TECHNICAL REPORT

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Documentation on design automation subjects – Mathematical algorithm hardware description languages for system level modeling and verification (HDLMath)

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IEC TR 63051

Edition 1.0   2017-01

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DOCUMENTATION ON DESIGN AUTOMATION SUBJECTS – MATHEMATICAL ALGORITHM HARDWARE DESCRIPTION LANGUAGES FOR SYSTEM LEVEL MODELING AND VERIFICATION (HDLMath)

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The text of this Technical Report is based on the following documents:

Enquiry draft	Report on voting
91/1349/DTR	91/1396/RVC

Full information on the voting for the approval of this Technical Report can be found in the report on voting indicated in the above table.

This document has been drafted in accordance with the ISO/IEC Directives, Part 2.

The committee has decided that the contents of this document will remain unchanged until the stability date indicated on the IEC website under "http://webstore.iec.ch" in the data related to the specific document. At this date, the document will be

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INTRODUCTION

Around the world, engineers in industries such as electronics and automobiles are developing many kinds of systems and products. However, these are developed based on conventional design processes and suffer from many design problems and long design times. Because the laws of nature can be expressed mathematically, mathematics is a good algorithmic method for the description and modeling of such systems. Mathematical modeling is also an important approach for both solving problems and visualizing the abstract concepts involved.

System LSI (Large Scale Integration) can be described at three levels of complexity as follows:

1) The the algorithmic level, which specifies only the algorithm used by the hardware for the problem solution;

2) the register transfer level, in which the registers are system elements and the data transfer between these registers is specified according to some rule;

3) the circuit level, where gates and flip-flops are replaced by the circuit elements such as transistors, diodes, resistors, etc.

For levels 2) and 3), VHDL (IEC 61691-1-1:2011 [1][1]) and SystemVerilog (IEC 62530:2011[2]) have already been standardized by the IEC and IEEE and have been in practical use for over twenty years.

For level 1), System C is able to describe hardware systems at the behavioral level.

The purpose of this document is to accelerate the standardization of a mathematical algorithm description language (HDLMath). HDLMath will be used to describe and verify the entire behavior of systems and/or products using mathematical algorithms of electronic systems. It is a higher level language than conventional HDL (Hardware Description Language) languages such as VHDL and SystemVerilog.

HDLMath and its design environment can support the design of many domains and applications as indicated in Table 1.

Table 1 – Examples of mathematics applications

Mathematics	Application examples
Complex numbers	Resistors, inductors, capacitors, power engineering, analysis of electric and magnetic fields, digital signal processing, image processing
Matrices and determinants	Electrical networks, computer graphics, image analysis
Laplace transforms	Circuits, power systems (generators), feedback loops
Statistics and probability	Failure rates for semiconductor devices, behavior of semiconductor materials, image analysis, data compression, digital communications techniques, error correction
Vector and trigonometry	Oscillating waves (circuits, signal processing), electric and magnetic fields, design of power generating equipment, radio frequency (RF) systems and antenna design
Differentiation and integration	Calculation of currents in a circuit, wave propagation, design of semiconductors, image analyses, design of firing circuits
Functions, polynomial, linear equations, logarithms, Euclidean geometry	Curve fitting, fuel cell design, traffic modeling, power analysis, stress analysis, determining the size and shape of parts, software design, computer graphics

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1 Numbers in square brackets refer to the Bibliography.

Recently, several HDLMath languages have already been used to design the mathematical algorithms in electronic systems. MATLAB/SIMULINK is one such popular design environment for the design and verification of various system behaviors. FinSimMath has been proposed and put to practical use by several groups to design and verify mathematical algorithms in ASIC (Application Specific Integrated Circuit) or FPGA (Field Programmable Gate Array). System C-AMS is mainly for analog circuit design and is an extension of the System C standardized by the IEEE and IEC. It is capable of describing mathematical algorithms using additional C-code extensions. IEC TR 62856:2013 [3] (BVDL, or Bird's-eye View of Design Languages) describes the features of existing design languages, as well as listing the requirements for enhancing design languages and for developing new ones.

