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**Software and system engineering —  
High-level Petri nets —**

Part 1:  
**Concepts, definitions and graphical  
notation**

AMENDMENT 1: Symmetric Nets

*Ingénierie du logiciel et du système — Réseaux de Petri de haut  
niveau —*

*Partie 1: Concepts, définitions et notation graphique*

*AMENDEMENT 1: Réseaux symétriques*

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## Foreword

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Amendment 1 to ISO/IEC 15909-1:2004 was prepared by Joint Technical Committee ISO/IEC JTC 1, *Information technology*, Subcommittee SC 7, *Software and systems engineering*.

This amendment to ISO/IEC 15909-1 concerns the addition of a class of high-level nets, known as Symmetric Nets, to Annex B and the corresponding changes required to the Conformance Clause. Additional references related to Symmetric Nets are to be included in the Bibliography. Revised Annex B is included in full, due to some minor notational corrections in clause B.1.

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# Software and system engineering — High-level Petri nets —

## Part 1: Concepts, definitions and graphical notation

### AMENDMENT 1: Symmetric Nets

*Cover page and page 1*

In the document title, replace “Software and system engineering” with “Systems and software engineering”.

*Page 19, Conformance*

Insert the following subclause after subclause 9.1 (PN Conformance):

#### **9.2 Conformance to Symmetric Nets**

This subclause expresses the requirements for a tool implementing high-level Petri nets to conform to the Symmetric Net class.

##### **9.2.1 Level 1**

To claim Level 1 conformance to the Symmetric Net class of this International Standard, an implementation shall demonstrate that it has the semantics defined in clause 4, with the types (domains) and pre and post functions that can be derived from the Symmetric Net Graph defined in Annex B.2 by providing a mapping from the implementation’s syntax to the semantic model in a similar way to that defined in clause 8.

##### **9.2.2 Level 2**

To claim Level 2 conformance to the Symmetric Net class of this International Standard, an implementation must satisfy the requirements for Level 1 conformance to the Symmetric Net class and additionally shall include the syntax of the Symmetric Net Graph defined in Annex B.2 and the notational conventions of clause 7.

Change the numbering of HLPN Conformance to subclause 9.3.

*Page 25, Annex B*

Replace normative Annex B with the text starting on the next page, which adds new clause B.2 to define the Symmetric Net class of High-level Petri Net Graphs (HLPNGs).

## Annex B

### (normative)

### Net Classes

The purpose of this Annex is to define various classes of nets as subclasses of the HLPNG. It currently comprises two clauses: B.1 for Place/Transition nets (without capacities), which is a common form of Petri nets where tokens are simply 'black dots'; and B.2 for Symmetric Nets, which describes a basic form of coloured Petri nets with simple types that are amenable to efficient analysis. Other subclasses may include Elementary Net systems and other high-level nets.

#### B.1 Place/Transition Nets

A Place/Transition net graph (without capacity), **PTNG**, is a special HLPNG

$$\mathbf{PTNG} = (NG, Sig, V, H, Type, AN, M_0)$$

where

- $NG = (P, T, F)$  is a net graph
- $Sig = (S, O)$  with  $S = \{Dot, Bool, Mdot\}$ ,  $O = \{\bullet_{Dot}, true_{Bool}, 1_{Mdot}, 2_{Mdot}, \dots\}$
- $V = \emptyset$
- $H = (\{dot, Boolean, \mu dot\}, \{\bullet, true, 1^{\bullet}, 2^{\bullet}, \dots\})$  a many-sorted algebra for the signature  $Sig$ , with  $dot = \{\bullet\}$ ,  $\mu dot = \{\{(\bullet, n)\} | n \in N\}$  and  $H_{Dot} = dot$ ,  $H_{Bool} = Boolean$ ,  $H_{Mdot} = \mu dot$ ,  $(\bullet_{Dot})_H = \bullet$ ,  $(true_{Bool})_H = true$ ,  $(1_{Mdot})_H = 1^{\bullet}$ ,  $(2_{Mdot})_H = 2^{\bullet}$  etc.
- $Type : P \rightarrow \{dot, Boolean, \mu dot\}$  is a function that assigns the type  $dot$  to all places ( $\forall p \in P, Type(p) = dot$ ).
- $AN = (A, TC)$  is a pair of net annotations.
  - $A : F \rightarrow \{1_{Mdot}, 2_{Mdot}, \dots\}$  is a function that annotates each arc with a syntactic 'positive integer' constant, that when evaluated becomes the corresponding multiset over  $dot$ .
  - $TC : T \rightarrow \{true_{Bool}\}$  is a function that annotates every transition with the syntactic constant true (which by convention is omitted) that on evaluation is the Boolean value  $true$ .
- $M_0 : P \rightarrow \mu dot$ .

