are geomagnetic dipole tilt angle, IMF B_y and B_z components, solar wind dynamic pressure, and Dst - index. An attempt is made to take into account the prehistory of the solar wind by introducing two functions, G1 and G2, that depend on the IMF B_z and solar wind velocity and their time history.

f) BATS-R-US, the Block-Adaptive-Tree-Solarwind-Roe-Upwind-Scheme (University of Michigan).

The BATS-R-US code solves 3D MHD equations in finite volume form using numerical methods related to Roe's Approximate Riemann Solver. BATSRUS uses an adaptive grid composed of rectangular blocks arranged in varying degrees of spatial refinement levels. The magnetospheric MHD part is attached to an ionospheric potential solver that provides electric potentials and conductances in the ionosphere from magnetospheric field-aligned currents. Inputs to the model are: solar wind plasma (density, velocity, V_x, V_y, V_z, temperature) and magnetic field (B_x, B_y, B_z) measurements, transformed into solar-magnetospheric GSM coordinates and propagated from the solar wind monitoring satellite's position propagated to the sunward boundary of the simulation domain. Outputs are the magnetospheric plasma parameters (atomic mass unit density N, pressure P, velocity V_x, V_y, V_z, magnetic field B_x, B_y, B_z, electric currents, J_x, J_y, J_z) and ionospheric parameters (electric potential PHI, and Hall and Pedersen conductances Sigma_H, Sigma_P).

Annex B
(informative)

Submodels

B.1 General

In the paraboloid model of the magnetosphere the values of parameters of the magnetospheric current systems are calculated using submodels. The submodels represent empirical relations or auxiliary models to relate parameters of the magnetospheric current systems to the measured data. While the magnetic field dependence on parameters is fixed, the parameters dependence on empirical data can be changed by model's user. B.2 to B.7 give the simple submodels allowing calculating the model input parameters. These submodels are not the standardization objects.

B.2 The tilt angle of geomagnetic dipole

The tilt angle of geomagnetic dipole, ψ , is calculated by Formula (B.1).

$$\sin\psi = -\sin\beta \ \cos\alpha_1 + \cos\beta \ \sin\alpha_1 \ \cos\varphi_m \tag{B.1}$$

where

$\alpha_1 = 11{,}43°$	is the angle between the Earth's axis and the geomagnetic dipole moment;
β	is the Sun's deflection ($\sin\beta = \sin\alpha_2 \ \cos\varphi_{se}$);
$\alpha_2 = 23{,}5°$	is the angle between the Earth's axis and the normal to the ecliptic plane;
$\varphi_{se} = 0{,}985\ 626\ 3\left(172 - I_{day}\right)$	is angle between Earth-Sun line and the projection of the Earth's axis at the ecliptic plane;
I_{day}	is the number of the day in a year;
$\varphi_m = t_{UT} \cdot 15° - 69{,}76°$	is the angle between the midnight geographic meridian plane and northern magnetic pole meridian plane;
t_{UT}	is the universal time in hours.

B.3 Magnetopause stand-off distance

The geocentric distance, R_1, to the subsolar point is calculated using solar wind data: solar wind dynamic pressure and IMF B_z component[15]:

$$R_1 = \{10{,}22 + 1{,}29 \ \tanh[0{,}184(B_z + 8{,}14)]\}\left(nv^2\right)^{-\frac{1}{6{,}6}}. \tag{B.2}$$

where

B_z is the IMF z-component, in nT;

n is solar wind density, in cm^{-3};

v is solar wind velocity km/s.

B.4 The distance to the earthward edge of the geomagnetic tail current sheet

The distance to the earthward edge of the geomagnetic tail current sheet, R_2, is calculated by Formula (B.3).

$$R_2 = 1 / \cos^2 \varphi_k \tag{B.3}$$

where

R_2 is expressed in R_E;

φ_k is the latitude of the equatorward boundary of the auroral oval at midnight.

B.5 Magnetic flux through the magnetotail lobes

Magnetic flux through the magnetotail lobes, Φ_∞, is calculated by Formula (B.4).

$$\Phi_\infty = \Phi_0 + \Phi_s \tag{B.4}$$

where

Φ_0 is the magnetic flux in the magnetotail during quiet periods, in Wb;

Φ_s is the time-dependent magnetic flux in the lobes associated with intensification of the magnetotail current system during disturbances.

$$\Phi_0 = 3{,}7 \cdot 10^8 \tag{B.5}$$

$$\Phi_s = -A_L \frac{\pi R_1^2}{14} \sqrt{\frac{2R_2}{R_1} + 1} \tag{B.6}$$

where A_L is the auroral index of geomagnetic activity.

B.6 The ring current magnetic field at the Earth's centre

The ring current intensity is characterised by the value of ring current magnetic field at the Earth's centre, which is calculated by the Dessler-Parker-Scopke relation:

$$b_r = -\frac{2}{3} B_0 \frac{\varepsilon_r}{\varepsilon_d} \tag{B.7}$$

where

ε_r is the total energy of ring current particles;

$\varepsilon_d = \frac{1}{3} B_0 M_E$ is the geomagnetic dipole energy.

Partial ring current (see e.g. Reference [12]) is essential only just in main phase of magnetic storm and not included in this document.

B.7 The total region 1 field-aligned current

The total Region 1 field-aligned current intensity is calculated by Formula (B.8).

$$I_0 = 2\sqrt{\frac{v}{400}} \cdot \begin{cases} 0{,}327\ 744, \text{ for } b_z > -1{,}6 \\ -1{,}017 \cdot \frac{b_z}{5}, \text{ for } b_z \leq -1{,}6 \end{cases} \quad \text{(B.8)}$$

where

b_z is the IMF north-south component, in nT;

v is solar wind velocity km/s.