Another purpose of this document is to add HDLMath to BVDL as a system modeling language. This document describes nine functional requirements for an HDLMath and compares current HDLMath languages from a design viewpoint. It is intended to accelerate the standardization of a mathematical algorithm design language and to establish a good system modeling environment in the world.

DOCUMENTATION ON DESIGN AUTOMATION SUBJECTS – MATHEMATICAL ALGORITHM HARDWARE DESCRIPTION LANGUAGES FOR SYSTEM LEVEL MODELING AND VERIFICATION (HDLMath)

1 Scope

A hardware description language provides a means to describe the behavior of a system precisely and concisely. This document describes the main functional requirements for an HDLMath language and compares existing HDLMath languages from the viewpoint of designers. It is intended to accelerate the standardization of a mathematical algorithm design language and to help establish a new and good system modeling and verification environment.

2 Normative references

The following documents are referred to in the text in such a way that some or all of their content constitutes requirements of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

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3 Terms and definitions

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4 Definition and positioning of HDLMath

4.1 General

HDLMath is defined as a language for describing and verifying the behavior of an entire system or product using mathematical algorithms.

IEC TR 62856:2013 (BVDL) describes the features of existing design languages used in the design processes applied to the development of System-on-Chip (SoC) devices, which range from system level design, IP block creation and analog block design, to SoC design implementation and verification. HDLMath will cover system level design in the BVDL schema.

4.2 Current HDLMaths

Currently, there are three kinds of language for these design environments: HDLMath1, HDLMath2, and HDLMath3.

HDLMath1 is a kind of high-level language that has an interactive environment for numerical computation, visualization, and programming. It is able to analyze data, develop algorithms, and create models and applications using the language, tools, and built-in mathematical functions. It features the following:

a) a block diagram environment for multi-domain simulation and model-based design;

b) simulation, automatic code generation, and continuous test and verification of embedded systems.

HDLMath2 is motivated by the need for mathematical modeling within the Verilog language. Its features are as follows:

- no explicit conversion functions are necessary;

- support for runtime changes of formats, including the number of bits of the various fields;

- data in multi-dimensional arrays that are easy to access globally.

The language is designed to support a large number of mathematical system tasks, and provides access to information regarding the occurrence of overflows, underflows, maximum number of bits needed, cumulative error, etc.

HDLMath3 is a language mainly to support analog design. It allows networks of analog parts such as resistors, capacitors, etc., to be defined. The simulator extracts the differential equations corresponding to the network of analog parts and solves them based on initial conditions and using a timestep provided by the user. It is able to handle blocks that are modeled mathematically and written at the C/C++ level. However, the mathematical capabilities in math.h (a kind of C function library) are limited at the low level of C/C++ and not at the high levels found in HDLMath1 or HDLMath2.