Although this is a rather baroque definition of Place/Transition nets, it can be seen to be in one to one correspondence with a more usual definition given below.

$$\mathbf{PTNG} = (NG, W, M_0)$$

where

- $NG = (P, T; F)$  is a net graph.
- $W : F \rightarrow N^+$  is the weight function, assigning a positive integer to each arc.
- $M_0 : P \rightarrow N$  is the initial marking assigning a natural number of tokens to each place. These are represented by dots ( $\bullet$ ).

This is because:

- the transition condition is true for each transition, and hence doesn't need to be considered,

- the type of each place is the same, comprising a single value  $\bullet$ , and hence there is no need for typing places,
- the number of dots ( $\bullet$ ) associated with each arc (Weight function) are in one to one correspondence with the positive integers, and
- the number of dots ( $\bullet$ ) associated with each place (marking) are in one to one correspondence with the Naturals.

## B.2 Symmetric Nets

### B.2.1 Introduction

Symmetric Net Graphs place restrictions on the many-sorted algebra of HLPNGs. Firstly, the carriers of the algebra (Types) are finite. Secondly, basic types are defined and then further types (products and multisets) are built from them. Basic types are classified as unordered, linearly ordered or circular. This classification depends on the functions that are associated with the type as defined below (see subclause B.2.5).

A symmetric net graph, **SNG**, is a special HLPNG

$$\text{SNG} = (NG, Sig, V, H, Type, AN, M_0)$$

with the following restrictions on the signature  $Sig = (S, O)$ , algebra,  $H = (S_H, O_H)$ , typing function,  $Type$ , and arc annotations,  $AN$ . The set of sorts,  $S$ , is partitioned to reflect the structure of the types of Symmetric Net Graphs. The allowed operators are defined for the sorts (including explicit operators for multiset constants). The restrictions on  $S_H$  are determined by defining all the allowable types. Then the allowable set of functions are defined, which enables the set of functions comprising  $O_H$  to be determined.

### B.2.2 Sorts

Symmetric Net Graphs allow the use of three kinds of basic sorts:  $U\text{sorts}$ ,  $LO\text{sorts}$  and  $C\text{sorts}$  which are disjoint and where  $Bool \in U\text{sorts} \cup LO\text{sorts}$ . Basic sorts are defined as the union:

$$BasicSorts = U\text{sorts} \cup LO\text{sorts} \cup C\text{sorts}.$$

A product sort may be created for each combination of basic sorts:

$$P\text{sorts} \subseteq \{PROD_\sigma \mid \sigma \in BasicSorts^* \text{ and } Length(\sigma) \geq 2\}$$

where  $Length$  is a function that takes a string and returns its length.

A multiset sort may be created for each basic sort and product sort:

$$M\text{sorts} \subseteq \{s_{ms} \mid s \in BasicSorts \cup P\text{sorts}\}.$$

Finally, there is the special dedicated sort,  $nat$ , (that is always interpreted as the Natural numbers,  $N$ , in the algebra) which is required for various operations involving  $M\text{sorts}$ .

Hence the set of sorts,  $S$ , is given by

$$S = U\text{sorts} \cup LO\text{sorts} \cup C\text{sorts} \cup P\text{sorts} \cup M\text{sorts} \cup \{nat\}.$$

### B.2.3 Operators

#### Operators for $LO\text{sorts}$

Comparison operators are defined for each sort in  $LO\text{sorts}$ :

$$CompOps = \{<_{(s,s,Bool)}, \leq_{(s,s,Bool)}, >_{(s,s,Bool)}, \geq_{(s,s,Bool)} \mid s \in LO\text{sorts}\}$$

NOTE 1: Infix notation is used for these comparison operators.

#### Operators for $C\text{sorts}$ :

A set of unary operators is defined for each sort in  $C\text{sorts}$ :

$$CircularOps = \{Succ_{(s,s)}, Pred_{(s,s)} \mid s \in C\text{sorts}\}.$$

**Specific Operators on Basic Sorts:**

The following specific operators are defined for basic sorts:

- Operators for Bool:

$$BoolOps = \{not_{(Bool, Bool)}, and_{(Bool, Bool, Bool)}, or_{(Bool, Bool, Bool)}, implies_{(Bool, Bool, Bool)}\};$$

NOTE 2: Infix notation is used for binary operators.

- A set of unary operators with output sorts in  $LOsorts$ :

$$PartitioningOps = \{PartitionOp_{(b, lo)} \mid b \in BasicSorts, lo \in LOsorts\};$$

NOTE 3: Symmetric nets are based on “well formed nets” (see Bibliography items 25 and 26). The intent of this operator is to allow the notion of “static subclasses” introduced for “well formed nets” to be used in Symmetric nets.

- A set of tupling operators with output sorts in  $Psorts$ :

$$TuplingOps = \{()_{(\sigma, PROD_\sigma)} \mid \sigma \in BasicSorts^*, PROD_\sigma \in Psorts\}.$$

NOTE 4: Tupling operators are required to allow us to write a tuple on an arc. The convention is adopted to use outfix notation, where the additional set of parenthesis is dropped, e.g.  $((x, y, z))$  is written  $(x, y, z)$ .

**Projection Operators on Product Sorts:**

A set of projection operators that select the  $i$ th component of a tuple:

$$ProjectionOps = \{Proj^i_{(PROD_{(b_1 \dots b_n)}, b_i)} \mid i \in \{1, \dots, n\}, n > 1, b_1 \dots b_n \in BasicSorts, \text{ and } PROD_{(b_1 \dots b_n)} \in Psorts\}$$

**Operators for both Basic Sorts and Product Sorts:**

- Equality Predicate:

$$EqualityOps = \{=(s, s, Bool) \mid s \in BasicSorts \cup Psorts\};$$

- A set of conversion operators with output sorts in  $Msorts$ :

$$Convert2MOps = \{\setminus_{(nat, s, s_{ms})} \mid s \in BasicSorts \cup Psorts, s_{ms} \in Msorts\}.$$

NOTE 5: As usual, the convention is adopted to use infix notation for these operators.

**Operators on Multiset Sorts:**

The following operators are defined for multiset sorts:

- Addition and subtraction operations:

$$MbinaryOps = \{+_{(s, s, s)}, -_{(s, s, s)} \mid s \in Msorts\};$$

- Scaling Operation:

$$MscalingOps = \{*_{(nat, s, s)} \mid s \in Msorts\};$$

- Predicates for equality and comparison:

$$Mpredicates = \{=(s, s, Bool), \leq_{(s, s, Bool)} \mid s \in Msorts\};$$

- Cardinality operation:

$$Mcardinality = \{||_{(s, nat)} \mid s \in Msorts\}.$$

NOTE 6: Infix Notation is used for multiset operations, except for cardinality which uses Outfix notation.

**Constants for all sorts**

A set called *Constants* is defined which contains constants of any sort. In particular, it includes dedicated constants:

- $BoolConstants \subset Constants$  where  $BoolConstants = \{true_{Bool}, false_{Bool}\}$ ;

- $NatConstants \subset Constants$  where  $NatConstants = \{0_{nat}, 1_{nat}, 2_{nat}, \dots\}$ ;

NOTE 7: Natural constants are required for multiset scaling and conversion.

- for  $s \in Msorts$ ,  $all_s, empty_s \in Constants$ .

NOTE 8:  $all_s$  denotes (in the algebra) a multiset with exactly one occurrence of each element of its basis set.

#### Set of allowed Operators:

All the operators (and constants) defined above are gathered into the set  $Ops_{SN}$ . Then  $O \subseteq Ops_{SN}$ , where

- the input and output sorts of each operator must be in  $S$ ; and
- only one unary operator with output sort in  $LOsorts$  is allowed for each basic sort: for  $b1, b2 \in BasicSorts$  and  $lo1, lo2 \in LOsorts$ ,  $o_{(b1, lo1)}, o_{(b2, lo2)} \in O$  and  $o_{(b1, lo1)} \neq o_{(b2, lo2)}$  implies  $b1 \neq b2$ .

NOTE 9: The rationale for this restriction is to enable the use of symbolic reachability graph techniques.