4.3   Design abstraction level of HDLMath

Figure 1 shows the number of lines of code for several small examples written using HDLMath1 and HDLMath2. It also shows the length of the C-code generated automatically from an HDLMath1 description. The number of lines of C-code is several hundred times larger than that of the HDLMath descriptions. The figure indicates how HDLMath languages can be used to design at a higher level of design abstraction and hence how design productivity is higher than C level design.
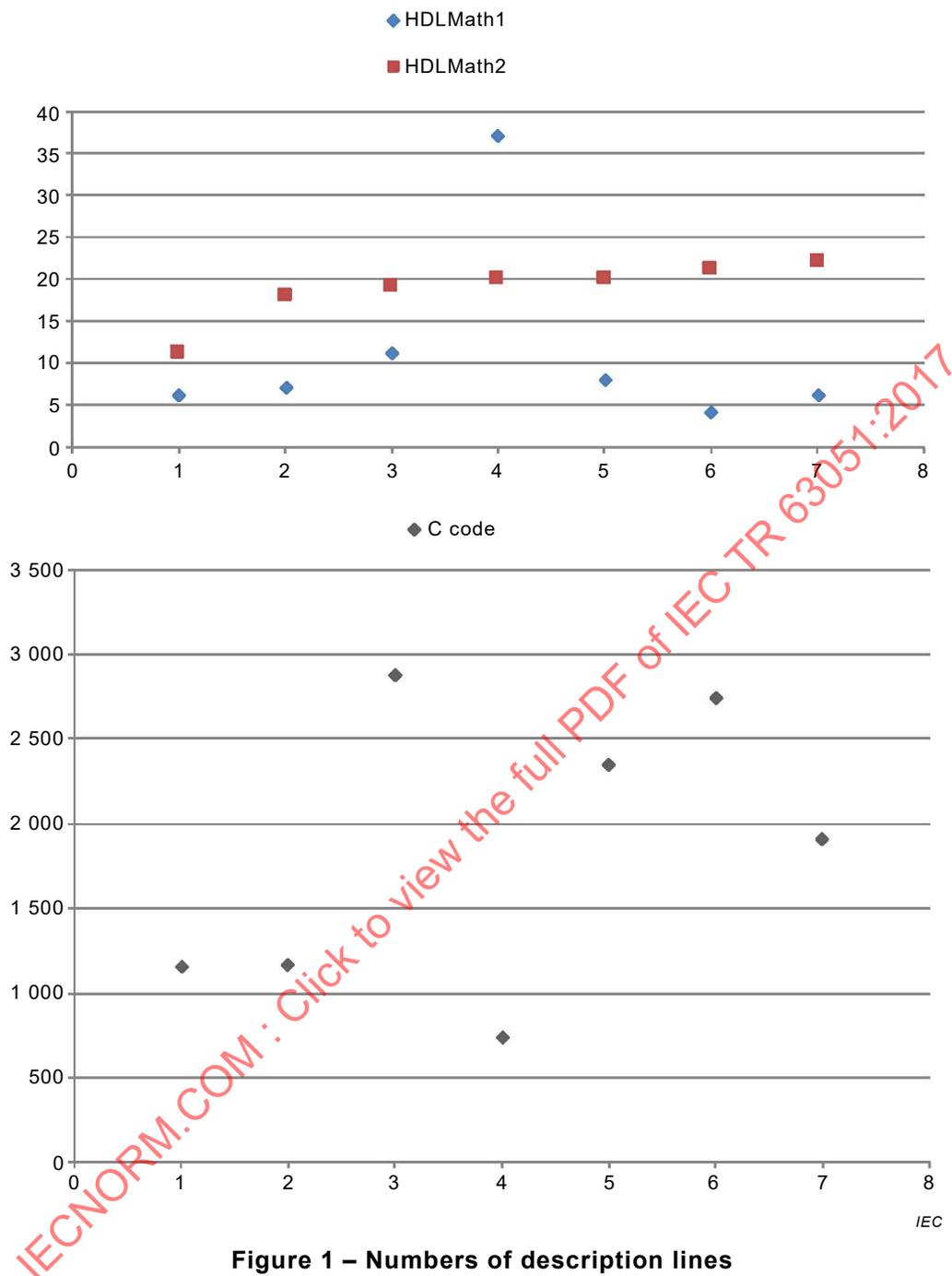
Figure 1 – Numbers of description lines

5 Functional requirements of HDLMath

5.1 General

When designing mathematical algorithms for system level modeling with an HDLMath, the HDLMath shall cover the following functional requirements in order to achieve utmost precision.

5.2 Mathematical expressions

The mathematical operators +, -, *, **, and / shall be applicable to any combination of the following operand and result formats: arbitrary-precision fixed-point, arbitrary-precision floating-point, integer, real, register, and constants. Trigonometric and hyperbolic (direct and inverse) functions shall be supported for any precision. Power, logarithm, and square root