#### B.2.4 Types

In the algebra,  $H = (S_H, O_H)$ , a type is associated with each sort, i.e.  $S_H \equiv \{H_s \mid s \in S\}$ . The corresponding sets of types in the algebra are:

- $UnorderedTypes = \{H_s \mid s \in Usorts\}$ ;
- $LinearOTypes = \{H_s \mid s \in LOsorts\}$ ;
- $CircularTypes = \{H_s \mid s \in Csorts\}$ ;
- $ProductTypes = \{H_s \mid s \in Psorts\}$ ;
- $MultisetTypes = \{H_s \mid s \in Msorts\}$ ;
- $H_{nat} = N$ ;
- $H_{Bool} = Boolean$ .

#### Basic types:

$BasicTypes = UnorderedTypes \cup LinearOTypes \cup CircularTypes$ .

$BasicTypes$  is the set of finite types, including *Boolean* (i.e.  $Boolean \in BasicTypes$ ).

NOTE: Finite types include any finite range of the *Integers* (e.g.  $\{0, 1, 2, 3, 4\}$ ) and usual enumerated types such as *rainbow* =  $\{red, orange, yellow, green, blue, indigo, violet\}$ . Compound sets, such as products, are not included.

#### Product types:

$ProductTypes$  is the set of Cartesian Products formed from  $BasicTypes$ .

$ProductTypes = \{bt_1 \times \dots \times bt_n \mid bt_1, \dots, bt_n \in BasicTypes \text{ and } n \in N^+ \setminus \{1\}\}$

#### Multiset types:

Let  $MultisetTypes$  be the set of the set of multisets over each basic type or product type.

$MultisetTypes = \{\mu TYPE \mid TYPE \in BasicTypes \cup ProductTypes\}$

#### Set of allowed types:

Define  $D_{SN} = BasicTypes \cup ProductTypes \cup MultisetTypes \cup \{N\}$ . Then  $S_H \subseteq D_{SN}$ , where  $Boolean \in S_H$ .

## B.2.5 Functions

### Functions for Linearly Ordered Types:

The functions corresponding to the set of comparison operators for  $LOsorts$  are given by:

$CompFns = \{lt_s, lteq_s, gt_s, gteq_s \mid s \in LOsorts\}$ , where for  $s \in LOsorts$ ,

$$lt_s, lteq_s, gt_s, gteq_s : H_s \times H_s \rightarrow Boolean$$

NOTE 1: From above,  $\forall s \in LOsorts, H_s \in LinearOTypes$ .

NOTE 2: For linearly ordered types the above functions must be antisymmetric, transitive and total:

$\forall fn \in CompFns$

1.  $\forall a, b \in H_s, fn(a, b) \wedge fn(b, a) \Rightarrow a =_s b$ ; and
2.  $\forall a, b, c \in H_s, fn(a, b) \wedge fn(b, c) \Rightarrow fn(a, c)$ ; and
3.  $\forall a, b \in H_s, fn(a, b) \vee fn(b, a) \vee a =_s b$

### Functions on Circular Types:

The corresponding set of successor and predecessor functions is given by:

$CircularFns = \{succ_s, pred_s \mid s \in Csorts\}$ , where for  $s \in Csorts$ ,

$$pred_s, succ_s : H_s \rightarrow H_s$$

and for  $H_s = \{a_0 \dots a_{(n_s-1)}\}$  where  $n_s \in N^+$ , for  $i \in \{0, 1, \dots, n_s - 1\}$  its successor function is given by  $succ_s(a_i) = a_{(i+1)(mod\ n_s)}$  and similarly its predecessor function is given by  $pred_s(a_i) = a_{(i-1)(mod\ n_s)}$ , where  $a_{i(mod\ n_s)} = a_i$ ,  $a_{n_s(mod\ n_s)} = a_0$  and  $a_{(-1)(mod\ n_s)} = a_{(n_s-1)}$ .

NOTE 3: From above,  $\forall s \in Csorts, H_s \in CircularTypes$ .

### Functions on Basic Types:

The following sets of functions correspond to the operators defined for basic sorts:

- Functions on Booleans

The unary function  $not : Boolean \rightarrow Boolean$  and connectives (binary functions)  $and, or, implies : Boolean \times Boolean \rightarrow Boolean$  with their usual meaning, are allowed in the algebra.

$Boolean = \{true, false\}$  may be unordered ( $Bool \in Usorts$ ) or a linearly ordered ( $Bool \in LOsorts$ ). When  $Boolean$  is unordered,  $Boolean \in UnorderedTypes$ . When it is linearly ordered,  $Boolean \in LinearOTypes$  with the following comparison function bodies:

$$\begin{aligned} lt_{Bool}(false, true) &= true \\ lteq_{Bool}(false, true) &= true \\ gt_{Bool}(false, true) &= false \\ gteq_{Bool}(false, true) &= false \end{aligned}$$

- For each unary operator,  $o_{(b,lo)} \in OrderOps$ , there is a function,  $o_H : H_b \rightarrow H_{lo}$  in  $O_H$ , where  $H_b \in BasicTypes$  and  $H_{lo} \in LinearOTypes$ . Let  $[A \rightarrow B]$  denote the set of all functions from type  $A$  to type  $B$ . The set of all functions from each basic type to each linearly ordered type is as follows.

$MixedFns = \bigcup_{BT, LT} [BT \rightarrow LT]$  where  $BT \in BasicTypes$  and  $LT \in LinearOTypes$

NOTE 4: Each of these functions can be considered to partition its domain (i.e. a basic type) in the sense that each subset in the partition is mapped to a value in the linearly ordered type. A comparison function defined for the linearly ordered type can then be used to induce an order on the partition. An example demonstrating the use of mixed functions is given in subclause B.2.8.

- For each tupling operator,  $(\cdot)_{((b_1 \dots b_n), PROD_{(b_1 \dots b_n)})} \in TuplingOps$ , there is a corresponding identity function given by

$$I_{(b_1 \dots b_n)} : H_{b_1} \times \dots \times H_{b_n} \rightarrow H_{b_1} \times \dots \times H_{b_n}$$

where for  $i \in \{1, \dots, n\}$ ,  $n \geq 2$ ,  $H_{b_i} \in BasicTypes$ .

**Projection Functions on Product Types:**

For each projection operator,  $Proj_{(PROD_{(b_1 \dots b_n), b_i})}^i \in ProjectOps$ ,  $i \in \{1, \dots, n\}$ , there is a function that returns the  $i$ th component in the tuple:

$$Proj_{((b_1 \dots b_n), i)}^i : H_{b_1} \times \dots \times H_{b_n} \rightarrow H_{b_i}$$

where  $Proj_{((b_1 \dots b_n), i)}^i(a_1, \dots, a_i, \dots, a_n) = a_i$ .

**Functions for both Basic Types and Product Types:**

## • Equality

For each equality predicate,  $=_{(s, s, Bool)} \in EqualityOps$ , with  $s \in BasicSorts \cup Psorts$  there is a corresponding Boolean function for equality:

$$=_s : H_s \times H_s \rightarrow Boolean$$

• Converting a value in *BasicTypes* or *ProductTypes* to a multiset

For each operator,  $\wedge_{(nat, s, s_{ms})} \in Convert2MOps$ , with  $s \in BasicSorts \cup Psorts$ , there is a corresponding function:

$$\wedge_s : N \times H_s \rightarrow \mu H_s$$

which converts a value  $a \in H_s$  to a multiset comprising  $n$  occurrences of  $a$ .  $\wedge_s(n, a) = n \setminus a$ .

**Functions for Multiset Types:**

For each operator defined for multiset sorts (addition, subtraction, scaling, equality and comparison predicates, and cardinality) there is a corresponding function defined in Annex A, clause A.2 in the algebra.

**Constants:**

For each  $o_s \in Constants$  there is a constant  $o_H \in H_s$  in the algebra. The values of the dedicated constants are as follows, where  $Val_{s, \alpha}$  (see clause A.3.6) is replaced by  $Val_s$ , since the assignment function,  $\alpha$ , is null for constants (as there are no variables):

- $Val_{Bool}(true_{Bool}) = true$  and  $Val_{Bool}(false_{Bool}) = false$ ;
- For  $i \in N$ ,  $Val_{nat}(i_{nat}) = i$ ;
- For  $s_{ms} \in Msorts$ ,  $Val_{s_{ms}}(all_{s_{ms}}) = all_{H_s} = \{(a, 1) \mid a \in H_s\}$ ;  
NOTE 5: When  $Type(p) = H_s$ ,  $all_{Type(p)} = \{(a, 1) \mid a \in H_s\}$  can be used as the initial marking of  $p$  ( $M_0(p) = all_{Type(p)}$ ) to denote that all elements of  $Type(p)$  reside in place  $p$  initially. An example is given in clause B.2.8.
- For  $s \in Msorts$ ,  $Val_s(empty_s) = \emptyset$ .