operations are also needed. Figure 2 shows a part of a filter described using logarithm function in HDLMath1 and HDLMath2.

```
/**** HDLMath1 ****/
function ComputeGainC()
step = (srate/SIZE)/2;
l10 = log(10.0);
omega = 0;
for j = 1: SIZE
    Hr = vp*fact;
    for i = 1: 15
        t1 = vp*fact;
        t1 = t1*2*cos(omega*i*T);
        Hr = Hr+t1;
    end
    Hr = abs(Hr);
    y(0,j) = 20*log(Hr)/l10;
    omega = omega + step;
end
```

```
/**** HDLMath2 ****/
task ComputeGainC;
begin
 step = (srate/SIZE)/2;
 l10 = $VpLn(10.0);
 omega = 0;
 for (j = 1; (j < SIZE); j = j+1)
 begin
  vp = $VpCopyReg2Vp(mem[fir.Na]);
  Hr = vp*fact;
  for (i = 1; (i <= 15); i = i+1)
  begin
   vp = $VpCopyReg2Vp(mem[fir.Na-i]);
   t1 = vp*fact;
   t1 = t1*2*$VpCos(omega*i*T);
   Hr = Hr+t1;
  end
  Hr = $VpAbs(Hr);
  y[0][j] = 20*$VpLn(Hr)/l10;
  omega = omega + step;
 end
end
endtask
```

Figure 2 – Examples of mathematical expressions

5.3   Various kinds of precision computation

Data shall include scalar, complex numbers in Cartesian coordinates, and complex numbers in polar coordinates. The high level support shall be bit-accurate, i.e. the result of computations performed during simulation should match the results produced by the actual hardware. The formats (floating or fixed point) of high level data, as well as the number of bits in their respective fields, shall be modifiable during algorithm design. Modifying formats and their respective fields allows for a more efficient design space exploration. Table 2 shows the precision type of HDLMath1 and HDLMath2. HDLMath2 can handle data up to 1 Mbit in width and the precision type is defined using the "descriptor" construct.

Table 2 – Examples of precision type

	HDLMath1	HDLMath2
bit width	8, 16, 32, 64	defined using "descriptor" construct
sign	sign and unsigned	
floating point	single/double	
fixed point	using tool box	

5.4   Exception and error handling

To help optimize the implementation of mathematical algorithms, errors shall be minimized using only the necessary number of bits. Access shall also be provided to information regarding

the occurrence of overflow, underflow, maximum number of bits required, and cumulative error. Table 3 shows the overflow handling of HDLMath1 and HDLMath 2. HDLMath2 can define these using the "descriptor" construct.

Table 3 – Examples of overflow handling

	HDLMath1	**HDLMath2**
floating point	rounds to infinite value	defined using "descriptor" construct
integer	saturated with the maximum number	
fixed point	rounds to the specified number	

5.5   Multi-dimensional arrays

One- and two-dimensional arrays of any kind of data, including sparse arrays, and arithmetic and logical operations on any kind of legal combination of data shall be supported. This capability allows the implementation of all mathematical algorithms.

5.6   Mathematical functions

There shall be support for a large number of mathematical functions, such as differential equations, FFT (Fast Fourier Transform), DFT (Discrete Fourier Transform), finding eigenvalues and eigenvectors, norms and distances, finding roots of polynomials. Although all mathematical functionality can be written using the arithmetic operators, such an implementation would be slow. Figure 3 and Figure 4 show multi-dimensional arrays and mathematical functions in HDLMath1 and HDLMath2, respectively.

```
function ar_f_total = diff_math();
alpha = 1.65;
r_total_time = 0.005;
. . . . . . . . . . . . . . . . .
           ar_f_total(slice,j) = ar_f_spring(slice) +   ar_f_damper(slice) + ar_f_flux(slice);
           if (isZero)
              ar_f_total(slice,j) =     0;
           elseif (ar_f_total(slice,j)>0)
              ar_f_total(slice,j)= ar_f_total(slice,j);
           else
              ar_f_total(slice,j)   = 0;
           end
           if ((slice ~= 1) && (ar_f_total(slice,j) < 15))
              isZero = 1;
. . . . . . . . . . . . . . . . . . . . .
function dydx = vplode(t,x);
global coef;
dydx = [x(2);-(coef(2)*x(2)+coef(3)*x(1))/coef(1)];
. . . . . . . . . . . . . . . . . . . .
```