**Set of allowed Functions:**

All the constants and functions defined above are gathered into the set  $Func_{SN}$ . Then  $O_H \subseteq Func_{SN}$ , where

- the type of each constant must be in  $S_H$ ;
- the domain and co-domain of each of these functions must be in  $S_H$ ; and
- only one mixed function is allowed for each basic type: for  $f, g \in O_H$ ,  $f \neq g$ ,  $f, g \in MixedFns$  implies  $Dom(f) \neq Dom(g)$ , where  $Dom(h)$  is the domain of function  $h$ .

**B.2.6 Typing Function**

The type of a place in Symmetric Nets is restricted. It may be a basic type or a product type.

$$Type : P \rightarrow S_H \setminus (MultisetTypes \cup \{N\})$$

### B.2.7 Arc Annotations

In the HLPNG, the only restriction on the arc annotation is that it is a term that evaluates to a multiset over the type of its associated place. In Symmetric Net Graphs there is a requirement to restrict the terms annotating the arcs associated with a particular place,  $p \in P$ , to one designated multiset sort,  $d_{ms} \in S$ , associated with a sort  $d \in BasicSorts \cup Psorts$ . Then the type of the place (associated with the arcs) is given by  $H_d$ , the carrier associated with sort  $d$ . This is formalised as follows.

$\forall p \in P, \exists d \in BasicSorts \cup Psorts$  such that  $\forall f \in F \cap ((\{p\} \times T) \cup (T \times \{p\})) A(f) \in TERM(O \cup V)_{d_{ms}}$  and  $Type(p) = H_d$ .

NOTE: For  $Type(p) = H_s$ ,  $all_{s_{ms}}$  can be used to annotate an arc  $(p, t)$  to remove all values of  $Type(p)$  from place  $p$ . Similarly, it can be used to annotate arc  $(t, p)$  to ‘broadcast’ all values of  $Type(p)$  to place  $p$ .

### B.2.8 Example of a Symmetric Net Graph

This subclause provides an example of a Symmetric Net Graph which includes a mixed function, in this case from an unordered type to a linearly ordered type, and illustrates the use of a constant multiset to represent a type (sometimes called a ‘Broadcast Function’) for the initial marking. Figure B.1 is a Symmetric Net Graph representing a file access policy. It comprises 3 places representing: users wishing to access files (*Users*), the files and their associated owner (*Files*), and the files currently being accessed by a user (*FilesBeingAccessed*); and one transition, *GrantAccess*. Thus  $P = \{Users, Files, FilesBeingAccessed\}$  and  $T = \{GrantAccess\}$ . Place *Users* is typed by *USERS*, and has an initial marking of  $All_{USERS}$ , the multiset constant representing all users. Place *Files* is typed by a product set, *OwnedFiles*, representing the set of file-owner pairs. It has an initial marking given by  $M_0(Files) = 1^{(index.html, apache)} + 1^{(emacs, chris)} + 1^{(article.tex, chris)} + 1^{(/etc/passwd, root)}$ . *FilesBeingAccessed* is typed by *AccessedFiles* and is initially empty. *GrantAccess* has a transition condition  $[u = v \text{ or } Access(u) > Access(v)]$ , which only allows the user to access its own files, or for a user that has higher access rights to access the file. The annotation of the arc (*Users*, *GrantAccess*) is  $u$ , that of (*GrantAccess*, *FilesBeingAccessed*) is  $(u, f)$  and for (*Files*, *GrantAccess*) is  $(f, v)$ .

Many conventions have been adopted in Fig. B.1 to simplify the presentation of a HLPNG. These conventions suppress the signature and concentrate on the algebra. Note that a tupling operator has been used to create  $(f, v)$  and  $(u, f)$ , and that the usual convention of dropping the conversion operator  $1^{\setminus}$  is adopted. For example,  $(u, f)$  has been used instead of  $1^{\setminus}(u, f)$ .