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Figure 3 – Multi-dimensional arrays and mathematical functions in HDLMath1

```
module top;
parameter real alpha = 1.65;
parameter real r_total_time = 0.005;/* seconds */
. . . . . . . . . . . . . . . . . . . . . . . . . . . . . .
ar_f_flux[slice] = 0;
ar_f_total[j][slice] = ar_f_spring[slice] + ar_f_damper[slice] + ar_f_flux[slice];
ar_f_total[j][slice] = (isZero) ? 0: ((ar_f_total[j][slice]>0)?ar_f_total[j][slice]:0);
if ((slice != 0) && (ar_f_total[j][slice] < 15)
. . . . . . . . . . . . . . . . . . . . . . . . . . . . . .
$VpLODE(order, nrEq, h, nr_pts_per_ct_coef+1,x_ct, coef, Fe_ct, y_ct, ressymb);
end
. . . . . . . . . . . . . . . . . . . . . . . . . . . . . .
```

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Figure 4 – Multi-dimensional arrays and mathematical functions in HDLMath2

5.7   Mixed numerical and symbolic computations

All the necessary processing should be performed in one execution. Users should not be burdened with passing data from a symbolic environment to a numeric environment. When performing symbolic simulation using strings, a string should be evaluated in the current context, as if it had been an expression in the numeric environment. Figure 5 shows mixed numerical and symbolic computations in HDLMath2, but HDLMath1 does not support this functional requirement.

```
/**** HDLMath1****/
syms x r;
symb1 = sin(r*x);
symb1_val = double(subs(symb1,[x r],[pi/6 pi/6]));
```

```
/**** HDLMath2****/
r = $Pi/6;
x = $Pi/6;
symbExpr1 = "$VpSin(r*x)";
$Eval(symbExpr1, val);
```

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Figure 5 – Mixed numerical and symbolic computations in HDLMath1 and HDLMath2

5.8   Feedback process

One important aspect in control system design is to analyze the effects of feedback loops on the overall system. Figure 7 shows the feedback process in HDLMath1 and HDLMath2 for Figure 6.
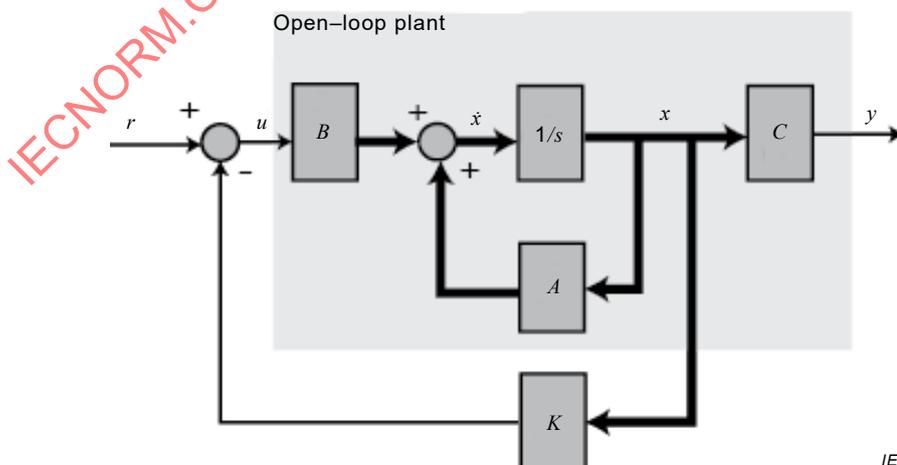
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Key

A, B, C, K matrix values

$1/s$ Laplace transform of step function

r, u, x, y variables

Figure 6 – Example of a feedback process

```
· · · · · · · · · · ·
poles = eig(A)
t = 0:0.01:2;
u = zeros(size(t));
x0 = [0.01 0 0];
sys = ss(A,B,C,0);
[y,t,x] = lsim(sys,u,t,x0);
plot(t,y)
xlabel('Time (sec)')
ylabel('Ball Position (m)')
· · · · · · · · · · ·
K = place(A,B,[p1 p2 p3]);
sys_cl = ss(A-B*K,B,C,0);
· · · · · · · · · · ·
```

```
· · · · · · · · · · · · · ·
poles = $Eig(A);
$PrintM(poles, "%e");
/* The poles are:
poles[0].Re = -3.130495e+01, poles[0].Im = 0.0
poles[1].Re = -1.000000e+02, poles[1].Im = 0.0
poles[2].Re = 3.130495e+01, poles[2].Im = 0.0
*/
· · · · · · · · · · · · · ·
K = $Place(A, B, poles);
BK = B*K;
AK = A-BK;
y = $LSim(AK, B, C, D, u, t0, dt, nr_samples, x);
· · · · · · · · · · · · · · · · · ·
```

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Figure 7 – Example of feedback process in HDLMath1 and HDLMath2

5.9   User-defined functions in C-code

Support for extending simulation functionality by having the capability to incorporate C code execution in the simulation in a standard manner is required to enhance performance.

The rationale behind this requirement is that many design teams have their own mathematical libraries and nothing else can work as well for them. In such cases, the designers can use their own libraries. Figure 8 is a user-defined C function call example in HDLMath1 and HDLMath2.

```
/****HDLMath1 ***/
static void yprime(· · · · · · · · · · · · ){
    · · · · · · · · · · · · · · ·
        yp[1]=
2*y[3]+y[0]-mus*(y[0]+mu)/(r1*r1*r1)-mu*(y[0]-mus)/(r
2*r2*r2);
    · · · · · · · · · · · · · · ·
        return;}
void mexFunction( i· · · · · · · · · · · · ){
    · · · · · · · · · · · · · · ·
        yprime(yp,t,y);
        return; }
```

```
/****HDLMath2 ***/
long tf2ssc(long file, int line,
    · · · · · · · · · · · · ·
        int sz2SS, int st2SS, int end2SS, long SS);
    · · · · · · · · · · · · ·

M = tf2ssc(b, a);        /*call C code */

    · · · · · · · · · · · · ·
```

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Figure 8 – Examples of user-defined functions in C-code in HDLMath1 and HDLMath2

5.10 Verification environment

Test benches are an essential tool in the circuit design environment. They provide a virtual environment used to verify the correctness of the design or model. The test bench capability of an HDLMath language shall include four components: input, circuit, check functions, and output. Figure 9 shows the structure of test-bench descriptions in HDLMath1 and HDLMath2.

```
***/ HDLMath1 test bench flow/***
// Description: test bench tasks, parameters
 task in_task;
 task idealOut_task;
 task Out_0_task;
    . . . . . . . . .
// Description: test bench data
    . . . . . . . . .
// Hierarchy Level: 1
    // Driving the test bench enable
    // System Clock (fast clock) and reset
    // Test-bench clock enable
    // Read the data and transmit it to the DUT
    // Read the data and transmit it to the DUT
    // Create done signal for Input data
    //Checker: Checking the data received from the
DUT.
    // Create done and test failure signal for output
data
    // Global clock enable
    . . . . . . . . . .
```

```
***/ HDLMath2 test bench flow/***
//Stimulus Generation
    . . . . . . . . . .
//Top level module of Test Bench
    //Test Bench declarations
    //Clock Generation
    //Amplitude Response Computation
    //Instantiation of Device Under Test
    // Instantiation of Modules generating Stimulus
    //Supplying Stimulus to the Device under Test
    // Getting the results from the Device under Test
    //Test Bench Controller
    //Computation and Display of Amplitude Response
    //Computation and Display of Input/Output
Spectrum
    //Display Input/Output Waveforms
    //Compute and Display Distances
    //Use of Mixed Level Assertions to compare
Results
    . . . . . . . . . .
 //Library of Elementary Modules
    . . . . . . . . . .
//Computational Unit of Device under Test
```

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Figure 9 – Structure of test-bench description of HDLMath1 and HDLMath2

6   Comparison of current HDLMath languages

Table 4 shows a comparison between current HDLMath languages based on the functional requirements for an HDLMath.

These languages support most of the functional requirements, but they still require further descriptive capabilities for larger scale designs.

HDLMath1 has bit length limitations (maximum 64 bits) and several problems from a hardware design perspective such as limitations for functional requirements 2, 3, and 4.

HDLMath2 requires more functionality such as the ability to handle feedback processes without additional C coding.

HDLMath3 is able to describe mathematical algorithms, but it needs much C coding and associated debugging.